Curriculum is one component of a larger mathematics instructional program in Washoe County School District (WCSD) for Kindergarten through $5^{\text {th }}$ grade students. The purpose of curriculum guides are to bridge the district's K-5 Philosophy of Mathematics Education with the Nevada Academic Content Standards (NVACS) through a connection of the Curriculum Pacing Frameworks, instructional materials (Bridges in Mathematics or enVisionmath2.0), research based instructional practices and clarification of the standards when necessary. The following describes a course of study for the specified grade for one year. $\underline{A L L}$ students must receive quality instruction in $\underline{A L L}$ grade level standards in one instructional year.

This guide is designed to be used with the instructional materials during planning. This guide is not meant to supplant any portion of the instructional materials. Teachers will continue to read through Units/Topics during instructional planning.

## Guide language:

Throughout the guide the following language is used to describe the level of understanding expected at the lesson level. This language is found in the lesson-by-lesson section in the column labeled "Big Idea Mathematical Development".

Beginning: Indicates students' initial explorations with the mathematical idea(s) explored in the lesson. Instruction continues to the next lesson.

Developing: Students have worked with the mathematical ideas in previous grades or previously during the year. The focus of the lesson is to connect and build student understanding. Teachers provide intensified support to students who may exhibit misconceptions, partial understanding, no or limited understanding. Instruction continues to the next lesson.

Secure: Indicates that students have worked previously with these ideas and are expected to be at a level of secure understanding. Students with secure understanding are able to make connections and use the mathematics in a variety of situations; yet may still struggle expanding the understanding to non-routine situations. Students who are secure may still make mistakes at times; yet these students demonstrate that they have mathematical understanding with limited if any misconceptions. Students not secure in the understanding by the end of that Unit/Topic might benefit from small group intensification on these ideas. Teachers may choose to use an A/D/E (Assessment, Differentiation or Extension) day to provide additional instructional opportunity; yet should be cautious to not spend too long exploring these ideas to ensure students have ample opportunity for instruction to ALL of the Nevada Academic Content Standards (NVACS) for mathematics.


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## 3rd Grade Mathematics Curriculum Considerations SBAC preparedness throughout the year

This document highlights concepts and ideas for supporting and reinforcing student understanding throughout the entire school year. Waiting until these concepts are introduced, developed or secured in our instructional resource materials may not provide enough instructional opportunities for all students.

## Time

## Standard(s):

- 3.MD.A. 1 Tell and write time to the nearest minute and measure time intervals in minutes. Solve word problems involving addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram.

Consideration: Students have fewer opportunities to tell time using analog clocks outside of school. While students begin working with analog \& digital clocks in $1^{\text {st }}$ grade; in third grade telling time to the minute and working with elapsed time are not explored until Topic 14. Students would benefit from ongoing and purposeful experiences with using time throughout the school year.

## Prior Learning:

2.MD.C. 7 Tell and write time from analogue and digital clocks to the nearest five minutes, using a.m. and p.m.

First grade Number Corner has a full month on developing understanding of a.m. and p.m. The $2^{\text {nd }}$ grade instructional materials provide 3 lessons in which students tell time to the nearest five minutes on analogue and digital clocks, develop understanding of a.m. and p.m. times and use the language quarter past, half past and quarter to, to describe time.

## Suggestions for supporting/reinforcing understanding:

Throughout the year, ask students to tell time to the nearest 5-minutes and slowly begin working on telling time to the nearest minute. Bring attention to a.m. and p.m. activities in the real-world including the school day. Provide opportunities for students to describe time using the terms quarter past, half past and quarter to for relevant situations within the school day. Once students demonstrate readiness and are able to tell time to the minute, consider asking them to determine small intervals of elapsed time. For example, if the time is $11: 45$ and they go to lunch at 12, ask them what time it is and how many minutes until lunch. After students have officially had the learning opportunities provided in Topic 14, continue these opportunities to meet grade level expectations.

## Money

## Standard(s):

- 3.NBT.A. 3 Multiply one-digit whole numbers by multiples of 10 in the range 10-90 (e.g., $9 \times 80,5 \times 60$ ) using strategies based on place value and properties of operations.
- 3.OA.D. 8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.

Consideration: Children have fewer opportunities to reinforce money concepts in the real-world as Debit/credit, electronic payment and/or barter methods are commonly used in today's society. Some students may not have had enough learning opportunities to demonstrate understanding of these standards due to insecure understanding of money (value of, combinations of, contexts involving money).

## Prior Learning:

2.MD.C. 8 Solve word problems involving dollar bills, quarters, dimes, nickels, and pennies, using $\$$ and $\mathbb{C}$ symbols appropriately.

## Suggestions for supporting/reinforcing understanding:

Whenever possible connect concepts of place value (e.g. 60c has 6 tens so I could use 6 dimes), play with different coin and bill combinations to make a total amount, use money context to solve two-step problems, and connect multiplication equations that have a factor of 5 or 10 to nickels and dimes.

## Geometry

## Standard(s):

- 3.G.A. 1 Reason with shapes and their attributes. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

Consideration: Demonstrating understanding of this standard requires use of precise academic vocabulary in order to classify shapes using their attributes. A task such as classifying a square can help to illustrate why vocabulary is such an important component of geometry. Students need to recognize that a square can be classified as several different shapes. As an example, a square is also a parallelogram because it meets the requirements that the shape must:

- be a polygon (and the all the attributes for a polygon)
- have four sides (be a quadrilateral)
- have 2 pairs of parallel sides
- opposite sides are the same length
- opposite angles are the same size.

Then, in addition, students must recognize there are additional attributes required to make the shape a square. Despite working on geometric concepts and terminology, if the rigor has not been established in prior grade levels, this may become overwhelming and present a significant language load.

Prior Learning: 2.G.A. 1 Reason with shapes and their attributes.
Recognize and draw shapes having specified attributes, such as a given number of angles or a given number of equal faces. Identify triangles, quadrilaterals, pentagons, hexagons, and cubes.

## Suggestions for supporting/reinforcing understanding:

Consider implementing something like a Geometry Corner (Vertex) in your classroom or as an occasional routine where students could solve Geometry Riddles on geoboards, sort, or explore examples and non-example activities using the terms:

| polygon | parallelogram | right angle(s) | angle(s) closed |
| :--- | :--- | :--- | :--- |
| sides | vertices | pentagon | hexagon |
| quadrilateral | triangle | rectangle | square |
| rhombus | trapezoid |  |  |

## Critical Mathematical Models

Van de Walle, Karp, Lovin, and Bay-Williams (2014) state the following in regards to the relevance of mathematical models, Models or representations, whether they are conventional or not, give learners something they can use to explore, reason, and communicate as they engage in problem-based tasks... Because different representations can illuminate different aspects of a mathematical idea, multiple representations should be explored and encouraged. The more ways students are given to think about and test an emerging idea, the better they will correctly form and integrate it into a rich web of concepts and thereby develop a relational understanding (p. 23).

Identifying critical mathematical models may appear contradictory to the above statement. The suggestion is not that other models presented in the instructional materials be disregarded, but rather that the following models be used consistently and connected to the other models as appropriate. With the exception of Fraction Strips, these models have the ability to represent several mathematical concepts across multiple domains.

Number Lines: Number lines are a useful model because they can be used to model all four operations and fractions. However, they can be problematic for younger students as there is a shift from counting collections to counting continuous unit lengths. In third grade it is imperative that students be familiar with using the number line to represent addition, subtraction, multiplication, division and fractions as future grade level work will build on this model. Fourth graders locate decimals on number lines and use them for measurements. Fifth graders will use perpendicular number lines on coordinate grids. (Van de Wall, et.al. 2014)



394 is closer to 390 than 400 , so 394 rounds to 390 .



Area Model: The area model is a useful tool for representing strategies for multiplication and division. As well as, developing understanding of equal partitions for fractions and meaning of unit fractions.



Bar Diagrams: Bar diagrams are extremely helpful in representing the operations and different problem types. Instructional suggestions as well as examples and explanations of bar diagrams for the different problem types and operations can be found on TE p. F31-F35.

Fraction Strips: The use of physical models in fraction tasks are critical for developing understanding of fractions as numbers. Fraction strips provide a physical model of a whole, equal parts, iterations of the unit fraction, identifying equivalent fractions and comparing fractional quantities. Fraction strips also support the eventual use of the number line.


## - Grade 3 Topic 1: Understand Multiplication and Division of Whole Numbers

Big Conceptual Idea: K-5 Operations and Algebraic Thinking (pp. 22-28)
Prior to instruction, view the Topic 1 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 1A-1F), the Topic Planner (pp.1l-1K), all 7 lessons, and the Topic Assessments (pp. 55-56A).

| Mathematical | Topic Essential Question: |
| :--- | :--- |
| Background: | What are the different meanings of multiplication and division? |
| Read Topic 1-2 | Reference Answering the Topic Essential Question (TE, pp. 53-54) for key elements |
| Cluster Overview/Math | Ba answers to the Essential Question. <br> Backround (TE, pp. |
| 1A-1F) |  |

The lesson map for this topic is as follows:

| $1-1$ | $1-2$ | $1-3$ | $1-4$ | $1-5$ | $1-6$ | $1-7$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

4 A/D/E days used strategically throughout the topic

| Topic 1 <br> Muftiplication <br> ond Division of <br> Whole Numbers <br> Number of <br> lessons: 7 <br> A/D/E: $\mathbf{4}$ days <br> NVACS Focus: <br> OA.A |
| :---: |
| Total Days: ~11 |
| 3rd Grade Curriculum |
| Pacing Framework: |
| Balanced Calendar |

## Instructional note:

This topic focuses on beginning to build the meaning of multiplication and division to meet the Nevada Academic Content Standards (NVACS) 3.OA.A cluster, "Represent and solve problems involving multiplication and division" (2010). This topic focuses on exploring multiplication as meaning equal groups and connects this understanding to $2^{\text {nd }}$ grade when children "Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and 5 columns; write an equation to express the total as a sum of equal addends" (NVACS, 2.OA.C.2, 2010).

Throughout this topic, children model various multiplication situations using tools including arrays and number lines. Additionally, students use strategies such as skip counting to explore the concept of equal groups and connect repeated addition to multiplication. Students are introduced to the Commutative Property of Multiplication which states that the order factors are multiplied in does not change the product. Students need to understand that multiplication equations model situations. For example, 4 teams of 6 players ( 4 $x 6$ ) is different from 6 teams of 4 players ( $6 \times 4$ ). Explore the equal groups within the array for each model of $(4 \times 6)$ and $(6 \times 4)$.

Conceptually, the focus is understanding multiplication as equal groups and relating this to division. In $2^{\text {nd }}$ grade, students understand that they are able to add and subtract groups with varying group size (e.g. $36-14$ or $45+76$ ), now this knowledge is pushed to realizing that in multiplication the group size must be equal ( $2+2+2+2$ is 4 groups of 2 , or $4 \times 2$ ). Emphasize and help students connect "equal group size", "equal addends" and "equal subtrahends" throughout the topic.

Students develop understanding of division as a way of separating one group of objects into equal groups. Division has two (2) different types of problems. Partitive division, also known as dealing or fair sharing, is when the number of groups is known but the size of each group is unknown. Measurement division, also known as chunking, is when the number in each group is known but the number of groups is unknown. Measurement division allows students to employ repeated subtraction. The two (2) types can only be determined when working with division in context or word problems and will be explored further in Topic 5.

This understanding of "equal groups" begins to develop the foundations for fluency and will build over the next few topics to support 3.OA.C.7, "Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g. knowing that $8 \times 5=40$, one knows $40 / 5=8$ ) or properties of operations. By the end of Grade 3 , know from memory all products of two one-digit numbers" (2010). It is important to note that this expectation may not be secure until "the end of Grade 3." Additionally, Van de Walle, Karp, Lovin, and Bay-Williams (2014) state that, "...students' progress through stages that will eventually result in 'just knowing'" (p. 128). Those stages are:

## - Phase 1: Constructing Meaning and Counting Strategies

- Phase 2: Reasoning Strategies
- Phase 3: Working toward quick recall

Detailed information about the three phases of development towards fact fluency can be found in the article Basic Math Facts: A Sequence of Learning. This topic focuses on phase 1: Constructing Meaning and Counting Strategies for multiplication and division. In this topic students develop understanding of multiplication as a way of joining equal groups by using repeated addition with arrays and skip counting with the open number line and arrays.

Tools are referenced several times in this topic in the Look Back!. Consider discussing these questions whole group to help establish a culture for learning mathematics with manipulatives seen as tools for working with, understanding and representing mathematics.

## Focus Math Practice 5: Use appropriate tools strategically

Focus on opportunities for students to develop Mathematical Practice 5 behaviors, as this is the focus of the Math Practices and Problem Solving lesson, 1-7. Reference the Teacher's Edition (TE, pp. F25-F25A) and the NVACS (2010, p. 6).

## Assessment Considerations:

On Topic Assessment item 6, students' arrays need to actually match the context described in the problem. For example, students must have 2 rows with 4 items in each row as their array to receive credit ( $2 \times 4$ ). Encourage students to continue to use tools while completing the assessment.

Both the Topic Assessment and the Topic Performance Assessment will provide opportunities to work at various DOK levels. Choose the assessment(s) that will provide the most information about student understanding. For Topic 1, consider scaffolding this resource by allowing students to work in groups throughout the topic and building in opportunities for discussion, peer feedback, and revision.

