# ▶ First Grade Unit 5: Geometry

Big Conceptual Idea: <u>K-6 Progression on Measurement and Data (Measurement Part)</u> (pp. 1-4, 8-11), <u>K-5 Progression on Geometry</u> (pp. 1-5, 8-9)

Read the Bridges <u>Unit Overview/Introduction</u> for Unit 5 pp. i-vi. Also, read each <u>Module Overview</u> for the current week's sessions, and the current <u>Session Summary</u> along with details for the teaching of each session as you work through Unit 5. These Introduction/Overview/Summary sections provide focus, clarity, vocabulary, definitions, and examples for the "big mathematical ideas and understandings" critical to 1<sup>st</sup> Grade. This information will support your professional decision-making within the Sessions and Modules as needed.

Mathematical	Essential Questions for teacher consideration:
Background:	What experiences and discussions will I provide to support students'
Read Bridges Unit 5	understanding of identifying, describing, constructing, drawing,
Overview pages (pp. i-xi)	comparing, composing, and sorting two- and three-dimensional shapes?
	Using pattern blocks, Polydrons, shape-sorting cards, and paper shapes
	how will I support understandings of components and properties of
	geometric shapes, composing and decomposing such shapes, and
	spatial structuring and spatial relations?

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1<sup>st</sup> Grade Curriculum Pacing Framework: Balanced Calendar

## Instructional note:

"If you learn something deeply, the synaptic activity will create lasting connections in your brain, forming structural pathways, but if you visit an idea only once or in a superficial way, the synaptic connections can "wash away" like pathways made in the sand." (Boaler, 2016, p. 1)

The big idea for *Unit 5* is deepening students' understandings of the attributes of two-dimensional and three-dimensional shapes, and beginning reasoning about the relationships of shapes to one another and parts of shapes to the whole. Descriptions of the Van Hiele levels of sophistication for geometric thinking are included in the *Bridges Unit 5 Introduction* (pp. 2-3). Students advance through the levels of geometric understanding as they have experiences and explore with shapes. For most of elementary school instruction students are involved with recognizing shapes, discussing shapes in terms of geometric properties, making comparisons between shapes, and beginning to reason about shapes based on their attributes. "All teachers should be aware that the experiences they provide are the single most important factor in moving children up this developmental ladder" (Van de Walle, Karp, Lovin, & Bay-Williams, 2014, p.304).

Distinction between defining and non-defining properties for two-dimensional and three-dimensional shapes are a major instructional target for 1<sup>st</sup> grade. Teachers utilize tasks or activities involving shapes to clarify the geometric terms or vocabulary students use, and continue to introduce new and more precise understanding of geometric content. Encourage students to use terminology such as edges, faces, surfaces, vertices, etc. (see definitions below), as they talk and write about their experiences with shapes. These terms are not expected to be mastered by students, but used to exposure students to precise academic terminology, thus supporting development of academic vocabulary and geometric concepts including shape attributes and properties.

Seeing relationships is a focus throughout all mathematics instruction. Developing the big idea of part-whole relationships occurred throughout the previous units. Geometry continues to support this idea of "building understanding of part-whole relationships as well as the properties of the original and composite shapes. Note that the process of combining shapes to create a composite shape is much like combining 10 ones to make 1 ten" (K-6 Progression on Geometry, 2013, p. 8). "Geometry instruction in grades pre-K-2 helps children learn more about the world they live in while also playing a significant role in supporting the development of number concepts" (Van de Walle et al., 2014, p. 299). Geometry instruction also develops "...the background for measurement and for initial understandings of properties such as congruence and symmetry" (NVACS, 2010, p. 13). Clements and Sarama state "...spatial sense can be defined as an intuition about shapes and the relationships between shapes and is considered a core area of mathematical study in the early grades" (as cited in Van de Walle et al., 2013, p. 299). For this reason, *NVACS* also identifies geometrical reasoning as one of the four critical content areas in mathematics for first grade and includes three important goals for elementary geometry: 1) geometric shapes, components, and properties; 2) composing and decomposing shapes; and 3) spatial relations and spatial structuring. These foci also include the idea, "Shapes can be moved in a plane in space without changing the shape's properties, and these movements can be described in terms of translations (slides), reflections (flips) and rotations (turns)" (Van de Walle et al., 2014, p. 299).

Support and instruct to the developmental understanding of:

**Circle**- a two-dimensional (flat) shape made by drawing a curve that is always the same distance from a point called the center.

Triangle- a two-dimensional (flat) shape with 3 sides.

Rectangle- a two-dimensional (flat) shape with 2 pairs of parallel sides (4 sides total) and 4 right angles.

Square- a two-dimensional (flat) shape with 4 congruent sides and 4 right angles.

Hexagon- a two-dimensional (flat) shape with 6 sides.

Trapezoid- a two-dimensional (flat) shape with 4 sides, exactly 1 pair of which are parallel.

Rhombus-a two-dimensional (flat) shape with 4 congruent sides.

Cube- a three-dimensional shape (solid) whose 6 faces are all squares.

Cone- a three-dimensional shape (solid) with a circular or elliptical base and a curved surface that tapers to the vertex.

**Sphere**- a three-dimensional shape (solid) constructed so that every point of the surface is the same distance from a point called the center.

Cylinder- a three-dimensional shape (solid) with one curved surface and two congruent flat ends that are circular or elliptical. Vertex/corner- the point at which the sides of a polygon, or the edges of a polyhedron meet.

**Edge**– (1) Any side of a polyhedron's faces. (2) A line segment or curve where two surfaces of a geometric solid meet. (e.g. The edge is the circular portion or circumference of the base of a cone).

**Face**– a flat surface on a 3-dimensional figure. Some special faces are called bases. More generally, any 2-dimensional surface on a 3-dimensional figure.

**Surface**– the boundary of a 3-dimensional object. The part of an object that is next to the air. Common surfaces include the top of a body of water, the outermost part of a ball, and the topmost layer of ground that covers the earth.

**Pyramid**– a polyhedron made up of any polygonal region for a base, a vertex (apex) not in the plane of the base, and all of the line segments with one endpoint at the apex and the other on an edge of the base. All faces, except perhaps the base, are triangular. Pyramids get their name from the shape of their base.

**Rectangular prism**– a prism with rectangular bases. The four faces that are not bases are either rectangles or parallelograms. For example, a brick models a rectangular prism in which all sides are rectangles.

Triangular prism – a prism whose bases are triangles.

Students explore 2-dimensional and 3-dimensional shapes and fractions (partitioning shapes into equal parts – halves and fourths and able to talk about the whole in relationship to the parts and the parts in relationship to the whole). Over time, with supportive and scaffolded instruction and interactions, students come to more precise understandings of shapes, as well as develop appropriate precision with geometric content and vocabulary. Consider the following possible misconceptions throughout the Unit:

- A trapezoid is always red (trapezoids in pattern blocks are red).
- Triangles are always equilateral (triangles in pattern blocks and on many pre-made posters are often equilateral).
- Size and orientation change the shape (triangles must be oriented with the horizontal base parallel to the bottom of the page; students consider a triangle with a horizontal base parallel to the top of the page as "upside down").
- A rhombus can be called a diamond (a diamond is not a shape, but a gemstone).
- Pattern blocks or attribute blocks are 2-D shapes (pattern blocks have thickness and are precisely 3-D; 2-D shapes can be constructed by tracing the footprint or outline of the pattern block resulting in the 2-D shape).

Consider using shapes of various colors, sizes, and orientations so students focus on defining attributes and characteristics rather than non-defining attributes.

Students also engaged in geometric activities in the October and December *Number Corner* activities. These prior experiences support students' continued work with geometry understandings during this *Unit*. Further experiences will also be continued in February *Number Corner*.

#### **On-going enrichment:**

Continue noting the *Skills Across the Grade Level* chart in the Introduction section (Unit 5 p. ix). All geometry standards for first grade are expected to be secure at the end of this *Unit*. This is important information for those day-to-day professional instructional decisions you have to make within each session as to what discussions or activities to extend or cut short or emphasize or skip or, etc. Expect all students to engage in the math.

Continue to consider "Support" and "Challenge" options within each *Session*, and "Game Variations", "Differentiate", and "English-Language Learners" ideas in *Work Places*.

	I Academic Vocabulary ords consistently during instruction.	
New Academic Vocabulary: (first time explicitly taught) *indicates Word Resource Cards are available in the Bridges materials	Review Academic Voca (Vocabulary from Number Corner of	
Side*	Attribute*	Pyramid*
Net	Add*	Quarter (one fourth)
Fraction*	Addition	Rectangle*
	Circle*	Rectangular prism*
	Compare*	Rhombus*
	Cone*	Rotate/Turn
	Cube*	Solid
	Cylinder*	Sphere*
	Edge*	Square*
	Equal*/the same as	Tally
	Equation*	Third*
	Face*	Trapezoid*
	Flat	Triangle*
	Fourth*	Triangular prism*
	Half*	Two-Dimensional shape (2-D)*
	Hexagon*	Three-Dimensional shape (3-D)*
	Parallel Lines	Vertex or Corner

Additional terminology that students might need support with: actual, actually, curved, identify, information, problem solving, strategies, plus, predict, prediction, slide (move over)

## \*Collaborative Team Conversations (CTC)

Consider using *one* of the following as part of the formative assessment process at the lesson level to **collect student work** to analyze for <u>evidence of mathematical understanding</u>:

#### Guiding question:

"What language are students using to identify, describe, and justify their understandings of 2-D and 3-D shapes (names, defining attributes)?" "How are students able to compare and decompose shape compositions to identify shapes that are not included?"

"How are students partitioning shapes into smaller portions?"

"How are students composing smaller shapes to make a new shape?"

"If needed, what intensification interactions will support the understanding geometry vocabulary, concepts and/or spatial reasoning skills?"

	Evidence	Look for
Shapes Checkpoint TG pp. 22-24	Shapes Checkpoint observation and student record sheet (TG U5M2S5 p. T6-T7) Shapes Checkpoint Scoring Guide (AG Bridges Unit Assessments pp. 49- 51)	<ul> <li>Focus CTC around conceptual understandings of the big idea and strategies used:</li> <li>understanding and using precise names of 2-D and 3-D shapes (see Essential Academic Vocabulary table above)</li> <li>understanding and using precise and defining attributes of 2-D and 3-D shapes (see Essential Academic Vocabulary table above)</li> <li>comparing and visually recognizing differences groups of shapes</li> </ul>
Unit 5 Assessment, Part 1 & Part 2 #5, 6, 7, 8 ( TG. pp. 27-29, 33-34	Unit 5 Assessment, Part 1 & Part 2 #5, 6, 7, 8 observations and student record sheet (TG U5M3S5 p. T12-T13) Unit 5 Assessment, Part 1 & Part 2 #5, 6, 7, 8 Scoring Guide #5, 6, 7, 8 (AG Bridges Unit Assessments pp. 54- 55, 57)	<ul> <li>Focus CTC around conceptual understandings of the big idea and strategies used:</li> <li>using precision and accuracy in identifying attributes</li> <li>identifying fourths and halves</li> <li>understanding the size of parts gets smaller with more parts</li> <li>composing a shape with smaller shapes</li> <li>using a variety of shapes in different placements</li> </ul>

Learning Cycle	No other assessment at this time	
Assessments (summative)		

Standards listed in **bold** indicate a focus of the lesson.