Finally, please note that lessons 1-1 and 1-2 indicate that these are possible 2-day lessons. Additional A/D/E days were built into the 2019/2020 WCSD 3 Grade Pacing Framework to allow time to establish class routines and expectations for:

- Accessing and returning manipulatives
- Classroom discussion norms
- Mathematical Mindset
- Integrating ideas from the Math Practices and Problem Solving Handbook (TE p. F19-F35)

|  | Essential Academic Vocabulary <br> Use these words consistently during instruction. |
| :--- | :--- |
| New Academic Vocabulary: <br> (First time explicity taught) | Review Academic Vocabulary: <br> (Vocabulary explicityly taught in prior grades or topics) |
| multiplication | equal groups |
| factors | number line |
| product | array |
| equation | row |
| unknown | column |
| Commutative (order) Property |  |
| of multiplication |  |
| division |  |

Additional terminology that students may need support with: repeated addition and repeated subtraction

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding question: "Are students using multiple strategies to multiply and divide whole numbers?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $1-3$ | Solve \& Share <br> (student work samples) | Focus CTC around big idea: <br> $\bullet \quad$ students can draw arrays to show joining groups. <br> students can use multiple tools, models or strategies (skip counting, <br> repeated addition, arrays). <br> students understand multiplication means equal groups. |
| $1-5$ | Quick Check (digital platform) | Focus CTC around data analysis and collection of student workspace <br> (scratch paper). <br> students understand that multiple objects can be shared by separating <br> into equal groups. <br> Printable version available under "Teacher Resources". |


| Learning Cycle Assessments (summative) | Topic Assessments SE pp. 53-56 | Use Scoring Guide TE pp. 53-56A |
| :---: | :---: | :---: |

Standards listed in bold indicate a focus of the lesson.



| Lesson 1-4: The Commutative Property |  |  |
| :---: | :---: | :---: |
| 3.OA.B. 5 <br> 3.OA.A. 3 <br> MP. 3 <br> MP. 7 | Access Prior Learning: <br> In Grade 2, students were secure in their understanding of the commutative (order) property of addition. This property states that order of addend does not change the sum. In lesson 1-3, Grade 3, students learned that arrays can represent multiplication and that the order of the factors gives the number of rows and the number in each row. <br> Beginning of the Big Idea: In this lesson students work with their secure understanding of the Commutative (order) Property of Addition to beginning to build the understanding of the Commutative (order) Property of Multiplication. The property states that we can multiply the factors in any order and the product stays the same. | Instructional note: <br> Throughout this lesson bring attention to how switching factors creates a different multiplication situation. The Commutative Property gives us a strategy for finding products. Therefore, if $2 \times 7$ is an easier fact to recall, I can use $2 \times 7$ to get the product for $7 \times 2$. You may consider having students return to modeling the differences in the expressions while still seeing that the product remains the same. <br> Solve \& Share: <br> To continue to support students' development of behaviors in selecting appropriate tools (MP.5), consider waiting to distribute the 25 counters until after posing the question, "What tools or strategies can you use to solve this problem?" (TE, p. 25). <br> Look Back: <br> In the event that a conjecture supporting the Commutative (order) Property is not developed during sharing of student solution methods and reasoning from the Solve \& Share, consider discussing the Look Back! and relating it back to models for the Solve \& Share. <br> Visual Learning: <br> Consider pausing the Visual Learning Animation before it shows the repeated addition in the array if students are still struggling with connecting repeated addition to a multiplication equation. <br> After discussing, "Did the order of the factors change?" consider posing the question, "Do we have the same multiplication situation for both arrays?" See the above instructional note for ways to expand this discussion. <br> Independent Practice/Math Practices and Problem Solving: <br> To formatively assess if students are able to distinguish a multiplicative situation from an additive situation consider posing item 13 , without students having access to the student edition since it leads students to knowing it is an additive situation. <br> Assess and Differentiate/Intervention Activity: <br> If time permits, you may consider replacing the On and Advanced Activity Center with either the games Toss and Talk (TE, p. 11A), Teamwork (TE, p. 23A) or the Fluency Practice Activity (TE, p. 49). <br> Child-watch to identify students who need additional support and pull them in a small group to complete the Intervention Activity (TE, p.29A). |
| Lesson 1-5: Division as Sharing |  |  |
| 3.OA.A. 2 <br> 3.OA.A. 3 <br> MP. 1 <br> MP. 3 <br> MP. 4 <br> MP. 5 <br> MP. 6 | Access Prior Learning: In Grade 2, students explored the idea of fair shares in geometry by dividing a shape into equal parts. Throughout this topic, students have been working to understand multiplication as the joining of equal groups. <br> Beginning of the Big Idea: <br> This lesson begins to build the understanding that multiple objects can be shared by separating into equal groups and is one way to think of division. | Instructional note: <br> This lesson works with partitive division (fair sharing or dealing) scenarios (known groups, unknown number in each group). <br> Solve \& Share: <br> To continue to support students' development of behaviors in selecting appropriate tools (MP.5), consider waiting to distribute the 20 counters until after posing the question, "How can we represent this problem?" (TE, p. 31). <br> Encourage students to model with a tool or a pictorial representation. Discuss where the mathematics is represented in their model (e.g. Where are the apples? Where are how many each person gets?). <br> Visual Learning: <br> Connecting student solution methods to the bar diagram and how their models are shown, can help students better understand the bar diagram as a model for division. <br> Convince Me: <br> Consider discussing the Convince Me! question to initiate a discussion about remainders. While third grade students do not work with remainders, it is important for them to know that we can still divide when the divisor doesn't exactly go into the dividend (leftovers). <br> Independent Practice/Math Practices and Problem Solving: <br> Consider discussing item 11 as it demonstrates the relationship between the size of the divisor (e.g., $15 \div 3=5,3$ is the divisor) and the quotient (e.g. $15 \div 3=5,5$ is the quotient). <br> Consider discussing item 12 to provide students with the opportunity to reason with a problem that does not provide enough information to solve. <br> -continues on next page- |


|  |  | Assess and Differentiate/Intervention Activity: <br> If time permits, teach students how to play "Toss and Talk" (TE, p. 35A). All students should have the opportunity to play this game it provides engaging and meaningful practice of a key concept. <br> Child-watch to identify students who need additional support with these ideas and pull them into a small group to do the Intervention Activity (TE, p.35A). <br> *CTC: Quick Check (digital platform) |
| :---: | :---: | :---: |
| Lesson 1-6: Division as Repeated Subtraction |  |  |
| 3.OA.A. 2 <br> 3.OA.A. 3 <br> MP. 2 <br> MP. 4 <br> MP. 5 <br> MP. 8 | Access Prior Learning: <br> In lesson 1-1, Grade 3, students saw that repeated addition is a way to think of multiplication and a way to join equal groups. In lesson 1-5, Grade 3, students learned to think of division as sharing. <br> Developing the Big Idea: <br> In this lesson, students work with their developing understanding that division involves separating one group of objects into equal groups. <br> Students also beginning to build understanding that one way to think about division is as repeated subtraction of the divisor from the dividend. Additionally, this lesson develops the understanding that we have 2 different types of division situations (fair sharing and chunking). | Instructional note: <br> Using repeated subtraction to divide can support students in recognizing the inverse relationship that exists between multiplication and division. Having students work with repeated subtraction as a way of thinking about division also emphasizes the connections between repeated addition as multiplication and repeated subtraction as division. In this lesson, students are working with measurement division (chunking) scenarios, which allows repeated subtraction to be used as a strategy. <br> Solve \& Share: <br> To continue supporting students' in selecting appropriate tools (MP.5), consider waiting to distribute the 12 counters until after posing the question, "What tools can you use to solve this problem?" (TE, p. 37). <br> For students that incorrectly use $12-2=10$ to solve this problem, consider asking them to model the problem with counters instead. Can they explain how many friends will get tacos using the counters? Can they connect the concrete modelling to repeated subtraction? <br> During the whole class discussion of student solution methods and reasoning, consider posing the question, "We used repeated addition to help us find the solution to a multiplication equation, how could we use repeated subtraction to find the solution to this division situation?" and "where are our equal groups in repeated subtraction?" "How many groups do we have? <br> Visual Learning: <br> The Visual Learning Animation uses the bar diagram to model the division situation presented in this problem. This lesson is focusing entirely on measurement (chunking) division. In this type of division, we know the number of objects in the equal groups and need to find the total number of equal groups. Consider discussing the differences in the bar diagrams to develop the understanding that we have 2 different types of division situations (fair sharing and chunking). <br> Convince Me: <br> Consider assigning the Convince Me! and discussing to help students understand the role of the dividend, divisor, and quotient. <br> Assess and Differentiate/Intervention Activity: <br> If time permits, you may consider replacing the On and Advanced Activity Center with the game Toss and Talk (TE, p. 35A) or the Fluency Practice Activity (TE, p. 49). <br> Child-watch to identify students who need additional support and pull them into a small group to complete the Intervention Activity (TE, p. 41A). |
| Lesson 1-7: Math Practices and Problem Solving- Use Appropriate Tools |  |  |
| 3.OA.A. 3 <br> 3.OA.A. 1 <br> 3.OA.A. 2 <br> MP. 5 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 7 | Access Prior Learning: <br> Previous lessons in this topic have developed students' understanding of multiplication and division situations, and how to use appropriate tools strategically as they have modeled with counters. <br> Securing the Big Idea: <br> This lesson secures the idea that we can use appropriate tools strategically to model multiplication and division situations. | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 5. Refer to the Math Practices and Problem Solving Handbook (TE, pp. F25-F25A, F29) for suggestions on how to develop, connect and assess this Math Practice. Also, reference the handbook in the Student Edition (SE, p. F25). <br> Solve \& Share: <br> Consider reintroducing MP. 5 Thinking Habits (SE, p. F25) before introducing the Solve \& Share. Use the time when students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP. 5 that are listed in the Math Practices and Problem Solving Handbook (p. F25A). After discussing student solution methods and reasoning, ask students to self-score for the behaviors associated with this math practice. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the On and Advanced Activity Center with the game Toss and Talk (TE, p. 35A) or the Fluency Practice Activity (TE, p. 49). <br> Child-watch to identify students who need additional support and pull them into a small group to complete the Intervention Activity (TE, p.47A). |

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## - Grade 3 Topic 2: Multiplication Facts: Use Patterns

Big Conceptual Idea: Operations and Algebraic Thinking (pp. 22-28)
Prior to instruction, view the Topic 2 Professional Development Video located in Pearson Realize online. Read the Teacher's
Edition (TE): Cluster Overview/Math Background (pp. 1A-1F), the Topic Planner (pp.57A-57B), all 6 lessons, and the Topic
Performance Assessment (pp. 103-104A).

## Mathematical <br> Background:

Read Topic 1-2 Cluster
Overview/Math Background
(TE, pp. 1A-1F)

## Topic Essential Question:

How can unknown multiplication facts be found using patterns and properties?

Reference Answering the Topic Essential Question (TE, pp. 101-102) for key elements of answers to the Essential Question.

## The lesson map for this topic is as follows:

| $2-1$ | $2-3$ | $2-4$ | $2-2$ | $2-5$ | $2-6$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 4 Assessment | Assays used strategically throughout the topic | Pracing Framework: |  |  |  |
| Palanced Calendar |  |  |  |  |  |

## Instructional note:

This topic focuses on continuing to build the meaning of multiplication to meet the 2010 Nevada Academic Content Standards (NVACS) primarily focusing on 3.OA.A cluster heading, "Represent and solve problems involving multiplication and division" and 3.OA.D cluster heading "Solve problems involving the four operations, and identify and explain patterns in arithmetic." This topic also introduces the Zero and Identity properties in lesson 2-3 (3.OA.B.5).

Topic 2 focuses on understanding multiplication through an exploration of patterns. Patterns play an important part of mathematical development and support algebraic reasoning, relationships and lead to mathematical generalizations. Throughout Topic 2, encourage students to reason mathematically, draw conclusions, justify and generalize solutions. For example, in lesson 2-1 the Solve \& Share provides an opportunity to explore patterns that occur when there are equal groups of 2 (there are 2 legs on $x$ amount of chickens). What do students notice about the patterns? Given the conditions of the problem, can there ever be an odd number? Why or why not?

Encourage student reasoning using tools or models that demonstrate the understanding of multiplication as equal groups. Spend time connecting student models to the patterns generated and connect both of these to understanding the meaning of multiplication. Building from Topic 1, ensure that the students' models use represent the given equation. For example, if students build an array to demonstrate $9 \times 4$, the array must be represented as 9 rows of 4 stated " 9 groups of 4". Or if they use a number line there should be 9 "jumps" or "hops" that are in equal increments of 4 . Some students may naturally start using the Commutative Property to build more efficient models or to assist their reasoning. For example, given the factors 9 and 2 students may reason about 9 groups of 2 or find it more efficient to think about 2 groups of 9 . Highlight and discuss how Properties help us reason more efficiently.

Teachers should use their professional discretion to decide on the placement of Lesson 2-2. The lesson may be kept in the same order as shown in the instructional materials, or moved after lesson 2-4 as shown in this guide. See the lesson note for more information to help with this decision. Regardless of the order taught, ensure that students make the connection of using known facts (factors with 10) to derive unknown facts (factors with 9). See the instructional note in lesson 2-2 for examples.

Looking ahead to the assessment, Part A, item 2 of the Topic Assessment asks students to, "Identify any hidden question" (TE, pp. 101-102). Students in $2^{\text {nd }}$ grade worked with the idea of a "hidden question" in 2-step word problems in Topics 8,13 \& 14 . They will revisit this idea in Lesson 2-6. Both the Topic Assessment and the Topic Performance Assessment will provide opportunities to work at various DOK levels. Choose the assessment(s) that will provide the most information about student understanding. Consider scaffolding this resource by allowing students to work in groups throughout the topic and by ensuring opportunities for discussion, peer feedback, and revision.