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NVACS (Content and Practices)	Mathematical Development of the Big Idea	Instructional Clarifications & Considerations
Module 1- Se	ssion 1: What's in the Box?	
1.MD.4 1.G.1 MP.1 MP.7	<ul> <li>Access Prior Learning:</li> <li>Kindergarten student worked on correctly naming shapes regardless of their orientations or overall size.</li> <li>Securing the Big Idea and key Strategic Behaviors:</li> <li>identifying 2-D shapes</li> <li>analyzing and describing 2-D shapes by defining and non- defining attributes</li> </ul>	<ul> <li>Guiding Questions:</li> <li>What are shapes?</li> <li>How can you organize shapes?</li> <li>How can you describe shapes?</li> <li>Instructional Notes:</li> <li>Consider sending the <i>Family Letter</i> home. Find it <u>here</u>.</li> <li>Consider starting a KWL chart to pre-assess the misconceptions that students might have about shapes. Do not correct these misconceptions at this time but use this chart to inform classroom discussions and discoveries throughout the unit.</li> <li>The <u>pattern block web app</u> can be useful throughout this unit.</li> <li>Although the teacher's guide appears to have "scripted" responses, the sessions are not intended to be taught as a scripted lesson. The suggested conversations are to showcase how</li> </ul>
		<ul> <li>student misconceptions about shapes might be dealt with through student discourse. They are also a guide of how to respond to student misconceptions while protecting the class culture of inquiry-based learning and risk taking.</li> <li>This lesson addresses two student misconceptions: size and color, which are non-defining attributes.</li> <li>Pay particular attention to the note on page 6 in regards to rectangles and squares.</li> <li>Child Watching:</li> <li>Identify students who think that a shape's color or size is a defining attribute. Address this through questioning and classroom discourse techniques.</li> </ul>
Module 1- Sea	ssion 2: Shape Sorting with Attril	
	Access Prior Learning:	Guiding Questions:
1.MD.4 <b>1.G.1</b>	<ul> <li>Kindergarten student worked on correctly naming shapes regardless of their orientations or overall size.</li> </ul>	<ul> <li>What are shapes?</li> <li>How can you organize shapes?</li> <li>How can you describe shapes?</li> </ul>
MP.4 MP.7	<ul> <li>Connect to previous geometry discussions.</li> <li>Securing the Big Idea and key Strategic Behaviors: <ul> <li>identifying 2-D shapes</li> <li>analyzing and sorting 2-D shapes by defining and non-defining attributes</li> </ul> </li> </ul>	<ul> <li>Instructional Notes:</li> <li>Some students might believe triangles need to be equilateral or have a horizontal base parallel to the bottom of the page. Expose students to a variety of triangles, such as isosceles and scalene triangles, and in various orientations. Students do not need to know the terms isosceles and scalene.</li> <li>This lesson adds geometry vocabulary to describe shapes by straight and curved sides and closed shapes with no holes or gaps.</li> <li>Allow misconceptions to present themselves for rich classroom discussion. Making a statement like "color doesn't matter" before students have a chance to discuss their thoughts can limit discussion and student growth. Discovery through experience and classroom discussion fosters growth, as opposed to direct explanation. "Students with a growth mindset have more positive brain activity when they make mistakes, with more brain regions lighting up and more attention to and correcting of errors." (Moser et al., 2011, pp. 1484-1489).</li> <li>Enrichment:</li> <li>See <i>Extension</i> in the margin (p. 16).</li> <li>Child Watching:</li> <li>Observe for the following misconceptions about shapes: color, size, orientation, leaving gaps or curved edges on drawings, only equilateral triangles are triangles.</li> </ul>
Module 1- Se	ssion 3: Last Shape in Wins	
1.G.1 1.G.2 MP.1 MP.7	<ul> <li>Access Prior Learning:</li> <li>Kindergarten student worked on correctly naming shapes regardless of their orientations or overall size.</li> <li>Connect to previous geometry discussions.</li> </ul>	<ul> <li>Guiding Question:</li> <li>How can you make shapes from other shapes?</li> <li>Instructional Notes:</li> <li>The online digital <i>Work Place</i> game: Last Shape In Wins is provided on the Educator Site.</li> <li>See the <i>Work Place Sentence Frames</i> for Unit 5 <u>here</u>.</li> <li>These sessions contain critical geometry vocabulary. Utilize, post and review the Vocabulary Resource Cards.</li> <li>Read the Math Practices in Action in the margin (p. 22).</li> <li>Students may discover that some of the pattern block shapes take up more area than others which supports understanding of composing or decomposing shapes.</li> </ul>
		-continues on next page-