## Focus Math Practice 4: Model with mathematics

Focus on opportunities for students to develop Mathematical Practice 4 behaviors, as this is the focus of the Math Practices and Problem Solving lesson 2-6. Reference the Teacher's Edition (TE, pp. F24-F24A) and the Nevada Academic Content Standards for Mathematical Practice (NVACS, 2010, p.7).

|  | Essential Academic Vocabulary <br> Use these words consistently during instruction. |
| :--- | :--- |
| New Academic Vocabulary: <br> (First time explicitly taught) | Review Academic Vocabulary: <br> (Vocabulary explicity taught in prior grades or topics) |
| multiples | factor <br> Identity (One) Property of Multiplication <br> Zero Property of Multiplication |
|  | product <br> array |
|  | multiplication |

Additional terminology that students may need support with: patterns, relationship

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding questions: "Are students identifying patterns in multiplication? Are students using tools, strategies or models to multiply whole numbers?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $2-4$ | Math Practices and Problem Solving <br> (student work samples) <br> Item 20 | Focus CTC around the big idea: <br> $\bullet \quad$ students are identifying patterns in multiplication and explaining their thinking. <br> students are using various tools, strategies or models to multiply. |
| $2-5$ | Quick Check (digital platform) | Focus CTC around data analysis and collection of student workspace (scratch <br> paper). <br> $\bullet$ students understand that multiplication facts can be found by identifying <br> patterns. <br> students are using various tools, strategies or models to multiply <br> Printable version available under "Teacher Resources". |


| Learning Cycle | Topic Assessments |
| :---: | :--- | :--- |
| SE pp. 101-104 |  |$\quad$ Use Scoring Guide TE pp. 101-104A

Standards listed in bold indicate a focus of the lesson.


|  | product has a 5 in the ones place. When 5 is multiplied by an even number, it has a 0 in the ones place. | After student solution methods and reasoning have been shared, asking students questions such as, "What do all the products have in common?" (e.g. they're even) and "Why is that?" will help them to make generalizations and reach the understandings stated in Beginning of the Big Idea for when 2 is a factor. Have students confirm, clarify, or correct their ideas during the Visual Learning Animation. <br> Visual Learning: <br> The Visual Learning Animation for this topic is helpful for reinforcing understanding of meanings of multiplication. If students are still struggling to understand multiplication as the joining of equal groups, view and discuss the ideas modeled as a class. Building in additional pausing points during the Visual Learning Animation will allow students to practice the skip counts and represent them on an open number line. <br> Convince Me: <br> Consider having a whole class discussion around the Convince Me! so students can continue their discovery of patterns in products when 2 and/or 5 is a factor. <br> Assess and Differentiate/Intervention Activity: <br> If time permits, teach students how to play "Quick Questions" (TE, p. 65A). All students should have the opportunity to play games that provide opportunities for practicing strategies for facts with 2 and 5 as factors. Students may also continue to play any of the games from topic 1. |
| :---: | :---: | :---: |
| Lesson 2-3: Apply Properties: Multiply by 0 and 1 |  |  |
| 3.OA.A. 3 <br> 3.OA.A. 1 <br> 3.OA.D. 9 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 7 | Access Prior Learning: <br> In Topic 1, students developed an understanding of multiplication as joining equal groups to find the total number of objects in groups. In $2^{\text {nd }}$ grade, students were secure in their understanding of the Zero Property of Addition. <br> Developing the Big Idea: <br> Students develop the understanding of multiplication as joining equal groups of objects to begin to build an understanding of the Zero Property of Multiplication and Identity (One) Property of Multiplication. | Instructional note: <br> See the Instruction note at the top of this document for an explanation of moving lesson 2-2. <br> Solve \& Share: <br> For concrete learners or students grappling with the misconception that multiplication always makes numbers bigger, you may consider having paper plates or bags available so that students can model having 6 groups of 0 objects. To support students' development of MP. 4 Model with mathematics, you might consider asking students how they could model or show this problem before letting them work on the Solve \& Share. <br> Before moving onto the Visual Learning, ask students "If Carlos had 6 bags with 1 apple in each bag, how many apples would he have?" Continue to question students to develop a class conjecture about multiplying by 1 . Confirm, clarify, and correct this conjecture during the Visual Learning Animation. <br> Visual Learning: <br> Consider pausing the Visual Learning Animation after they introduce each property to have students test the property using counters and groups of other factors to confirm the stated property. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 26 as this problem allows for multiple entry points and answers. When a student solves the problem, you can extend thinking by asking if that is the only answer. Students may give a generalized rule for the answer (any number greater than 4 , as 4 is the minimum number needed to have a greater number of bikes than Barb's class). <br> Assess and Differentiate/Intervention Activity: <br> If time permits, you may consider replacing Problem Solving Reading Mat with either the games from previous topics, the game Quick Questions (TE, p. 65A), or the Fluency Practice Activity (TE, p. 97). <br> Child-watch to identify students who need additional support and pull them into a small group to complete the Intervention Activity (TE, p.77A). |
| Lesson 2-4: Multiply by 10 |  |  |
| $\begin{gathered} \text { 3.OA.A. } 3 \\ \text { 3.OA.A. } 1 \\ \text { 3.OA.D. } 9 \\ \text { MP. } 2 \\ \text { MP. } 3 \\ \text { MP. } 4 \\ \text { MP. } 7 \\ \text { MP. } 8 \end{gathered}$ | Access Prior Learning: <br> Students have been skip counting by 10 since Kindergarten. In Topic 1 students used skip counting on the open number line to represent multiplication. <br> Developing the Big Idea: <br> Students are developing their understanding of patterns in multiplication by identifying a pattern when multiplying by 10. | Solve \& Share: <br> Consider providing students with tools, such as two-colored counters or place-value blocks to solve the problem. Students may only write the products for each week which can make identifying a pattern for multiplying by 10 difficult to see. In this event, consider asking students to write out the equations they used to solve each week and to looks for patterns in the factors and products. <br> During the class discussion of students' solution methods and reasoning, push to get students to use place value reasoning to support their explanations of the justification offered in the Transition to the Visual Learning Bridge (TE, p. 79). For example, students may explain, "Since $6 \times 10$ means we have 6 groups of 10 miles we do not have any ones because 6 tens is 60 resulting in a 0 in the ones place for all products when 10 is a factor." <br> -continues on next page- |


|  |  | Referring to 60, 70, and 80 as multiples of 10 will support students' understanding of the term multiples. <br> Visual Learning: <br> Consider pausing the video after it asks, "How many miles will Greg run to train for the race?" Discuss as a class what operation is needed to solve this question. The video will ask students this question as it's showing the 10's times tables; however, at this point connect student responses to the 10 s fact table. This will support student understanding of multiplication being 'groups of'. Avoid teaching students the "zero trick" of just adding a zero to the right and instead maintain the focus on patterns that appear when multiplying by 10. <br> Consider continuing to support students' understanding of the term "multiple(s)" by asking them to identify the multiples of 10 in the 10 's times table. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider including item 15 so that students have the opportunity to revisit reasoning with repeated subtraction situations. <br> Assess and Differentiate: <br> The On-Level and Advanced Activity Centers for this lesson includes 9 as a factor. Consider allowing students to play the game, but first challenge them to use what they know about multiplication with factors of 10 to develop a strategy for solving problems with 9 as a factor. Alternatively, you may wish to have students play a game from previous topics or lessons. <br> Child-watch to identify students who need additional support and pull them into a small group to complete the Intervention Activity (TE, p.83A). <br> *CTC: Math Practices and Problem Solving (student work samples) |
| :---: | :---: | :---: |
| Lesson 2-2: 9 as a Factor |  |  |
| 3.OA.A. 3 <br> 3.OA.A. 1 <br> 3.OA.D. 9 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 7 | Access Prior Learning: <br> In Topic 1 students came to understand multiplication as the joining together of equal groups. In Lesson 2-4, Multiples of 10, students identified a pattern for solving for multiplication problems with 10 as a factor. <br> Developing the Big Idea: <br> In this lesson, students are developing their understanding of multiplication as joining equal groups and of multiples of 10 to generate a derived fact strategy for multiplication problems with 9 as a factor. | The purpose of this lesson is to explore the patterns that occur in multiplication and build mathematics curiosity and wonder at why these patterns occur. 9 as a factor reveals fascinating and unique opportunities to recognize and explore patterns beyond those that are found when looking at other factors, which may just reveal multiples or simple and easily recognizable patterns. Exploring 9 as a factor can push toward arithmetic patterns beyond those explored in earlier grades. <br> The pattern explorations should not be seen as tricks to help students memorize the 9's facts. <br> If using 2-2 after 2-4 then build opportunities for students to use known facts such as $10 \times 4$ <br> (40) to derive a 9 fact such as $9 \times 4$ (I know that 10 groups of 4 is 40 so one less group of 4 will be 36). Moving from known to derived facts will be explored further in topic 3 . <br> Solve \& Share: <br> Prior to the Solve \& Share assess student readiness by asking students to state the meaning of the equation $6 \times 10$ from yesterday's Solve \& Share (e.g. $6 \times 10$ means we have 6 groups of 10 for a total of 60 ) and asking what if Duke ran 9 miles. How many will he run in 6 weeks? <br> Consider asking a student that has direct-modeled the Solve \& Share either with counters or pictorial representations and a student that used a 10 as a factor and completed a derived fact strategy to share. <br> Orchestrate a class discussion around these two solution methods and the reasoning used. As a class, consider how to model the math (MP.4) when using 10 as a factor. Connect the reasoning between the student's model who use a derived fact to model and that of the student that chose to direct model the $4 \times 9=36$. <br> Look Back: <br> Consider discussing the Look Back! problem revisit ideas about the Commutative (Order) Property of Multiplication. |


|  |  | Visual Learning: <br> Since the Visual Learning Animation is more procedural than conceptual, consider replacing the animation by writing the 10 's and 9's times tables next to each other. Facilitate a discussion to help students identify a pattern for using multiples of 10 to solve problems with 9 as a factor. Students can generalize to discover a derived fact strategy for multiplication problems with 9 as a factor. For example: <br> See the Instructional Note at the beginning of this topic for an explanation of student reasoning of this strategy. <br> Consider modeling the multiple by 10 , and subtract the extra group using Base-10 blocks or counters and connect to the array model to support student understanding. <br> If the Visual Learning Animation is replaced with the above activity, item 2 in the Guided Practice will need to be skipped or reworded to have students describe using a multiple of 10 to solve a 9s fact. <br> Independent Practice/Math Practices and Problem Solving: <br> Notice that item 15 is the same equation students used in today's Solve \& Share. This is an opportunity to see if students will recognize that they have worked with this problem already and it will therefore have the same product. <br> Assess and Differentiate/Intervention Activity: <br> If time permits, teach students how to play Toss and Talk (TE, p. 83A). All students should have the opportunity to play this game. <br> Child-watch to identify students who need additional support and pull them into a small group to complete the Intervention Activity (TE, p.71A). For this activity, you can still do the Intervention Activity Modeling 9s Facts; however, consider replacing the worksheet with relating the models made to the finger strategy for finding multiples of 9 . |
| :---: | :---: | :---: |
| Lesson 2-5: Multiplication Facts: 0, 1, 2, 5, 9, and 10 |  |  |
| 3.OA.A. 3 <br> 3.OA.A. 1 <br> 3.OA.D. 9 <br> MP. 3 <br> MP. 4 <br> MP. 5 <br> MP. 6 <br> MP. 7 | Access Prior Learning: <br> In previous lessons in Topic 2 students have identified patterns that can be used as strategies for solving for facts with $0,1,2$, 5,9 , and 10. <br> Developing the Big Idea: <br> This lesson further develops the understandings students began to understand in the previous lessons to apply the strategies for solving for facts with 0,1 , $2,5,9$, and 10 as a factor. | Solve \& Share: <br> For the whole class discussion consider sequencing solution strategies so that the first student to share has a solution method that is similar to Stephanie's work (TE, p. 85). Consider having the second student to share be one that used solutions from having solved for the previous numbers of boxes to determine the products for the other boxes. <br> Visual Learning: <br> As students likely did not use a bar diagram to find the solution to the Solve \& Share, the Try It! provides the opportunity to work with modeling the math (MP.4) using a bar diagram. It may be helpful to discuss how the bar diagram is able to represent the joining of the equal groups. <br> Assess and Differentiate: <br> If time permits, consider replacing Problem Solving Reading Mat with either the games from previous topics, the game Quick Questions, Toss and Talk, or the Fluency Practice Activity (TE, p. 97). <br> Child-watch to identify students who need additional support and pull them into a small group to complete the Intervention Activity (TE, p.23A). <br> *CTC: Quick Check (digital platform) |
| Lesson 2-6: Math Practices and Problem Solving- Model with Math |  |  |
| 3.OA.A. 3 MP. 4 MP. 1 MP. 2 | Access Prior Learning: <br> In this topic students have identified patterns that can be used as strategies for solving for facts with $0,1,2,5,9$, and 10. Lesson 1-7 involved students solving for a 2-step word problem. Students also worked with 2-step word problems involving addition and subtraction and the idea of a | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 4. Refer to the Math Practices and Problem Solving Handbook (TE p. F24-F24A, F29) for suggestions on how to develop, connect and assess this Math Practice. Also, reference the handbook in the student edition (SE, p. F24). <br> -continues on next page- |


| MP. 3 | "hidden problem" in 2nd grade Topics 8, 13 |  |
| :--- | :--- | :--- |
| \& 14. |  |  |
|  | Developing the Big Idea: <br> In this lesson, students are developing their <br> understanding of multiplication as joining <br> equal groups and the use of patterns for <br> multiplying with 0, 1, 2, 5, 9, and 10. | Solve \& Share: <br>  <br> Share. Restating that an equation is an example of MP.4 Modeling the Math can be a good <br> reminder. Many students are under the misconception that MP. 4 means they must show a <br> drawing or concrete representation of the math. While having a drawn or concrete <br> representation of the math can make for a stronger argument (MP.3), it is not necessary for <br> modeling mathematical situations. <br> Consider using the time when students are working on the Solve \& Share as an opportunity to <br> child-watch for behaviors associated with MP.4 that are listed in the Math Practices and <br> Problem Solving Handbook (p. F24A). After discussing student solution methods and <br> reasoning, have students self-score for the behaviors associated with this math practice. <br> Convince Me: <br> Consider assigning the Convince Me! as it offers another opportunity to work with MP. 4 and <br> assess for behaviors attributed to this math practice. |
| Assess and Differentiate: <br> If time permits, consider assigning the Math and Science Activity (TE, p. 95A) as this relates the <br> mathematics in this topic to a real world context. <br> Child-watch to identify students who need additional support and pull them into a small group to <br> complete the Intervention Activity (TE, p.95A). |  |  |

## References

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Big Conceptual Idea: Operations and Algebraic Thinking, K-5 (pp. 22-28)
Prior to instruction, view the Topic 3 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 105A-105F), the Topic Planner (pp.105l-105K), all 8 lessons, and the Topic Performance Assessment (pp. 163-164A).