	Securing the Big Idea and key Strategic Behaviors:	<ul> <li>Enrichment:</li> <li>See the Game Variations on Work Place Instructions (p. T5).</li> </ul>
	<ul> <li>identifying 2-D shapes</li> <li>analyzing 2D shapes</li> <li>composing new shapes using 2-D shapes</li> </ul>	<ul> <li>Child Watching:</li> <li>Identify students unsure of the names of the shapes or having difficulty telling them apart (see p. T4 for support).</li> </ul>
Nodule 1- Se	ession 4: Pattern Block Puzzles: H	low Many Ways?
	Access Prior Learning:	Guiding Question:
1.G.1	Kindergarten student worked on	How can you make shapes from other shapes?
1.G.2	correctly naming shapes	
MP.7	regardless of their orientations or overall size.	<ul> <li>Instructional Notes:</li> <li>The online digital Work Place game: Pattern Block Puzzles is provided on the Educator Site.</li> <li>The idea of 3 triangles fitting into a trapezoid shape begins building the idea of parts and</li> </ul>
WP.7	Connect to previous geometry discussions.	wholes.
	Securing the Big Idea and key Strategic Behaviors:	See the Assessment and Differentiation Chart on Work Place Guide (p. T6).
	<ul> <li>identifying 2-D shapes</li> </ul>	Child Watching:
	<ul> <li>analyzing 2D shapes</li> </ul>	<ul> <li>Identify students unsure of the names of the shapes or having difficulty telling them apart (See</li> </ul>
	<ul> <li>composing new shapes using 2-D shapes</li> </ul>	p. T6 for support).
Nodule 1- Se	ession 5: There's a Shape in My F	Pocket
	Access Prior Learning:	Guiding Question:
1.G.1	Kindergarten student worked on	How do attributes help you identify and sort shapes?
1.G.2	correctly naming shapes	
1.0.2	regardless of their orientations or	Instructional Notes:
	overall size.	<ul> <li>Address the misconception that a rhombus is a diamond by reinforcing that a diamond is a type of each and each actions.</li> </ul>
MP.1	Connect to previous geometry	of rock and not a shape.
MP.7	discussions.	<ul> <li>A square is both a rhombus and a rectangle.</li> <li>Even thembus is a kite bayever not even kite is a thembus. A thembus is an equilatoral with</li> </ul>
	Securing the Big Idea and key	<ul> <li>Every rhombus is a kite, however, not every kite is a rhombus. A rhombus is an equilateral with all four sides equal in length. A kite has two pairs of adjacent side equal in length, but not equa to each other.</li> </ul>
	Strategic Behaviors:	
	<ul> <li>identifying 2-D shapes</li> </ul>	Enrichment:
	<ul> <li>analyzing and sorting 2-D</li> </ul>	• See the <i>Extension</i> activity in margin (p. 38).
	shapes by defining and non-	Child Watching:
	defining attributes	
	3	<ul> <li>Observe how students are describing shapes. Are they beginning to use vocabulary such as sides and vertices? Are they beginning to gain confidence in naming shapes?</li> </ul>
lodulo 2 C	accion 1. Shana Dataatiyaa	sides and venices? Are they beginning to gain connuence in naming snapes?
1000le 2- 30	ession 1: Shape Detectives	Cuiding Question
1.G.1	<ul><li>Access Prior Learning:</li><li>Kindergarten students described</li></ul>	<ul><li>Guiding Question:</li><li>Where do you find 3-D shapes?</li></ul>
	2-D and 3-D objects in the	Instructional Notes:
MP.7	environment using names of	Read the About This Session in the margin (p. 4).
1411 ./	shapes regardless of size or	• A two-dimensional shape is the line segments which form the shape lying in a plane. When yo
	orientation.	cut out a shape from paper, mathematically that shape then has depth and is three-
	Connect to all previous geometry	dimensional. Consider for this lesson just drawing a circle (or rectangle) on a piece of paper as
	discussions.	opposed to actually cutting it out.
	Coording the Dig Ideo and Korr	In early development students may confuse many actual three-dimensional shapes with narror
	Securing the Big Idea and key	depth as "flat" or two-dimensional. Bridges actually uses pattern blocks in Kindergarten as 2-
	Strategic Behaviors:	dimensional shapes. To clarify, if you trace around these shapes the "footprint" that results will actually be the two-dimensional shape.
	identifying 3-D shapes	<ul> <li>Conversation around the image of the three dimensional shape on the card might need to</li> </ul>
	analyzing 3-D shapes by	occur. Show how the artist tries to represent all the sides in the image but address the fact tha
	defining and non-defining	an artist cannot show all the sides at one time on the paper, just as your eyes cannot see all
	<ul><li>attributes</li><li>locating 3-D shapes in the</li></ul>	sides of the solid cube at one time either, but the sides are still there. Also, the artist shows a sphere as 3-dimensional by drawing or shading a shadow to show depth.
	environment	
		<ul> <li>Enrichment:</li> <li>See the <i>Extension</i> activity in margin (p. 6).</li> </ul>
		Enrichment:

Module 2- Se	ession 2: Mystery Bag Sorting	
	Access Prior Learning:	Guiding Questions:
1.G.1	Kindergarten students identified	What do you see that is the same or different?
1.MD.4	and described shapes by	What attributes do you already know about?
1.IVID.4	attributes.	
	Connect to all previous geometry	Instructional Notes:
MP.7	discussions.	• Read the <i>Math Practices in Action</i> in the margin (p. 9).
MP.8	013003310113.	<ul> <li>Encourage the use of accurate and precise geometry vocabulary.</li> </ul>
WI .0	Securing the Big Idea and key	Consistently expose students to precise vocabulary by repeating what students might say with
	Strategic Behaviors:	precise language.
	<ul> <li>identifying 3-D shapes</li> </ul>	Enrichment:
	<ul> <li>analyzing 3-D shapes by</li> </ul>	See the <i>Extension</i> activity in margin (p. 10).
	defining and non-defining	
	attributes	Child Watching:
	<ul> <li>locating 3-D shapes in the</li> </ul>	<ul> <li>Identify students using accurate vocabulary to describe the shape attributes.</li> </ul>
	environment	
Module 2- Se	ession 3: Shape Walk	
	Access Prior Learning:	Guiding Questions:
1.G.1	Kindergarten students described	What 3-D shapes do you see around you?
1.MD.4	2-D and 3-D objects in the	What do you notice that is the same or different?
1.IVID.4	environment using names of	
	shapes regardless of size or	Instructional Notes:
MP.7	orientation.	Model precise mathematical language for students to hear. Students,
MP.8	Connect to all previous geometry	however, are not expected to use formal names such as "right circular cylinder."
	discussions.	<ul> <li>Students are likely to generalize shapes in the real world which could result in misconceptions. For example, they might select a water bottle as a cylinder.</li> </ul>
		Mathematically a plastic water bottle with hourglass curved face and/or ridges
	Securing the Big Idea and key	is not truly a cylinder. Use students' generalizations as an opportunity to
	Strategic Behaviors:	discuss the precise attributes by posing a question such as, "What attributes
	<ul> <li>identifying 3-D shapes</li> </ul>	does this water bottle have that make you say it is a cylinder?" Honor student
	<ul> <li>analyzing 3-D shapes by</li> </ul>	thinking and discovery, while pointing out the attributes (such as the lip on the
	defining and non-defining	lid, or the ridges) that make it a non-example.
	attributes	Place 3-dimensional solids next to the object for Cylinder Cylinder
		comparison. There are many types of water bottles in a school setting. Some of them will be true (right
		in a school setting. Some of them will be true (right circular) cylinders and some may not be. See
		pictures.
		• A straw is another non-example of a cylinder because it does not have bases. Other non-
		examples of right circular cylinders include soda cans and some containers of canned food.
		The standard states: 1.G.2- Compose 2-D or 3-D
		shapes (cubes, right rectangular prisms, right circular
		cones, and right circular cylinders) (NVACS, 2010).
		There are other types of cylinders and cones. It is not necessary to name them or have students identify them.
		It is only necessary for them to distinguish the attributes
		that make a true right-circular cylinder and identify when
		a solid is a non-example.
		• Non-examples for right circular cones include: traffic cones (it has a lip), ice cream cones (it has
		no base), party hat (it has no base), and teepee (no base and not a culturally responsive
		example).
		Validate students reasoning of approximate objects but provide accurate and precise language     and approximate objects but provide accurate and precise language
		and concepts within the discussion. Spend time addressing why a shape doesn't meet the
		criteria. Perhaps the Shape Walk becomes more of a "Finding the Rare Shape Hunt" and a celebration occurs if an accurate example is found.
		Enrichment:
		• See the <i>Extension</i> activity in margin (p. 13).
		Child Watching:
		<ul> <li>Identify students using imprecise vocabulary to describe the shape attributes and extend</li> </ul>
		<ul> <li>Identity students using imprecise vocabulary to describe the shape attributes and extend precise vocabulary when appropriate.</li> </ul>
		<ul> <li>Identify students finding non-examples of the solids help them discover the different attributes</li> </ul>
		that make it a non-example.

<ul> <li>Access Prior Learning:</li> <li>Kindergarten students composed simple 2-D shapes to form larger shapes.</li> <li>Connect to all previous geometry discussion</li> </ul>	<ul> <li>Guiding Question:</li> <li>What does a cube look like and feel like?</li> <li>Instructional Notes:</li> <li>Consider including an orange pattern block in this session. Although an orange pattern block is</li> </ul>
<ul><li>simple 2-D shapes to form larger shapes.</li><li>Connect to all previous geometry</li></ul>	Instructional Notes:
<ul><li>shapes.</li><li>Connect to all previous geometry</li></ul>	
Connect to all previous geometry	
	and the second second second second in the second in the second in the second in the second second in the second s
	actually a rectangular prism, it has two square faces and can be easily confused with a cube.
discussions.	Capitalize on the opportunity to discuss the differences.
	• A unifix cube is a non-example of a cube due to the protruding affixation feature and the open
Securing the Big Idea and key	face.
Strategic Behaviors:	
<ul> <li>identifying 3-D shapes</li> </ul>	Enrichment:
<ul> <li>analyzing 3-D shapes by</li> </ul>	Work Place Guide Assessment & Differentiation chart (p. T1).
defining and non-defining	Child Watching:
attributes	Identify students using imprecise vocabulary to describe the shape attributes and extend
<ul> <li>constructing 3-D shapes</li> </ul>	precise vocabulary when appropriate.
ssion 5: Four Triangles & One Sq	
Access Prior Learning:	Guiding Question:
Kindergarten students composed	How do you make a 3-D shape?
simple 2-D shapes to form larger	Jacoba selfore el Mada a
shapes.	Instructional Notes:
<ul> <li>Connect to all previous geometry</li> </ul>	<ul> <li>Although students will be building pyramids with 4 triangles and a square, pyramids can be made with other shapes as the base.</li> </ul>
sessions.	<ul> <li>Polydrons are mathematically not 3-D shapes themselves. Support students with any</li> </ul>
	confusions with this use of materials.
Securing the Big Idea and key	• The Assessment Binder under the Bridges Unit Assessment tab provides the scoring guide for
Strategic Behaviors:	this checkpoint (p. 51).
<ul> <li>identifying 3-D shapes</li> </ul>	• Read the Math Practices in Action in the margin (p. 26).
	<ul> <li>Kindergarten students had limited exposure to pyramids, so this content will be new information</li> </ul>
attributes	Enrichment:
<ul> <li>constructing 3-D shapes</li> </ul>	• See the <i>Extension</i> activity in margin (p. 26).
5 1	Child Watching:
	<ul> <li>Use the scoring guide to assess students and inform your instruction.</li> </ul>
ssion 1: Nine-Patch Inventions	
Access Prior Learning:	Guiding Questions:
<ul> <li>Activate prior knowledge about</li> </ul>	How can a grid represent an equation?
quilts, by perhaps bringing in an	How many equations do you think you can make from the same grid colored differently?
example, or showing images.	Instructional Notaci
	<ul> <li>Instructional Notes:</li> <li>Make a deliberate connection to part/whole relationships with addition and subtraction</li> </ul>
	equations and the idea that shapes can also be composed of parts that can make a whole
•	shape when put together, or when decomposed can be parts of a whole shape. This supports
	the part/whole reasoning students are developing.
shapes	• There are various suggested literature connections listed on p. 4 that can be read to the class to
	build background knowledge of quilting.
•	Child Watching
<ul> <li>writing equations</li> </ul>	Child Watching:
sion 2: Nine-Patch Mini-Ouilte	Identify students making connections to the parts and wholes (e.g. 3 and 6 both parts of 9).
	Guiding Questions:
9	<ul> <li>How many different patterns do you think we can make with our quilt squares?</li> </ul>
	<ul> <li>What happens when you change the pattern around?</li> </ul>
example, or show images.	Instructional Notes:
Developing the Big Idea and key	• Read the About This Session in the margin (p. 8).
	Emphasize Math Practice 7 in this lesson and support students in looking for and making use of
	structure.
shapes	<ul> <li>"As students combine shapes, they continue to develop their sophistication in describing</li> </ul>
<ul> <li>using and making sense of</li> </ul>	geometric attributes and properties and determine how shapes are alike and different, building
	foundations for measurement and initial understandings of properties such as congruence and
structure	symmetry" (K-5 Progression on Geometry, pp. 8-9).
	Strategic Behaviors: identifying 3-D shapes analyzing 3-D shapes by defining and non-defining attributes constructing 3-D shapes Ssion 5: Four Triangles & One So Access Prior Learning: Kindergarten students composed simple 2-D shapes to form larger shapes. Connect to all previous geometry sessions. Securing the Big Idea and key Strategic Behaviors: identifying 3-D shapes analyzing 3-D shapes by defining and non-defining attributes constructing 3-D shapes sosion 1: Nine-Patch Inventions Access Prior Learning: Activate prior knowledge about quilts, by perhaps bringing in an example, or showing images. Developing the Big Idea and key Strategic Behaviors: composing a new pattern from shapes understanding part/whole relationship writing equations ssion 2: Nine-Patch Mini-Quilts Access Prior Learning: Activate prior knowledge about quilts, perhaps bring in an example, or show images. Developing the Big Idea and key Strategic Behaviors: Activate prior knowledge about quilts, perhaps bring in an example, or show images. Developing the Big Idea and key Strategic Behaviors: Activate prior knowledge about quilts, perhaps bring in an example, or show images. Developing the Big Idea and key Strategic Behaviors: Activate prior knowledge about quilts, perhaps bring in an example, or show images. Developing the Big Idea and key Strategic Behaviors: Composing a new pattern from

Module 3- Se	ession 3. Sandwich Fractions	
<u>Module 3- Se</u> 1.G.1 <b>1.G.3</b> МР.6 МР.7	<ul> <li>Access Prior Learning:</li> <li>Kindergarten students were not exposed to fractional parts, only the idea of composing shapes with smaller shapes.</li> <li>Securing the Big Idea and key Strategic Behaviors:</li> <li>partitioning shapes into smaller equal fractional pieces – halves and fourths</li> <li>understanding part/whole relationship</li> </ul>	<ul> <li>Guiding Questions:</li> <li>What do you know about sharing?</li> <li>Do you ever have to share?</li> <li>Instructional Notes:</li> <li>Read the Math Practices in Action in the margin (p. 15).</li> <li>*students learn to intentionally compose and decompose plane and solid figures building an understanding of part-whole relationships as well as the properties of the original and composite shapes" (K-5 Progression on Geometry, p. 8).</li> <li>Precision is important when thinking about parts having to be exactly the same.</li> <li>In 2<sup>nd</sup> grade students will explore that halves do not need to be the same shape to represent the same area. Halves shaped like triangles and halves shaped like rectangles are both still the same area. Halves shaped like triangles and halves shaped like rectangles are both still the same area. Halves shaped like triangles and halves shaped like rectangles are both still the same amount if the whole is the same.</li> <li>Research suggests "starting work with fractions using words and not symbolsThis approach of using words rather than symbols emphasizes that <i>one hall on ore fourth</i> is one number. This is an important foundation for ensuring that subsequent work in fractions is well grounded" (Small, 2014, p. 8). Therefore, when labeling and naming fractions, use the word labels (one-fourth, one hall) and do not introduce the symbol (1/4 or 1/2). It is not necessary at this time for students to understand fraction notation. "Fraction symbolism: Let children first focus on making sense of fractions without the complication of also trying to make sense of fractions by teaching them to think of one fourth as 1 "out of" 4. This creates the idea that 1 and 4 are two separate numbers and that there are 4 wholes, when a fraction represents parts of a one whole. The standards stale, "describe the shares using the words halves, fourths, and quarters, and use the phrases half of, fourth of, and quarter of. Describe the whole as two of, or four of the shares" (NVACS, 2010, 1.G.</li></ul>
		<ul> <li>Child Watching:</li> <li>Identify students' struggling with precision resulting in sizes that are not equal.</li> </ul>
Module 3- Se 1.G.1 <b>1.G.3</b> MP.4 MP.7	<ul> <li>Access Prior Learning:</li> <li>Kindergarten students were not exposed to fractional parts, only the idea of composing shapes with smaller shapes.</li> <li>Securing the Big Idea and key Strategic Behaviors:</li> <li>partitioning shapes into smaller equal fractional pieces         <ul> <li>halves and fourths</li> <li>understanding part/whole relationship</li> </ul> </li> </ul>	<ul> <li>Guiding Question:</li> <li>How can you equally share a pizza?</li> <li>Instructional Notes:</li> <li>See the notes above about fraction labeling. Even though the materials suggest labeling the parts with ½ or ¼, consider labeling these with the words "one-half" or "one-fourth," not the symbols.</li> <li>Reinforce the idea of fractions as numbers by counting them using the language one-fourth, two-fourths, three-fourths, four-fourths.</li> <li>Encourage students to attend to precision as they cut.</li> <li>Pieces of pizza are not triangles due to the curved edge. If this comes up, consider showing students a triangle shape and compare it with the slice of pizza to highlight the differences. Reinforce "one-fourth" as the label you have given the piece, a one-fourth slice.</li> <li>Enrichment:</li> <li>See Step 12 (p. 20).</li> <li>Child Watching:</li> <li>Observe for students' use of precise language.</li> </ul>