Mathematical
Read Topic 3-4 Cluster Overview/Math Background (pp. 105A-105F)

Topic Essential Question:
How can unknown multiplication facts be found using known facts?

Reference Answering the Topic Essential Question (TE, pp. 161-162) for key elements of answers to the Essential Question.


The lesson map for this topic is as follows:

| $3-1$ | $3-2$ | $3-3$ | $3-4$ | $3-5$ | $3-6$ | $3-8$ | $3-7$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Instructional note:

The Nevada Academic Content Standard (NVACS) cluster 3.OA.B states, "Understand properties of multiplication and the relationship between multiplication and division". In Topic 3, students work with the Properties of Operations to build reasoning strategies using known facts explored in Topic 2. Students do this by multiplying with $3,4,6,7$, and 8 as factors. Students will continue to work with multiplication using contextual problems (3.OA.A.3) and explore patterns that occur with factors and products (3.OA.D.9). Building understanding of multiplication strategies, including using the Distributive and Associative Properties will lead to fluency later in grade 3 (See Topic 5).

The Topic 3 Professional Development Video states, "Using known facts along with the properties of multiplication is a strategy for learning the multiplication facts for $3,4,6,7$, and 8 " (Dr. Schielack, enVisionmath2.0, 2016). This topic introduces the Distributive and Associative Properties of Multiplication with a focus on the standard 3.OA.B.5, "Apply properties of operations as strategies to multiply and divide." (NVACS, p. 23). While grouping symbols are not explicitly stated in the standards until 5 th grade, the use of parentheses is an assumed part of the mathematics in the properties and should be used to communicate the grouping of the expressions and thus the order of the operations. For more information about the use of parentheses in 3 rd grade and the progression of Order of Operations please read page 27 of the K-5, Operations and Algebraic Thinking progression document. The footnote on this standard indicates that students do not need to use the formal terms for these properties; therefore, it is acceptable for students to refer to them as the turn-around, break-apart, and order properties of multiplication. However, you may want to consider restating their informal language with the formal terms to support precise mathematical vocabulary development.

Topic 3 uses the Distributive Property of Multiplication extensively to support student understanding by linking an array with the decomposition of a factor. Students model decomposing a factor into smaller factors to breaking apart larger arrays into smaller arrays. For example, given an array that models $7 \times 5$, students may choose to decompose or break the first factor ( 7 ) into a 5 and 2 as they know their 5 facts and their 2 facts. Thus, students are using the distributive property to solve unknown facts using known facts: $(5 \times 5)+(2 \times 5)$.

In lesson 3-7, the focus is on understanding the Associative Property, which allows factors to be grouped in different ways. When given three or more factors students are able to group the factors differently depending upon what is more efficient for the student. For example, given the factors $2 \times 5 \times 3$ (which can be modeled with two separate $5 \times 3$ arrays), students may group the factors as ( $2 \times 5$ ) $x 3$ or as $2 \times(5 \times 3)$. They should see the equivalence between these groupings and the new facts created by associating different factors together; in this case $10 \times 3$ or $2 \times 15$. Consider using one of the A/D/E days for this topic to spend more time exploring these ideas from the Associative Property of Multiplication.

When students demonstrate readiness, consider replacing the two-colored counters used in arrays with colored tiles to begin building area models. This will begin to lay the foundation for the connection between the array model and the area model explored in Topic 6. Note: If colored tiles are used, be sure that there are no gaps between tiles as you are now connecting to area concepts.

Looking ahead to the Topic Assessment, consider having tools available for students that may need them. Item 11 Part B requires students to generalize their understanding and apply it to a new situation. In the Topic Performance Assessment for item 2 Part B, accept multiple answers for where students draw the line; also accept responses where students have drawn multiple lines to use the Associative Property of Multiplication.

## Focus Math Practice 8: Look for and express regularity in repeated reasoning

Focus on opportunities for students to develop Mathematical Practice 8 behaviors, as this is the focus of the Math Practices and Problem Solving lesson 3-8. Reference the Teacher's Edition (TE, pp. F28-F28A) and the Nevada Academic Content Standards for Mathematical Practice (2010, p. 8).

| Essential Academic Vocabulary <br> Use these words consistently during instruction. |  |
| :--- | :--- |
| New Academic Vocabulary: <br> (First time explicity taught) | Review Academic Vocabulary: <br> (Vocabulary explicitly taught in prior grades or topics) |
| Distributive (break-apart) Property of | factor |
| Multiplication | product |
| Associative (Grouping) Property of | commutative property of <br> Multiplication |
|  | multiplication <br> doubles <br> halving |

Additional terminology that students may need support with: break-apart, addend, sum, compose, decompose, generalization

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding question: "Are students using the properties of multiplication and known facts to find products of unknown facts?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $3-1$ | Solve \& Share <br> (student work samples) | Focus CTC around the big idea: <br> $\bullet \quad$students understand that arrays can be broken apart (decomposed) into <br> smaller arrays based on the distributive property. <br> $3-3$Math Practices and Problem Solving <br> (student work samples) <br> Items 22 and 23 |
| Focus CTC around the big idea: <br> $\bullet \quad$ students apply the properties of multiplication with 4 as a factor. <br> $\bullet \quad$ students use known facts to find products of unknown facts. |  |  |


| Learning Cycle | Topic Assessments | Use Scoring Guide TE pp. 161-164A |
| :---: | :--- | :--- |
| SE pp. 161-164 |  |  |


| NVACS <br> (Content and Practices) | Mathematical Development of the Big Idea | Instructional Clarifications \& Considerations |
| :---: | :---: | :---: |
| Lesson 3-1: The Distributive Property |  |  |
| 3.OA.B. 5 <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 6 <br> MP. 7 | Access Prior Learning: Commutative Property of Multiplication, familiarity with facts that include $2,5,0,1,10$, and 9 as a factor. <br> Developing the Big Idea: Students are beginning to understand that the Distributive Property of Multiplication can be used to break a large array into a small array that represents known facts. | Topic Opener: <br> Introduce the Topic Essential Question, "How can unknown multiplication facts be found using known facts?" (TE, p. 105). Consider making this an anchor chart in your classroom where each day new ideas are added so that students can see the development and make connections throughout the topic. If building an anchor chart, this could be an appropriate time to quickly revisit the Commutative Property of Multiplication and add it to the chart. You may want to expand on this idea and include in the chart that since they already know $2 \times 7=14$ they also know that $7 \times 2=14$. <br> You might also consider having students complete the Review What You Know prior to beginning instruction on Topic 3 so that you can respond to student instructional needs using the Item Analysis for Diagnosis and Intervention (TE, p. 106-108). <br> Consider introducing vocabulary as they encounter them in the lessons rather than introducing all terms at the beginning of the lesson. |

$\left.\begin{array}{|l|l|l|l|}\hline & & \begin{array}{l}\text { Solve \& Share: } \\ \text { Consider waiting to distribute the } 25 \text { two-color counters until students suggest them in response } \\ \text { to the question, "What tool can you use to solve this problem?" (TE, p. 109). }\end{array} \\ \text { While students are working on the Solve \& Share consider asking them: } \\ \text { e "What equation does the original array represent?" (e.g. } 5 \times 4)\end{array}\right\}$


|  |  | Visual Learning: <br> The Visual Learning Animation makes one strategy explicit for solving for a 6 fact. This strategy will also work for 7 facts but the animation does not make this connection. Therefore, you may want to ask students how they could use this strategy to solve for 7's facts. <br> Alternatively, you may consider replacing the Visual Learning Animation with the Another Look! video as it makes the strategy explicit for both 6 \& 7's facts. If choosing to go this route, consider pausing after it displays the equations " $6 \times 4=$ ?" to collect student responses on how they might solve using known facts (e.g. double-double with the four so $(6 \times 2)+(6 \times 2)=24$, double-double with the six so $(3 \times 4)+(3 \times 4)$, or using 2 s facts so $(2 \times 4)+(2 \times 4)+(2 \times 4)=$ 24 , using 3 s facts so $(6 \times 3)+(6 \times 1)=24)$. Consider asking students if doubling will work for 7 (e.g. no because 7 is not a double). You may want to build in additional class practice with counters in modeling and writing the equations for these strategies. <br> Assess and Differentiate/Intervention Activity: <br> If time permits, teach students how to play Teamwork (TE p. 131A). All students should have the opportunity to play this game as this reinforces the idea of using known facts to solve for unknown facts and provides meaningful practice with identifying the known fact and working from that fact. Consider modifying to other factors (e.g. have students role dice to get the factors) for future extended play. |
| :---: | :---: | :---: |
| Lesson 3-5: Apply Properties: 8 as a Factor |  |  |
| 3.OA.B. 5 <br> 3.OA.A. 3 <br> 3.OA.D. 9 <br> MP. 1 <br> MP. 4 <br> MP. 7 <br> MP. 8 | Access Prior Learning: <br> In Topic 2, Grade 3 students identified the patterns in multiplying with 1,2 , and 5 as a factor. In previous lessons within Topic 3, students have developed the understanding that they can use these known facts to solve for facts with $3,4,6$, and 7 as a factor. <br> Developing the Big Idea: <br> This lesson further develops the idea that we can use known facts to solve for unknown facts using the Distributive Property of Multiplication. | Look Back: <br> Consider assigning the Look Back! prompt after the Solve \& Share, and ask groups to take a different factor to share out. These are good ideas to add to the class anchor chart. <br> Visual Learning: <br> Students that are struggling to keep track of all the doubles shown in the Visual Learning Animation may prefer to use the Distributive Property of Multiplication by decomposing the 8 into $5+3$. This also might be a good time to revisit the Commutative Property of Multiplication by posing the question, "For $8 \times 2$, what is the most appropriate/efficient strategy for me to solve (e.g. I know $2 \times 8=16$ so it's 16)?" <br> Convince Me: <br> You might consider discussing the Convince Me! whole group. <br> Independent Practice/Math Practices and Problem Solving: <br> For more information beyond the explanation provided in the Teacher's Edition on Quick Check item 19, watch the Listen and Look For video for this lesson. <br> Assess and Differentiate/Intervention Activity: <br> If time permits, you may consider replacing the Math and Science Activity with the game <br> Teamwork (TE, p. 131A). Please see the comments for this game in Lesson 3-4. |
| Lesson 3-6: Practice Multiplication Facts |  |  |
| 3.OA.B. 5 <br> 3.OA.A. 3 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 4 | Access Prior Learning: In Topic 2, Grade 3 students identified the patterns in multiplying with 1,2 , and 5 as a factor. In previous lessons in this topic students have developed the understanding that they can use these known facts to solve for facts with $3,4,6,7$, and 8 as a factor. <br> Developing the Big Idea: <br> This lesson further develops the understanding that we can use known facts to solve for unknown facts by including using a bar diagram as a model for the math. | Solve \& Share: <br> To assess student readiness, you may consider posing the question, "How can we model multiplication using a bar diagram? What other ways can we model multiplication?" <br> Visual Learning: <br> Consider pausing the video after it shows, "Each section is 3 feet long" and posing the question, "What is our multiplication equation for this problem? (e.g. $9 \times 3=$ ?) How could you solve this?" Provide time for students to solve and use this as an opportunity to see what reasoning strategies students are using to solve. <br> Convince Me: <br> If you already provided time for students to solve for $9 \times 3$, you might consider doing the Convince Me! to have students share their strategies and reasoning that wasn't shown in the video. Having exposure to these strategies would be beneficial for the whole group. <br> Independent Practice/Math Practices and Problem Solving: <br> Students have to reason that a week has 7 days in order to solve item 26; therefore, it might be beneficial to assign this item to build problem solving reasoning habits. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Problem Solving Read Mat with the game Teamwork (TE, p. 131A). Please see the comments for this game in Lesson 3-4. <br> Child-watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p.23A). |

Lesson 3-8: Math Practices and Problem Solving- Repeated Reasoning

Access Prior Learning:
3.OA.B. 5

In this topic students have
3.OA.A. 3
developed understanding of how they can use known facts for 1,2 , and 5 to solve for unknown facts
MP. 8 MP. 1
MP. 3
MP. 5
MP. 7 for $3,4,5,6,7,8$, and 9 focusing mostly on the Distributive Property of Multiplication as a justification for why this works.

## Developing the Big Idea:

In this lesson, students develop their understanding of MP. 8 Use repeated reasoning to secure their understanding of using the Distributive Property of Multiplication as a strategy for solving unknown facts.

This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 9 . Refer to the Math Practices and Problem Solving Handbook (TE p. F28-F28A, F29) for suggestions on how to develop, connect and assess this Math Practice. Also reference the handbook in the student edition (SE, p. F28).

## Solve \& Share:

Consider reintroducing MP. 8 Look for and express regularity in repeated reasoning Thinking Habits (SE, p. F28) before introducing the Solve \& Share. You may want to restate that an equation is an example of MP. 8 Look for and express regularity in repeated reasoning. In this case, the general method we want students to notice is the use of the Distributive Property of Multiplication in solving for unknown facts.

You may also consider using the time where students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP. 8 that are listed in the Math Practices and Problem Solving Handbook (F28A), and afterwards discussing student solution methods and reasoning. Ask students to self-score for the behaviors associated with this math practice.