	ession 5: Fraction Bingo	
	Access Prior Learning:	Guiding Question:
1.G.3	Kindergarten students were not	What patterns do you notice?
	exposed to fractional parts, only the idea of composing shapes	Instructional Note:
MP.2	with smaller shapes.	• The fraction bingo cards do have the symbol ( $\frac{1}{2}$ , etc.) written on the cards. This is appropriate
MP.7	with smaller shapes.	for student exposure, however, consider adding the fraction words ( <i>one-half</i> or <i>halves, etc.</i> ) to
	Securing the Big Idea and key	support the standard expectation.
	Strategic Behaviors:	Enrichment:
	<ul> <li>partitioning shapes into</li> </ul>	• See the <i>Extensions</i> in the margin (p. 24).
	smaller equal fractional pieces	
	<ul> <li>halves and fourths</li> </ul>	Child Watching:
	<ul> <li>understanding part/whole</li> </ul>	<ul> <li>Identify students' use of precise language. Are they counting fractional parts with the terms one half, two-halves?</li> </ul>
	relationship	Observe for understanding of the "whole." You can assess this by frequently asking, "What is
		the whole?"
Module 3- Se		Part 1 & Part 2 (spread over 2 days)
	Access Prior Learning:	Instructional Notes:
1.G.1	Kindergarten students were not	<ul> <li>The Assessment Guide under the Bridges Unit Assessmentst tab provides the scoring guide for Unit 5 Assessment (p. 56).</li> </ul>
1.G.2	exposed to fractional parts, only	<ul> <li>The Grade 1 Assessment Map in the Assessment Binder under the Overview tab (pp. 13-15)</li> </ul>
1.G.3	the idea of composing shapes	identifies the Geometry Standards targeted for mastery (secure understandings). If students ar
	with smaller shapes.	still struggling, consider using the next module as time to provide intensification, and support.
MP.1	Securing the Big Idea and key	April Number Corner will also revisit these standards.
MP.2	Strategic Behaviors:	Child Watching:
MP.7	<ul> <li>identifying 2 and 3-D shapes</li> </ul>	Use the Scoring Guide to inform your instruction. If any students are not secure, consider
	<ul> <li>composing and decomposing</li> </ul>	pulling for small group support throughout the next week.
	shapes	
	<ul> <li>partitioning shapes into smaller</li> </ul>	
	equal fractional pieces – halves	
	and fourths	
	<ul> <li>understanding part/whole</li> </ul>	
	relationship	
Module 4- Se	ession 1: Shape Riddles	
	Access Prior Learning:	Guiding Questions:
1.G.1	• The previous sessions have	<ul><li>What do you know about these shapes?</li><li>How are they the same and different?</li></ul>
	provided students with many	<ul> <li>What does eliminate mean?</li> </ul>
MP.1	shape experiences that they will	
MP.7	draw upon during this lesson.	Instructional Note:
	Securing the Big Idea and key	The online digital resource for this work place, Shape Riddles is provided on the Educator Site
	Strategic Behaviors:	Enrichment:
	• identifying 2-D shapes	See Assessment & Differentiation Chart on the Work Place Guide (p. T3).
	analyzing 2-D shapes by	
	defining attributes	Child Watching:
		<ul> <li>Observe for the language students use when discussing shapes. Begin thinking about which students are in Van High Lovel 0 and describing shapes as "bayes" or "isides." Observe which</li> </ul>
		students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which
		students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes
		<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue</li> </ul>
		<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue Identify students who are confused with the language and possibly eliminate triangles when th</li> </ul>
Modula 4		<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue</li> <li>Identify students who are confused with the language and possibly eliminate triangles when the prompt is "My shape has 3 straight sides."</li> </ul>
Module 4- Se	ession 2: Shape Sorting & Graphir	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue Identify students who are confused with the language and possibly eliminate triangles when the prompt is "My shape has 3 straight sides."</li> </ul>
	Access Prior Learning:	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue Identify students who are confused with the language and possibly eliminate triangles when th prompt is "My shape has 3 straight sides."</li> <li>Guiding Question:</li> </ul>
1.G.1	<ul><li>Access Prior Learning:</li><li>The previous sessions provided</li></ul>	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue Identify students who are confused with the language and possibly eliminate triangles when th prompt is "My shape has 3 straight sides."</li> </ul>
	<ul> <li>Access Prior Learning:</li> <li>The previous sessions provided students with many shape</li> </ul>	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue Identify students who are confused with the language and possibly eliminate triangles when th prompt is "My shape has 3 straight sides."</li> <li>Guiding Question:</li> <li>How many different ways can you sort shapes?</li> </ul>
1.G.1 <b>1.MD.4</b>	<ul> <li>Access Prior Learning:</li> <li>The previous sessions provided students with many shape experiences that they will draw</li> </ul>	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue Identify students who are confused with the language and possibly eliminate triangles when th prompt is "My shape has 3 straight sides."</li> <li>Guiding Question: <ul> <li>How many different ways can you sort shapes?</li> </ul> </li> <li>Instructional Notes: <ul> <li>Read the Math Practices in Action in the margin (p. 9).</li> </ul> </li> </ul>
1.G.1 1.MD.4 MP.1	<ul> <li>Access Prior Learning:</li> <li>The previous sessions provided students with many shape experiences that they will draw upon during this lesson.</li> </ul>	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue.</li> <li>Identify students who are confused with the language and possibly eliminate triangles when the prompt is "My shape has 3 straight sides."</li> <li>Guiding Question:</li> <li>How many different ways can you sort shapes?</li> <li>Instructional Notes:</li> <li>Read the <i>Math Practices in Action</i> in the margin (p. 9).</li> <li>Consider asking students to do an open sort of their shapes before using the Shape Sorting &amp;</li> </ul>
1.G.1 1.MD.4	<ul> <li>Access Prior Learning:</li> <li>The previous sessions provided students with many shape experiences that they will draw upon during this lesson.</li> <li>Students engaged in sorting and</li> </ul>	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue.</li> <li>Identify students who are confused with the language and possibly eliminate triangles when the prompt is "My shape has 3 straight sides."</li> <li>Guiding Question:</li> <li>How many different ways can you sort shapes?</li> <li>Instructional Notes:</li> <li>Read the <i>Math Practices in Action</i> in the margin (p. 9).</li> </ul>
1.G.1 1.MD.4 MP.1	<ul> <li>Access Prior Learning:</li> <li>The previous sessions provided students with many shape experiences that they will draw upon during this lesson.</li> <li>Students engaged in sorting and graphing in the previous unit with</li> </ul>	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue.</li> <li>Identify students who are confused with the language and possibly eliminate triangles when the prompt is "My shape has 3 straight sides."</li> <li>Guiding Question:</li> <li>How many different ways can you sort shapes?</li> <li>Instructional Notes:</li> <li>Read the <i>Math Practices in Action</i> in the margin (p. 9).</li> <li>Consider asking students to do an open sort of their shapes before using the Shape Sorting &amp;</li> </ul>
1.G.1 1.MD.4 MP.1	<ul> <li>Access Prior Learning:</li> <li>The previous sessions provided students with many shape experiences that they will draw upon during this lesson.</li> <li>Students engaged in sorting and</li> </ul>	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue.</li> <li>Identify students who are confused with the language and possibly eliminate triangles when the prompt is "My shape has 3 straight sides."</li> <li>Guiding Question:</li> <li>How many different ways can you sort shapes?</li> <li>Instructional Notes:</li> <li>Read the <i>Math Practices in Action</i> in the margin (p. 9).</li> <li>Consider asking students to do an open sort of their shapes before using the Shape Sorting &amp; Graphing Record Sheet which limits their sorting to only 2 categories.</li> </ul>
1.G.1 <b>1.MD.4</b>	<ul> <li>Access Prior Learning:</li> <li>The previous sessions provided students with many shape experiences that they will draw</li> </ul>	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe whic students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue Identify students who are confused with the language and possibly eliminate triangles when the prompt is "My shape has 3 straight sides."</li> <li>Guiding Question: <ul> <li>How many different ways can you sort shapes?</li> </ul> </li> <li>Instructional Notes: <ul> <li>Read the Math Practices in Action in the margin (p. 9).</li> </ul> </li> </ul>
1.G.1 1.MD.4 MP.1	<ul> <li>Access Prior Learning:</li> <li>The previous sessions provided students with many shape experiences that they will draw upon during this lesson.</li> <li>Students engaged in sorting and graphing in the previous unit with</li> </ul>	<ul> <li>students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe whic students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue Identify students who are confused with the language and possibly eliminate triangles when the prompt is "My shape has 3 straight sides."</li> <li><b>Guiding Question:</b></li> <li>How many different ways can you sort shapes?</li> <li><b>Instructional Notes:</b></li> <li>Read the <i>Math Practices in Action</i> in the margin (p. 9).</li> <li>Consider asking students to do an open sort of their shapes before using the Shape Sorting &amp; Graphing Record Sheet which limits their sorting to only 2 categories.</li> </ul>

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	<ul> <li>Securing the Big Idea and key Strategic Behaviors:</li> <li>analyzing and sorting shapes by defining attributes</li> <li>analyzing graphs and data</li> </ul>	<ul> <li>Child Watching:</li> <li>Observe for the language students use when discussing shapes. Begin thinking about which students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they label the columns and generate sorting categories.</li> </ul>
Module 4- Se	ession 3: More Shape Riddles	
<b>1.G.1</b> MP.1 MP.7	<ul> <li>Access Prior Learning:</li> <li>The previous sessions provided students with many shape experiences that they will draw upon during this lesson.</li> <li>Connect to Session 1.</li> </ul>	Guiding Questions:         • What do you know about these shapes?         • How are they the same and different?         • What does eliminate mean?         Enrichment:         • Encourage students to create their own riddles for others.
	<ul> <li>Securing the Big Idea and key Strategic Behaviors:</li> <li>analyzing 2-D shapes by defining attributes</li> <li>sorting shapes by defining attributes</li> </ul>	<ul> <li>Child Watching:</li> <li>Observe the language students use when discussing shapes. Begin thinking about which students are in Van Hiele Level 0 and describing shapes as "boxes" or "icicles." Observe which students are in Van Hiele Level 1 and are using the language of geometry, describing shapes by their attributes.</li> <li>Observe student reasoning and deduction skills as they eliminate shapes that don't fit the clue.</li> </ul>

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