Finally, during the whole group discussion on students' solution strategies and reasoning, ensure that the generalization recognizes that when decomposing a factor, it's being broken into addends. For further ideas on how to facilitate the conversation so that students recognize this, preview the Listen and Look For video prior to teaching the lesson so that you can use their questions. This understanding is important as students learn to decompose factors and make known facts from unknown facts.

## Visual Learning:

During the Visual Learning Animation, consider asking the students what they decomposed the factors for each equation into to make a known fact (e.g. A 3 was decomposed into the addends 2 and 1, B 4 was decomposed into the addends 2 \& 2, C 6 was decomposed into the addends 5 and 1, D 7 was decomposed into the addends 5 and 2).

## Independent Practice/Math Practices and Problem Solving:

Watch for students that do not recognize the " 35 minutes to bake the pizzas" is extraneous information and try to use it to solve the problem. These students are not reasoning with the context to make sense with the mathematics and need additional support on how to problem solve.

## Assess and Differentiate/Intervention Activity:

If time permits, teach students how to play Clip and Cover (TE, p. 155A). All students should have the opportunity to play the games.

Child-watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p.155A).

## Lesson 3-7: The Associative Property: Multiply by 3 Factors

## 3.OA.B. 5 <br> 3.OA.A. 3

In Topic 2, Grade 3 students identified the patterns in multiplying with 1,2 , and 5 as a factor. In previous lessons in this topic,
MP. 1
MP. 2
MP. 3
MP. 4
MP. 8

Watching the Topic Professional Development Video will help to clarity the ideas around the Associative Property of Multiplication and strengthen facilitation of the Visual Learning Animation during instruction.

## Solve \& Share:

The Listen and Look For video for this lesson goes into detail about how to use this problem to facilitate understanding of the Associative Property of Multiplication.

While students work to solve this problem, watch for those that do not include parentheses as a grouping symbol. These students might be working with the misconception that parentheses are limited to the Distributive Property of Multiplication. Offer the clarification that parentheses are used anytime we want to communicate that we have grouped expressions together.

Watch for students that represent the problem as $(5 \times 3)+(5 \times 3)$ or $15+15$. Help them connect these forms of repeated addition to multiplication; ask students to write a number sentence for this situation using only multiplication. $2 \times 15$ could be a first step. Where did the 15 come from? Do students notice it represents the total number of squares in one quilt? Can they replace the 15 with ( $5 \times 3$ ) to create the number sentence $2 \times(5 \times 3)$ ? Help students to see the equivalence between these different forms. What will happen now if we decide to use the 2 $x(5 \times 3)$ model but instead associate the factors 2 and 5 ? We have created a new number sentence, $(2 \times 5) \times 3$ and a different number sentence of $10 \times 3$. Do students notice that there are 10 rows between the two quilts with 3 squares in each row? The associative property allows us to represent the same situation using different but equivalent number sentence models.

|  |  | Visual Learning: <br> The Visual Learning Animation uses a very similar problem to model use of the Associative <br> Property of Multiplication. Help students make connections between their reasoning and <br> strategies used during the Solve \& Share and those seen in the Visual Learning Animation. |
| :--- | :--- | :--- |
| In this lesson, students have seen that when working with 3 factors, the order they multiply <br> them does not change the final product although it does require an extra step. Connect to our <br> Topic Essential Question, "How can unknown multiplication facts be found using known facts?" <br> by asking, "How can we use the Associative Property of Multiplication to decompose an <br> unknown multiplication fact into known facts? Can we solve $4 \times 2 \times 5$ as $8 \times 5$ or $4 \times 10$ ? How <br> can we use this property to make simpler problems for solving?" |  |  |
| Assess and Differentiate: <br> If time permits, you may consider returning to the game Teamwork (TE p.131A) with a variety of <br> factors (see notes in Lesson 3-4) and have students decomposing the larger arrays into 2 or <br> more small arrays while writing the multiplication equation modeled. |  |  |

## References

Common Core Standards Writing Team. (2011, May 29). Progressions for the Common Core State Standards in Mathematics (draft). K, Counting and Cardinality; Grades K-5, Operations and Algebraic Thinking. Tucson, AZ: Institute for Mathematics and Education, University of Arizona.

Council of Chief State School Officers. (2010). The Nevada Academic Content Standards. Retrieved from http://www.doe.nv.gov/uploadedFiles/nde.doe.nv.gov/content/Standards Instructional Support/Nevada Academic Standards/Math Doc uments/mathstandards.pdf.

Fosnot, C. T., \& Dolk, M. (2001). Young mathematicians at work: Constructing multiplication and division. Portsmouth, N.H.: Heinemann.
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## - Grade 3 Topic 4: Use Multiplication to Divide-Division Facts

Big Conceptual Idea: Operations and Algebraic Thinking (pp. 22-28)
Prior to instruction, view the Topic 4 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 105A-105F), the Topic Planner (pp.165l-165D), all 9 lessons, and the Topic Performance Assessment (pp. 233-234A).

| Mathematical | Topic Essential Question: |
| :--- | :--- |
| Background: | How can unknown division facts be found using known multiplication |
| Read Topic 4 Cluster | facts? |
| Overview/Math | Reference Answering the Topic Essential Question (TE, pp. 229-230) for key elements |
| Background (TE, pp. <br> 105A-105F) | of answers to the Essential Question. |

The lesson map for this topic is as follows:

| $4-1$ | $4-2$ | $4-3$ | $4-4$ | $4-5$ | $4-6$ | $4-7$ | $4-8$ | $4-9$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 3 A/D/E days used strategically throughout the topic | 3rd Grade Curriculum | Pacing Framework: <br> Balanced Calendar |  |  |  |  |  |  |  |

## Instructional note:

This topic focuses on the inverse relationship of multiplication and division and using multiplication to solve division problems. These understandings meet the 2010 Nevada Academic Content Standards (NVACS) 3.OA.B6, "Understand division as an unknown-factor problem. For example, find $32 \div 8$ by finding the number that makes 32 when multiplied by 8 ." Students that understand this inverse relationship realize that they already know division facts because they know the multiplication facts.

Although students explored the concept of division in Topic 1 as fair sharing and repeated subtraction, they have not yet fully explored the relationship between multiplication and division. Students are familiar with using models such as arrays and bar diagrams to represent multiplication situations. Now they will be asked to use these models to explore division situations. For example, given a visual model for the problem $24 \div 6$, "Where is the 24 represented in the model? Where is the 6 represented in the model? Where would the unknown be represented in the model?" Facilitate discussions helping students draw connections between the models, multiplication and division equations, and the inverse relationship between multiplication and division.

As a reminder from Topic 1, there are 2 different types of division problems:
Partitive (dealing or fair sharing): Number of groups are known; the size of each group is unknown
Measurement (chunking): Size of the group is known; the number of groups are unknown

## Focus Math Practice 1: Make sense of problems and persevere

Focus on opportunities for students to develop Mathematical Practice 1 behaviors throughout the entire topic, as this is the focus of the Math Practices and Problem Solving lesson 4-9. Reference the Teacher's Edition (TE, pp. F21-F21A) and the Nevada Academic Content Standards for Mathematical Practice (2010, p. 6).

|  | Essential Academic Vocabulary <br> Use these words consistently during instruction. |  |
| :--- | :--- | :---: |
| New Academic Vocabulary: | Review Academic Vocabulary: |  |
| (First time explicitly taught) | (Vocabulary explicitly taught in prior grades or topics) |  |
| dividend | even |  |
| divisor | odd |  |
| fact family |  |  |
| quotient | multiple |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  | dactors |  |
| division |  |  |
| multiplication |  |  |

Additional terminology that students may need support with: related fact, inverse relationship, opposite

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding question: "Are students able to use the relationship between multiplication and division to find unknown facts?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $4-1$ | Quick Check <br> (digital platform) | Focus CTC around data analysis and collection of student workspace (scratch <br> paper). <br> $\bullet \quad$ students understand that multiplication and division are inverse operations. <br> $\bullet$ students use the inverse operation to determine fact families. <br> Printable version available under "Teacher Resources". |
| $4-7$ | Solve \& Share <br> (student work samples) | Focus CTC around the big idea: <br> $\bullet \quad$ students understand that multiplication and division are inverse operations. <br> $\bullet$ <br> students use the inverse operations and known facts to determine fact <br> families and their equations. |


| Learning Cycle | Topic Assessments | Use Scoring Guide TE pp. 229-234A |
| :---: | :--- | :--- |
| SE pp. 229-234 |  |  |

Standards listed in bold indicate a focus of the lesson.


|  |  | Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 18 as this problem provides a formative assessment opportunity to check for students' understanding of fact families. Students will often think that any 3 numbers can be put together to make a fact family. Lesson $4-2$ will revisit ideas involved with fact families should students demonstrate that they are still struggling. <br> Assess and Differentiate: <br> If time permits, teach students how to play Teamwork (TE, p. 173A). Before assigning any students the Advanced level activity consider asking students to play the On-Level with the modification that students are to create the array and show the related division fact. All students should have the opportunity to play this game. <br> *CTC: Quick Check (digital platform) |
| :---: | :---: | :---: |
| Lesson 4-2: Use Multiplication to Divide with 2, 3, 4, and 5 |  |  |
| 3.OA.B. 6 <br> 3.0A.A. 3 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 6 <br> MP. 7 | Access Prior Learning: In lesson 4-1, students began to develop understanding of the inverse relationship between multiplication and division and the resulting fact families. <br> Beginning of the Big Idea: <br> Students begin to understand that the inverse relationship between multiplication and division can be used to solve for division with a divisor of 2 through 5 . <br> Students are also beginning to develop the understanding that every multiplication fact has a related division fact because of their inverse relationship. | Solve \& Share: <br> Since students are just beginning to develop an understanding that we can use multiplication to solve for division, consider asking what strategies and tools they might use to solve this to ensure that all students have an entry point to this problem. <br> Visual Learning: <br> Consider pausing the Visual Learning Animation after they ask, "Why are you able to use multiplication to help you divide?" (00:21) to get student responses. This will provide you with formative assessment data about whether students are understanding the inverse relationship between these two operations. The Visual Learning Animation asks the question, "What is the division sentence?" for the first problem while showing the division sentence. You may wish to pause the video after they display the multiplication sentence and then ask your students, "What is the division sentence?" <br> The Visual Learning Animation only provides one pause. It may be beneficial for your students to pause the video after they introduce each of the problems so they can have more opportunity to reason with division as an unknown factor problem while receiving immediate feedback through the video. <br> Also consider pausing the video after they introduce Dee's sticker problem (01:33) because the problems up to this point have been Partitive (fair share) division and this is a Measurement (chunking) problem. These division types have different entry level strategies. Partitive problems allow students to use dealing into groups (one at a time or in small quantities) to fair share while measurement division problems allow students to use repeated subtraction. <br> Independent Practice/Math Practices and Problem Solving: <br> Quick Check item 28 Common Core Assessment is Measurement division (chunking) problem. Students have mostly worked with Partitive division (fair share) types so far. See the Instructional Note for more information regarding Measurement division. <br> Assess and Differentiate: <br> If time permits, you may consider having students play the Teamwork game from lesson 4-1 (TE, p. 173A). It is recommended that all students have the opportunity to play the modified version of the Teamwork game from lesson 4-1 before playing the Teamwork game provided in this lesson (TE, p. 179A). <br> Child-watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p.179A). |
| Lesson 4-3: Use Multiplication to Divide with 6 and 7 |  |  |
| 3.OA.B. 6 <br> 3.OA.A. 3 <br> MP. 1 <br> MP. 2 <br> MP. 4 | Access Prior Learning: <br> Students have developed the understanding that inverse relationship between multiplication and division means we can use multiplication to solve for division facts. In previous lessons in this topic, they have used this understanding to solve for division facts that have a divisor of 2 through 5. In Topic 3, Grade 3 students developed strategies for solving multiplication facts with 6 and 7 as a factor. | Solve \& Share: <br> To assess students' readiness to use known multiplication facts with 6 s or 7 s as factors to solve corresponding division facts, consider asking students, "How would you explain how to solve 7 $\times 3$ to a friend that didn't know how?" This question can activate prior learning that students will be extending to new learning. By making this question a journal response that you collect, it can also provide meaningful formative assessment data on what phase students are working in to solve for 7's facts. Students that use repeated addition or skip counting are still in Phase 1, students that used a derived fact (e.g. $(2 \times 7)+7)$ are in Phase 2 , while students that just know it and would tell them it's 21 are in Phase 3. While Phase 3 is not expected at this time, all students progress at different times and speeds. <br> Look Back: <br> Assigning the Look Back! will be beneficial to students still struggling to understand the inverse relationship between multiplication and division. <br> -continues on next page- |

\(\left.$$
\begin{array}{|l|l|l|}\hline & \begin{array}{l}\text { Developing the Big Idea: } \\
\text { Students begin to understand } \\
\text { using known multiplication facts to } \\
\text { solve for a corresponding division } \\
\text { fact by dividing by } 6 \text { or 7. }\end{array} & \begin{array}{l}\text { Visual Learning: } \\
\text { Consider pausing the animation at } 32 \text { seconds after it asks, "What operation should be used to } \\
\text { solve this problem?" Accept both multiplication and division solutions with justifications. } \\
\text { Students that respond with multiplication should also identify the inverse relationship with } \\
\text { division. This is an opportunity to reinforce that multiplication situations are joining equal sized } \\
\text { groups to find a total amount, division situations are separating a total amount into equal sized } \\
\text { groups, and to clarify any misconceptions about the two operations. } \\
\text { Convince Me: }\end{array}
$$ <br>
It may be beneficial to assign the Convince Me! to continue to support conceptual development <br>

of the inverse relationship between multiplication and division.\end{array}\right\}\)| Assess and Differentiate: |
| :--- |




## References

Common Core Standards Writing Team. (2011). Progressions for the Common Core State Standards in Mathematics (draft). K, Counting and Cardinality; Grades K-5, Operations and Algebraic Thinking. Tucson, AZ: Institute for Mathematics and Education, University of Arizona.

Council of Chief State School Officers. (2010). The Nevada Academic Content Standards. Retrieved from http://www.doe.nv.gov/uploadedFiles/nde.doe.nv.gov/content/Standards Instructional Support/Nevada Academic Standards/Math Doc uments/mathstandards.pdf.

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# - Grade 3 Topic 5: Fluently Multiply and Divide within 100 

Big Conceptual Idea: Operations and Algebraic Thinking (pp. 22-28)
Prior to instruction, view the Topic 5 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background pages (pp. 235A-235F), the Topic Planner (pp.235I-235K), all 8 lessons, and the Topic Performance Assessment (pp. 295-296A).

| Mathematical |
| :--- |
| Background: |
| Read Topic 5 Cluster |
| Overview/Math Background |
| (TE, pp. 235A-235F) |

Topic Essential Question:
What are strategies to solve multiplication and division facts?
Reference Answering the Topic Essential Question (TE, pp. 291-292) for key elements of answers to the Essential Question.

The lesson map for this topic is as follows:

| $5-1$ | $5-2$ | $5-3$ | $5-4$ | $5-5$ | $5-6$ | $5-7$ | $5-8$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 4 A/D/E days used strategically throughout the topic. |  |  | 3rd Grade Curriculum <br> Instructional note: | Pacing Framework: |  |  |  |  |

This topic focuses on securing reasoning strategies for multiplication and division within 100 by applying the strategies needed to meet the Nevada Academic Content Standards (NVACS) for standard 3.OA.C.7, "Multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g. knowing that $8 \times 5=40$, one knows $40 \div 5=8$ ) and properties of operations. By the end of Grade 3 , know from memory all products of two one-digit numbers" (2010). It is important to note that this expectation "know from memory all products of two one digit numbers" is not expected until "the end of Grade 3". Encourage students to find connections between facts and look for patterns. Can they derive $x 4$ and x 6 facts based on their knowledge of $x 5$ facts? The acquisition of basic math fact fluency occurs in three phases of development:

Phase I: Constructing meaning and counting strategies<br>Phase II: Reasoning strategies<br>Phase III: Working toward quick recall

These three phases should not be perceived as linear as students often work simultaneously within these phases (Washoe County School District, 2007). The Operations and Algebraic Thinking, K-2 Progression Document states, "Fluency in each grade involves a mixture of just knowing some answers, knowing some answers from patterns (e.g. 'adding 0 yields the same number'), and knowing some answers from the use of strategies. It is important to push sensitively and encouragingly toward fluency of the designated numbers at each grade level, recognizing that fluency will be a mixture of these kinds of thinking which will differ between students" (Common Core Standards Writing Team, 2013, p. 18). In Topic 5 students are working toward fluency. It is important to note that NVACS identify four components of fluency in its definition, which states that fluency is, "skill in carrying out procedures flexibly, accurately, efficiently, and appropriately" (NVACS, 2010, p. 6). Additionally,

This is somewhat different than "instant recall" in that it does not preclude a student's ability to use a known fact to quickly derive an unknown one. Phase III is simply about a student's quick recall. This involves increasing the speed in which the student selects and applies a strategy for solving the problem. (Washoe County School District, 2007)

Topic 5 provides the opportunity for students to continue to practice and select the most appropriate reasoning strategies introduced in previous topics. The question becomes, when do we reach Phase III? The Coherence section of this topic states,

Throughout the rest of Grade 3, students will have many opportunities to consolidate and extend their understanding of multiplication and division and to demonstrate fluency with multiplying and dividing within 100 . By the end of Grade 3, students will know from memory all products of two 1-digit numbers (TE, p. 235D).

However, Phase III can only be achieved when students are provided frequent opportunities to select the most appropriate strategy through exposure to purposeful tasks and games. Prompt students to use a strategy and defend why the strategy they chose was the most appropriate. Encourage them to include the given factors and context of the problems they are using

While the focus of this topic is on the application of multiplication and division strategies we must make connections to how situations can be represented with multiplication. This can be done through connecting the multiplication and division models (bar diagram, arrays, number lines) to the ideas (e.g. joining equal groups, repeated addition, known rows and columns for multiplication and separating equal groups, repeated subtraction, unknown factor for division).

It might be tempting to implement timed fact assessments; however, research indicates that timed tests tend to be harmful to students' mathematical mindsets and can cause life-long math anxiety.

Occurring in students from an early age, math anxiety and its effects are exacerbated over time, leading to low achievement, math avoidance, and negative experiences of math throughout life. Educators have witnessed the impact of math anxiety for decades, but only in recent years have timed math tests been shown to be one cause of the early onset of math anxiety. Indeed, researchers now know that students experience stress on timed tests that they do not experience even when working on the same math questions in untimed conditions (Boaler, 2014, p.469).

The multiplication table is used extensively in Topic 5 as a tool to connect strategies and understandings from previous topics, analyze patterns and make new connections. It is important that the multiplication table is used as a mathematical tool and not only to find products. For example, students will use the table to show the properties of multiplication; as well as, the inverse relationship between multiplication and division. In lesson 5-1 item 13 Common Core
Assessment of the Independent Practice/Math Practices and Problem Solving (shown to the right) illustrates the Commutative Property of Multiplication, as well as, the Identity Property of Multiplication. The multiplication table becomes a crutch for students using it to solve multiplication and division facts without attempting reasoning strategies or application of derived facts. Such procedural use will not result in students reaching Phase III, but instead will keep them dependent upon the multiplication tool to solve basic facts.


## Focus Math Practice 7: Look for and make use of structure

Focus on opportunities for students to develop Mathematical Practice 7 behaviors as this is the focus of the Math Practices and Problem Solving lesson 5-8. Reference the Teacher's Edition (TE, pp. F27-F27A) and the Nevada Academic Content Standards for Mathematical Practice (2010, p. 8).

Looking ahead to the Topic Performance Assessment, Part B asks students to explain how they could have figured out Part A by comparing multiplication equations. In lesson 5-8 students apply MP. 7 "Look for and make use of structure" to generate multiplication equations from contexts with comparison symbols (through reasoning) to solve a multi-step problem. Developing the thinking habits that allow students to engage in this problem type is highly beneficial.

## Meaningful Fluency Practice \& Assessment:

As stated above, the focus of this topic is on securing reasoning strategies for multiplication and division within 100 by applying an appropriate strategy and properties of operations. The version of the How Close to 100 game at the end of this document is appropriate for students that have demonstrated security with use of strategies and properties of operations to solve for facts with all factors. Games from previous topics should continue to be used based on student needs.

Phase 3: How Close to 100 (game directions and materials found at the end of this document)
Directions: Player 1 roles 2 dice. The numbers that come up are the factors. The player then draws the array on the shared grid anywhere, so long as it does not overlap another array, and writes the equation that describes the array.
Player 2 repeats the same process. Each player continues in turn until both players have rolled the die and cannot put any more on the grid.

| Essential Academic Vocabulary <br> Use these words consistently during instruction. |  |  |
| :--- | :--- | :--- |
|  |  | Review Academic Vocabulary: <br> New Academic Vocabulary: <br> (First time explicitly taught) |
|  | factor | Commutative (turn-around) Property of |
|  | multiple | Multiplication |
|  | product | Distributive (break-apart) Property of |
|  | dividend | Multiplication |
|  | divisor | Associative (order) Property of |
|  | quotient | Multiplication |

Additional terminology that students may need support with: strategy

## Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding question: "Are students using the properties of multiplication, tools, strategies or models to multiply whole numbers?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $5-1$ | Quick Check <br> (digital platform) | Focus CTC around data analysis and collection of student workspace (scratch <br> paper). <br> students use their knowledge of facts and the distributive property to see <br> patterns in factors and products on the multiplication table. |
| Printable version available under "Teacher Resources". |  |  |


| Learning Cycle | Topic Assessments |
| :---: | :--- | :--- |
| SE pp. 291-296 |  |$\quad$ Use Scoring Guide TE pp. 291-296A



\begin{tabular}{|c|c|c|}
\hline \multicolumn{3}{|l|}{Lesson 5-2: Use a Multiplication Table} \\
\hline \begin{tabular}{l}
3.OA.C. 7 \\
MP. 1 \\
MP. 2 \\
MP. 3 \\
MP. 4
\end{tabular} \& \begin{tabular}{l}
Access Prior Learning: In Topic 4, Grade 3 students developed understanding of the inverse relationship between multiplication and division to help solve division facts. \\
Securing the Big Idea: Students secure the understanding of multiplication as joining equal groups of objects, thinking of division as a missing factor multiplication problem, and their inverse relationship by using the multiplication table to model these connections.
\end{tabular} \& \begin{tabular}{l}
Instructional note: \\
As students used the addition table in \(2^{\text {nd }}\) grade, it may be beneficial to compare and contrast the multiplication table from the addition table at some point in the lesson. Ideas to bring out include: \\
- Just as the addends are on the outside of the addition table, factors are on the outside of the multiplication table. \\
- Just as the sums are on the inside of the addition table, products are on the inside of the multiplication table. \\
- The addition table can be used to solve subtraction problems and the multiplication table can be used to solve division problems. \\
- Contrast the difference in language; addition uses addends to make sums and multiplication uses factors to make products. \\
Solve \& Share: \\
Watch for students who look for any 18 in the Multiplication Chart, but don't necessarily align it with the 3 as a factor. For those that do identify 6 as the missing factor, look for understanding by asking them how they found 6 as the quotient. We want students to be able to explain that they intentionally looked for 18 in the 3's column (or row). \\
If possible, have a student that used an understanding of the inverse multiplication/division relationship and the Multiplication Table to solve a division problem share their reasoning and explain their strategy. \\
Guided Practice: \\
For the Guided Practice, it is not necessary for students to do all of the items. Child-watch to determine when it's appropriate to move to the Quick Check items. \\
Independent Practice/Math Practices and Problem Solving: \\
Consider assigning items 24 and 25 to give students an opportunity to work with additive compare problems and reading charts. \\
Assess \& Differentiate: \\
If time permits, you may consider replacing the Problem-Solving Reading Mat with games from previous topics or the Fluency Practice Activity (TE, p. 285). \\
Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p.247A).
\end{tabular} \\
\hline \multicolumn{3}{|l|}{Lesson 5-3: Find Missing Numbers in a Multiplication Table} \\
\hline 3.OA.C. 7

MP. 2
MP. 3
MP. 4

MP. 6 \& \begin{tabular}{l}
Access Prior Learning: <br>
In Topic 3, Grade 3 students developed strategies for using known facts to solve for unknown facts by using the properties of multiplication. In Topic 4, Grade 3 students developed understanding of the inverse relationship between multiplication and division to solve division facts. <br>
Securing the Big Idea: <br>
Students secure the understanding of multiplication strategies for solving for an unknown fact by using a known fact, solving for division facts by thinking of division as a missing factor multiplication problem, and their inverse relationship by using the multiplication table to model these connections.

 \& 

Instructional note: <br>
The Solve \& Share for this lesson requires students to apply all the previous learning stated in Access Prior Learning. This is a very meaningful and powerful task with a high level of cognitive demand. Scaffolds may be needed to support students' engagement in productive struggle throughout the task. It is recommended that teachers engage in child watching to provide scaffolds when students demonstrate that they are in a state of struggle versus productive struggle (e.g. productive struggle has evidence of students asking questions and using reasoning to attempt the problem). <br>
Solve \& Share: <br>
Consider asking the questions provided in Build Understanding (TE, p. 249) with time to think and/or share with a partner. Can students generate possible solution strategies they might attempt for finding unknowns in the multiplication chart? Share students' ideas as a whole group and post strategy suggestions. Allow student differentiated (independent, partner, or group work) time on the Solve \& Share. <br>
After students have had time to think and collaborate, it may be beneficial to scaffold the problem for some and give the products for the $5^{\text {th }}$ row down (where students need to figure out that 7 is the factor). You may consider bringing the class together to share and discuss when students are able to share some solution strategies; even if they haven't fully completed the multiplication table. <br>
Assess and Differentiate: <br>
If time permits, you may consider replacing the Math and Science Activity with games from previous topics or the Fluency Practice Activity (TE, p. 285).
\end{tabular} <br>

\hline
\end{tabular}



|  | , |  |
| :---: | :---: | :---: |
| 3.OA.C. 7 <br> 3.OA.A. 3 <br> MP. 1 <br> MP. 4 <br> MP. 5 <br> MP. 6 <br> MP. 8 | Access Prior Learning: In Topics1 \& 4, Grade 3 students learned to think of division as separating an amount into equal sized groups and developed strategies for solving division problems. <br> Securing the Big Idea: This lesson secures the understanding that division situations involve separating an amount into equal sized groups and develops students' strategies for solving by asking them to write a division problem. | Solve \& Share: <br> Writing their own division stories provides students with an opportunity to demonstrate their understanding of division situations and a formative assessment opportunity for teachers. Creating problems is often challenging, but also engaging for students. <br> Watch for students that create the same problem type for both their division word problems. (see Instructional note at the beginning of Topics 1 and 4 for more details on the 2 different types of division) Students should write one problem with the number of groups as an unknown and another problem with the amount in each group as an unknown. For students that are struggling, provide support by asking the questions provided under Ask Guiding Questions As Needed (TE, p. 273). During the whole class discussion on student solutions and reasoning, consider using the "My Favorite No" (title is hyperlinked to a video to explain instructional strategy) with a student's work where the 2 problems are only 1 problem type. As a class, discuss whether there are 2 different division problem types present and how to revise one of the problems so that there are 2 different division problem types. <br> Convince Me: <br> Consider assigning the Convince Me! to help students secure their understanding that there are 2 different problem types for division. <br> Assess and Differentiate: <br> If time permits, teach students how to play "Display the Digits" (TE, p. 277A), consider asking students to write down at least 2 of the division stories they create that includes 1 of each type of division situation. <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p.277A). |
| Lesson 5-8: Math Practices and Problem Solving- Look for and Use Structure |  |  |
| MP. 7 MP. 1 MP. 3 MP. 4 3.OA.C. 7 | Access Prior Learning: <br> In Topics 2 through 4, students used the structure of numbers (decomposing numbers), the multiplication chart to identify patterns, fact families, and the properties of multiplication to solve multiplication and division problems. <br> Securing the Big Idea: In this lesson, students secure their understanding of multiplication and division situations, and develop further understanding of looking for and using mathematical structures by identifying patterns and comparing equations. | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 7. Refer to the Math Practices and Problem Solving Handbook (TE, pp. F27-F27A, F29) for suggestions on how to develop, connect, and assess this Math Practice. <br> Solve \& Share: <br> Consider reintroducing MP. 7; "Look for and use structure" Thinking Habits (SE, p. F27) before introducing the Solve \& Share. Ask students how we can use structure to use a known fact to solve for unknown facts. Consider using the time when students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP. 7 that are listed in the Math Practices and Problem Solving Handbook (TE, p. 27A). After discussing student solution methods and reasoning strategies, consider having students self-score for the behaviors associated with this math practice. <br> Convince Me: <br> Consider assigning the Convince Me! as it provides an opportunity for students to apply MP. 7 by explaining the use of the Zero and Identity Properties of Multiplication. <br> Assess and Differentiate <br> If time permits, teach students how to play "Clip and Cover" (TE, p. 283A) as this relates the mathematics developed in this topics to a real world context. <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 283A). |

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## How Close to 100?

## Mathematical Understanding:

Building fluency with factors, multiples, and recall of single-digit multiplication facts.

Grade Level: 3<br>Number of Players: 2<br>Materials Needed: How Close to 100 ? gameboard, 2 dice, pen or pencil

## Object of the Game:

The goal is to fill up the grid to get it as full as possible.

## Directions:

Player 1 roles 2 dice. The numbers that come up are the factors. The player then draws the array on the shared grid anywhere, so long as it does not overlap another array, and writes the equation that describes the array.

Player 2 repeats the same process.
Each player continues in turn until both players have rolled the die and cannot put any more on the grid.

## Guiding Questions:

What are you going to try?
What did you think about to come to your answer?
Is there another way you could figure it out?
Can you think of another fact that strategy would work well for?
What equation was the hardest for you to do? Why?
What equation was the easiest for you to do? Why
Differentiation:
Each player can have their own number grid. Play moves forward to see who can get closest to 100 .

## Game Trajectory:

Grade 3 Fall: Players use 1 die to generate a factor and then choose the other factor from $1,2,5,10$ based on which will yield the array that is the most strategic.

Grade 3 Winter: Players use 1 or 2 dice depending on comfort with factors $3,4,6,7,8$, and 9 . Players that need more practice with one of the factors should play with 1 dice and select the difficult factor as a "fixed factor" (will be used for all arrays) and use the die to generate the other factor.

Grade 3 Spring: Players use 2 dice to generate both factors.

Clean up Checklist for Game Bag:
Copies of gameboard
2 Dice
Markers, crayons, pencils, or pens

## How Close to 100? Using Known Facts



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## - Grade 3 Topic 6: Connect Area to Multiplication and Addition

Big Conceptual Idea: Measurement and Data (Measurement Part) (pp. 16-18)
Prior to instruction, view the Topic 6 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 297A-297F), the Topic Planner (pp.297l-297K), all 7 lessons, and the Topic Assessments (pp. 353-354A).

| Mathematical | Topic Essential Question: |
| :--- | :--- |
| Background: | How can area be measured and found? |
| Read Topic 6 Cluster |  |
| Overview/Math Background |  |
| (TE, pp. 297A-297F) | Reference Answering the Topic Essential Question (TE, pp. 349-350) for key <br> elements of answers to the Essential Question. |

The lesson map for this topic is as follows:

| $6-1$ | $6-2$ | $6-3$ | $6-4$ | $6-5$ | $6-6$ | $6-7$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2 AIDIE days used strategically throughout the topic |  | 3rd Grade Curriculum |  |  |  |  |  |
| Instructional note: |  |  |  |  |  |  |  |

This topic focuses on cluster heading 3.MD.C "Geometric measurement: understand concepts of area and relate area to multiplication and division" (2010, NVACS). This topic focuses on beginning to understand the measure of area. A key idea that students need to conceptualize is that area is an attribute of an object that can be measured. The total number of same-sized square units needed to cover a region without having gaps or overlaps determines the quantity. In $3^{\text {rd }}$ grade, area is described by multiplication expressions such as $3 \times 4$ an area model with 3 rows of 4 same sized units.

Students build on their understanding of multiplication and repeated addition to begin to understand area concepts. To connect this idea to prior learning from this year continue to ask students the following questions when applicable:

- Explain how determining the area of an object is similar to using an array to show a multiplication equation.
- Where is the repeated addition in this shape? (Asking this question before determining the area of irregular shapes can allow students to generalize this idea and transfer more easily to finding the area of irregular shapes.)
- How can the Distributive Property of Multiplication help us to find the total area of large objects?

Lessons 6-5, 6-6, 6-7 work with students to apply the Distributive property to compose or decompose rectilinear figures into two or more rectangles. Making this connection explicit through classroom discussion will help students to generalize these understandings and conceptualize finding the area of irregular rectilinear figures.

Note that our goal in this topic is not to formalize a formula for area, but rather to see the relationships that exist between area and the operations of multiplication and addition. This relationship is revealed through the spatial structure (MP.7) of two-dimensional shapes in the number of square units in a row and the number of rows or columns. Strongly emphasize throughout this unit that when finding area, the result is reported in square units. Students also learn that the area depends upon the size of the units used to cover the entire figure. Laying this foundation in grade 3 will provide students with the necessary prior knowledge needed to generate the formula in grade 4.

## Focus Math Practice 7: Look for and make use of structure

Focus on opportunities for students to develop Mathematical Practice 7 behaviors throughout the entire topic, as this is the focus of the Math Practices and Problem Solving lesson 6-7. Reference the Teacher's Edition (TE, pp. F21-F21A) and the Nevada Academic Content Standards for Mathematical Practice (2010, p. 8).

Looking ahead to the Topic Performance Assessment, students will be expected to find the area of rectilinear shapes within a larger rectilinear area, create a figure with a set area, explain why we can multiply to determine the area of a figure and explain decomposing a rectilinear area to find smaller areas or to determine the area of irregular shapes. While developing the thinking habits that allow students to engage in this problem type are highly beneficial, you may need to scaffold working with the Topic Performance Assessment.

|  | Essential Academic Vocabulary <br> Use these words consistently during instruction. |  |
| :--- | :--- | :--- |
| New Academic Vocabulary: <br> (First time explicitly taught) | Review Academic Vocabulary: <br> (Vocabulary explicitly taught in prior grades or topics) |  |
| area | estimate | length |
| unit square | addend | inches |
| square unit(s) | array | feet |
|  | equal groups | centimeters |
|  | multiply | meters |
|  | row | rectangle |
|  |  | square |

Additional terminology that students may need support with: decompose, non-standard

Collaborative Team Conversations (CTC)
Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding question: "Are students using their understanding of multiplication and addition to find the area of a figure?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $6-3$ | Math Practices and Problem Solving <br> (student work samples) | Focus CTC around the big idea: <br> $\bullet \quad$ students communicate the area of a shape by using standard units. |
| $6-6$ | Solve \& Share <br> (student work samples) | Focus CTC around the big idea: <br> students determine the area of an irregular shape by decomposing the <br> irregular shape into rectangles. |


| Learning Cycle <br> Assessments (summative) | Topic Assessments <br> SE pp. 349-354 | Use Scoring Guide TE pp. 349-354A |
| :---: | :--- | :--- |


| NVACS <br> (Content and Practices) | Mathematical Development of the Big Idea | Instructional Clarifications \& Considerations |
| :---: | :---: | :---: |
| Lesson 6-1: Cover Regions |  |  |
| $\begin{gathered} \text { 3.MD.C.5a } \\ \text { 3.MD.C.5b } \\ \text { 3.MD.C. } 6 \\ \\ \text { MP. } 1 \\ \text { MP. } 2 \\ \text { MP. } 3 \\ \text { MP. } 5 \\ \text { MP. } 6 \end{gathered}$ | Access Prior Learning: <br> At the end of second grade students covered rectangles with rows and columns of squares. <br> Developing the Big Idea: <br> Students are beginning to understand that the amount of space inside a shape is its area, and area can be found or estimated using unit squares. | Topic Opener: <br> Introduce the Topic Essential Question, "How can area be measured and found?" (TE, p. 297). Consider making an anchor chart in your classroom. Each day new ideas are added so that students are able to see the development and connections throughout the topic. <br> Consider having students complete the Review What You Know prior to beginning instruction on topic 6 so that you can respond to students' instructional needs using the Item Analysis for Diagnosis and Intervention (TE, pp. 298-300) prior to beginning the topic. <br> Consider introducing vocabulary as students encounter academic language in the lessons rather than introducing all terms at the beginning of the lesson. <br> Solve \& Share: <br> Students will need Teaching Tool 12 found in the Teacher's Resource Master Volume 2 to solve the problem. Watch for students that find the area by covering the shapes with the square tiles, decompose the shape, then multiply the sub-units, and add the sub-units together to find the total area. Consider having this student share their solution strategy and reasoning last as they have already connected understanding of multiplication to finding area. <br> Look Back: <br> Consider discussing as a whole group the Look Back! as this directly addresses a key idea in area concepts; area is a measure of two-dimensional shapes of square units needed to cover a region without having gaps or overlaps. Consider asking students the same question, but in this case, there are overlapping tiles. |


|  | Another Example: <br> Consider discussing the Another Example! (TE, pp. 303-304) should students still seem to be <br> unclear about finding area using partially filled unit squares before assigning the Quick Check <br> items. <br> Assess and Differentiate: |  |  |  |  |  |
| :--- | :--- | :--- | :---: | :---: | :---: | :---: |
| If time permits, you may consider replacing the Problem Solving Reading Mat with games from |  |  |  |  |  |  |
| previous topics. The "Teamwork" game from lesson 3-4 (TE, p. 131A) has students practicing |  |  |  |  |  |  |
| decomposing arrays to find the total number of objects. Revisiting this game at this time could |  |  |  |  |  |  |
| help activate prior learning that will be generalized to finding area of shapes. |  |  |  |  |  |  |
| Child-watch to identify students who need additional support and pull them in a small group to |  |  |  |  |  |  |
| do the Intervention Activity (TE, p. 305A). |  |  |  |  |  |  |


|  | Developing the Big Idea: <br> Students develop understanding of communicating the area of a shape by using standard units of length, such as inches, centimeters, etc. | Independent Practice/Math Practices and Problem Solving: <br> Students who are struggling with solving item 15 may need to draw a picture like the one they may have for item 1. <br> Assess and Differentiate: <br> If time permits, consider replacing the Problem Solving Reading Mat with game "Teamwork" (TE, p. 311A). All students should have the opportunity to play this game. <br> Child-watch to identify students who need additional support and pull them in a small group to do the Intervention Activity (TE, p. 317A). <br> *CTC: Math Practice and Problem Solving (student work samples) |
| :---: | :---: | :---: |
| Lesson 6-4: Area of Squares and Rectangles |  |  |
| 3.MD.C.7a <br> 3.MD.C.7b <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 8 | Access Prior Learning: <br> In previous grades, students have learned that a square has 4 sides that measure the same length. In previous topics in Grade 3, students have used arrays to model multiplication to show the repeated addition of rows and columns to find the total. <br> Developing the Big Idea: <br> In this lesson students further develop their understanding of area by beginning to understand the relationship between area and multiplication. | Solve \& Share: <br> Consider asking students what they know about squares to assess students' readiness for finding the area of a square. Students need to recall that a square has 4 sides that measure the same length. This is necessary so that they are able to apply the understanding to finding the area of a square where only one side's measure is given. <br> Watch for students that do not recognize that when we are finding the area of a square, the other side's measures will also be 6 meters. Revisit what we know about squares that can help determine the area of the shape. <br> Watch for students that solve using Kyoko and Shelly's work (TE, p. 319). Consider having a student whose solution method is similar to Kyoko's share first as most students in the class should be able to understand the method of drawing in the unit squares and counting each unit square. Consider having the student whose solution method is similar to Shelly's share last as this student understands how area measurements connect to multiplication. <br> Visual Learning: <br> Consider pausing the Visual Learning Animation after it shares another way to find the area by counting the number of rows and multiply by the number in each row. Ask students, "Why can we multiply?" (E.g., we have equal rows of 6 so we could skip count by 6 or use repeated addition of 6.) Throughout the Visual Learning Animation consider asking students, where is the repeated addition in this shape, to facilitate connecting multiplication to area. <br> Independent Practice/Math Practices and Problem Solving: <br> For Quick Check item 7 encourage students to use what they know of multiplication and division to solve for the unknown side length. Students did this in topic 4 when they compared and contrasted what was known and unknown in a multiplication array versus a division array. Item 11 of the Quick Check offers distributed practice of multiplication concepts learned in lesson 2-4 Multiply by 10 to an area context. <br> Assess and Differentiate: <br> If time permits, teach students how to play "Clip and Cover" (TE, p. 323A). Consider providing students with centimeter grid paper so that they can draw, see, and label the rectangles and areas they are creating. All students should have the opportunity to play this game. <br> Child-watch to identify students who need additional support and pull them in a small group to do the Intervention Activity (TE, p.323A). |
| Lesson 6-5: Apply Properties- Area and the Distributive Property |  |  |
| 3.MD.C.7c <br> MP. 1 <br> MP. 3 <br> MP. 4 <br> MP. 7 <br> MP. 8 | Access Prior Learning: <br> In topic 3, Grade 3 students used the Distributive Property of Multiplication to break a large array into smaller arrays of known facts to solve for unknown multiplication problems. <br> Developing the Big Idea: Students further develop understanding of area as the measure of unit squares inside a shape by modeling the Distributive Property of Multiplication using rectangles. | Solve \& Share: <br> After students have shared their solution methods and reasoning, consider asking if they could find the full area of the floor. Ask, "How does this connect to the Distributive Property of Multiplication?" Students will more easily be able to understand how to find the area of irregular shapes if in this lesson they connect using the Distributive Property of Multiplication to solving for unknown multiplication facts by breaking a larger array into smaller arrays of known facts. <br> Visual Learning: <br> To help students understand that decomposing the rectangle into smaller rectangles does not change the total area, connect topic 3 learning of breaking larger arrays into smaller arrays of known facts to find the product of unknown facts. <br> Convince Me: <br> Consider assigning the Convince Me! and having students post their solution methods for a Gallery Walk. Focus the walk on identifying different ways to break up the large area into smaller areas. <br> -continues on next page- |


|  |  | Assess and Differentiate: <br> If time permits, you may consider replacing Math and Science Center Activity with either the game "Teamwork" (TE, p. 311A), "Clip and Cover" (TE, p. 323A) or the Fluency Practice Activity (TE, p. 343). |
| :---: | :---: | :---: |
| Lesson 6-6: Apply Properties- Area of Irregular Shapes |  |  |
| 3.MD.C.7d MP. 1 MP. 2 MP. 7 $M P .8$ | Access Prior Learning: <br> In previous lessons in this topic, students learned how to find the area of rectangles building on their understanding of multiplication and the Distributive Property of Multiplication to decompose large areas into smaller areas of known multiplication facts. <br> Developing the Big Idea: <br> In this lesson, students further develop their understanding of area by exploring that the area of irregular shapes can be found by dividing the original shapes into rectangles, finding the area of each rectangle, and adding all of the areas. | Solve \& Share: <br> After introducing the Solve \& Share consider asking students how today's Solve \& Share is similar to what they have done in previous lessons in this topic. Pose questions to get students to share out the following ideas: <br> - they are still finding the area of a shape <br> - they can decompose the shape so that they are still finding the area of rectangles. <br> For struggling students, you may want to offer geoboards, or if geoboards are not available use centimeter grid paper (Teaching Tool 13). Ask students how this tool might help them find the area (e.g., students would need to redraw the figure with each square centimeter being equivalent to a foot on the drawn figure in their book). For students that use the grid paper and count each individual square centimeter consider pairing them with a student that decomposed the shape into rectangles and solved by multiplying the sides of each decomposed rectangle and then added the areas. <br> After students have shared their solution method and reasoning (if they have not already explained how they knew they could multiply the sides to get the area), consider posing a question that will make the connection to multiplication explicit. <br> Convince Me: <br> After viewing the Visual Learning Animation, consider having students solve the Convince Me! with geoboards, or if geoboards are not available use centimeter grid paper (Teaching Tool 13). Have students share the different ways they could divide the shape. As a whole class, discuss how all the shapes still have the same area. A common misconception students will often develop is that changing the way they decompose the original shape will change the area measurement. After students have reviewed each other's solutions consider asking students what was the most efficient way to decompose the shape? <br> Guided Practice: <br> Item 4 on Guided Practice requires students to reason with the measures offered to determine the measures of unknown sides. Consider asking students that figured it out to share with the whole class how they figured out the measures of the unknown sides. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 10 to assess formatively students' development of the mathematical vocabulary in this topic. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Problem Solving Reading Mat with either the game "Teamwork" (TE, p. 311A), "Clip and Cover" (TE, p. 323A) or the Fluency Practice Activity (TE, p. 343). <br> *CTC: Solve \& Share (student work samples) |
| Lesson 6-7: Math Practices and Problem Solving- Look for and Use Structure |  |  |
| 3.MD.C.7a <br> 3.MD.C.7b <br> 3.MD.C.7d <br> MP. 7 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 5 <br> MP. 6 | Access Prior Learning: <br> In this topic students have developed an understanding of area and how to find the area of regular and irregular shapes. <br> Developing the Big Idea: In this lesson, students continue to develop their understanding of area and finding the area of irregular shapes by applying MP. 7 to find the area in real-world contexts. | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 7. Refer to the Math Practices and Problem Solving Handbook (TE, pp. 27A-27F, F29) for suggestions on how to develop, connect and assess this Math Practice. Also, reference the handbook in the Student Edition (SE, p. 27F). <br> Solve \& Share: <br> Consider reintroducing MP. 7 Thinking Habits (SE, p. 27F) before introducing the Solve \& Share. Consider using the time when students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP. 7 that are listed in the Math Practices and Problem Solving Handbook (TE, p. 27A). After discussing student solution methods and reasoning, have students self-score for the behaviors associated with this math practice. <br> Assess and Differentiate: <br> If time permits, teach students how to play "Display the Digits" (TE, p. 323A). All students should have the opportunity to play this game. |

## References

Common Core Standards Writing Team. (2012). Progressions for the Common Core State Standards in Mathematics (draft). Grades K-5, Measurement and Data. Tucson, AZ: Institute for Mathematics and Education, University of Arizona.

Council of Chief State School Officers. (2010). The Nevada Academic Content Standards. Retrieved from http://www.doe.nv.gov/uploadedFiles/nde.doe.nv.gov/content/Standards Instructional Support/Nevada Academic Standards/Math Doc uments/mathstandards.pdf.

## - Grade 3 Topic 7: Represent and Interpret Data

Big Conceptual Idea: Measurement and Data (Data Part) (pp. 7-8)

Prior to instruction, view the Topic 7 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 355A-355F), the Topic Planner (pp. 355l-355J), all 5 lessons, and the Topic Performance Assessment (pp. 399-400A).


Read Topic 7 Cluster
Overview/Math
Background (TE, pp.
355A-355F)

## Topic Essential Question:

How can data be represented, interpreted and analyzed?
Reference Answering the Topic Essential Question (TE, pp. 395-396) for key elements of answers to the Essential Question.
\(\left.\begin{array}{|c}Topics 7 <br>
Represent and <br>

Interpret Data\end{array}\right\}\)| Number of |
| :--- |
| Lessons: 5 |
| A/D/E: $\mathbf{2}$ days |
| NVACS Focus: |
| MD.B |
| Total Days: $\sim \mathbf{7}$ |

The lesson map for this topic is as follows:
Pacing Framework:

| $7-1$ | $7-2$ | $7-3$ | $7-4$ | $7-5$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- |

2 A/D/E days used strategically throughout the topic
Balanced Calendar

## Instructional note:

In this topic, students explore and create picture graphs and bar graphs as a means to interpret categorical data. Categorical data is data that can be grouped by category or attribute. As a result, an important misrepresentation to look for and address is having the bars touch. In bar graphs, the bars should not be touching unless we have grouped categories of a main category. See image 1 for an example of this type of bar graph. Students do not encounter scenarios such as this in grade 3. For those interested in deepening their own content knowledge consider this resource from NC State University (https://www.ncsu.edu/labwrite/res/gh/gh-
 bargraph.html).

An important idea students will be exploring is scaling. This builds on the work that has been done so far this year in multiplication. Students will be using scaled graphs to interpret the data represented. Students will determine the most appropriate scale for representing data shown in a frequency table that will be transferred to either a picture graph or a bar graph.

The K-5, Measurement and Data (Data Part) progression document states that, "They (students) can solve one- and two-step 'how many more' and 'how many less' problems using information present in scaled bar graphs" (p.7). Students will have an opportunity to work with several different problem types, some that may prove challenging. When working with contextual problems avoid connecting specific words to a specific operation, often referred to as "keyword strategies." In the article 13 Rules that Expire, Karp, Bush, and Dougherty (2014) state:

Using keywords often encourages students to strip numbers from the problem and use them to perform a computation outside of the problem context. Unfortunately, many keywords are common English words that can be used in many different ways...reducing the meaning of an entire problem to a simple scan for key words has inherent challenges. Keywords become particularly troublesome when students begin to explore multistep word problems because they must decide which keywords work with which component of the problem (Clement \& Bernard, 2005, p, 21).

Finally, the Measurement and Data (Data Part) progression document states that students can collect their own data in the context of other content areas that can be communicated through either a picture graph or bar graph. The Math and Science Project for this topic does provide the opportunity for students to collect and represent data. This may be a good extension for students that are ready for this activity. It is important to note that the progression document also states that, "The standards in grades 1 through 3 do not require students to gather categorical data" (p. 7).

## Focus Math Practice 6: Attend to precision

Focus on opportunities for students to develop Mathematical Practice 6 behaviors, as this is the focus of the Math Practices and Problem Solving lesson 7-5. Reference the Teacher's Edition (TE, pp. F26-F26A) and the Nevada Academic Content Standards (NVACS) for Mathematical Practice (p. 7).

Looking ahead to the Topic Performance Assessment, students will be expected to solve problems from data presented in scaled bar and picture graphs that use comparative language found in the compare problem types for NVACS Math p. 88-89. Students will also be expected to self-select from a variety of options the most appropriate scale and create a picture graph based on a provided set of
data. Throughout instruction, to support students' development of selecting an appropriate scale for a graph based on data, consider frequently discussing with students the reason why the scales were chosen in the graphs. While developing the thinking habits that allow students to engage in this problem type are highly beneficial, you may need to scaffold working with the Topic Performance Assessment.

| Essential Academic Vocabulary <br> Use these words consistently during instruction. |  |
| :---: | :---: |
| New Academic Vocabulary: <br> (First time explicitly taught) | Review Academic Vocabulary: <br> (Vocabulary explicitly taught in prior grades or topics) |
| data scaled picture graph key scaled bar graph frequency table survey | tally <br> multiplication equal groups number line multiples scale graph |

Additional terminology that students may need support with: information, symbol, conclusion, analyze, record

## Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding question: "Are students able to represent, interpret and analyze data?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $7-1$ | Quick Check <br> (digital platform) | Focus CTC around data analysis and collection of student workspace (scratch <br> paper). <br> $\bullet \quad$ students analyze and interpret scaled pictures and bar graphs. <br> students understand the key shows the units used. <br> Printable version available under "Teacher Resources". |
| $7-3$ | Solve \& Share <br> (student work samples) | Focus CTC around the big idea: <br> students can make, read and analyze bar graphs using information from a <br> table. |


| Learning Cycle <br> Assessments (summative) | Topic Assessments <br> SE pp. 395-400 | Use Scoring Guide TE pp. 395-400A |
| :---: | :--- | :--- |

Standards listed in bold indicate a focus of the lesson.

| NVACS <br> (Content and Practices) | Mathematical Development of the Big Idea | Instructional Clarifications \& Considerations |
| :---: | :---: | :---: |
| Lesson 7-1: Read Picture Graphs and Bar Graphs |  |  |
| $\begin{aligned} & \text { 3.MD.B. } 3 \\ & \text { 3.OA.A. } 3 \end{aligned}$ | Access Prior Learning: In Grade 2 students read and interpreted bar and picture graphs with single-unit scales. | Topic Opener: Introduce the Topic Essential Question, "How can data be represented, interpreted, and analyzed?" (TE, p. 355). |
|  |  |  |
|  |  |  |
| MP. 2 | Developing the Big Idea: <br> Students are developing | Consider having students complete the Review What You Know prior to beginning instruction on topic 3 to respond to students' instructional needs using the Item Analysis for Diagnosis and Intervention prior to beginning the topic (TE, p. 356-358). |
| MP. 6 |  | Consider introducing vocabulary as students encounter the academic language in the lessons rather than introducing all terms at the beginning of the lesson. |
| MP. 8 | understanding using scaled picture and bar graphs to compare data. Students develop understanding of how to interpret data in a scaled picture, using the key and that the scale for a bar graph shows the units used. |  |
|  |  | Solve \& Share: <br> Consider making sure, that after you pose the question, "What do you need to use to solve this problem?" (TE, p. 359) students recognize the key and demonstrate understanding of what it means for the picture graph. |
|  |  |  |
|  |  | Consider ensuring that the last student that shares has understanding of the structure of multiplication and can explain how they used multiplication to solve. |


|  |  | Visual Learning: <br> Consider pausing the Visual Learning Animation after the final pause when it asks, "What is another way to find how many more teams the East Falls League has than the South Falls League?" If students recognize that they can just compare the two rows and identify the difference between the two rows (e.g. there are 3 more hockey sticks in East Falls row than in South Falls row) discuss which solution method (calculating both teams amounts and subtracting or identifying the difference in rows) is more efficient. If students do not come up with the method of comparing the rows, play the animation and then discuss efficiency. <br> After viewing and discussing the Visual Learning Animation consider asking students why using a scaled picture graph would be helpful (e.g. a scaled picture graph more easily represents larger sets of data). <br> Another Example: <br> Consider discussing the Another Example! as a class as students have only reasoned with scaled picture graphs. Consider asking students how the two graphs are similar (e.g. both represent data with a scale, both are useful for comparing data, both having heading, items being compared that are identified, etc.) <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 7 to provide students with distributed practice using comparative symbols. <br> Assess and Differentiate: <br> Consider using the Math and Science Activity as stated in the Instructional Note above or consider replacing with games from previous topics or the Fluency Practice Activity (TE, p. 389). <br> Child-watch to identify students who need additional support and pull them in a small group to do the Intervention Activity (TE, p. 389A). <br> *CTC: Quick Check (digital platform) |
| :---: | :---: | :---: |
| Lesson 7-2: Make Picture Graphs |  |  |
| 3.MD.B. 3 <br> 3.OA.A. 3 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 6 | Access Prior Learning: In lesson 7-1, Grade 3, students learned about scaled picture graphs. In topic 4, Grade 3, students developed understanding of "half" as division by 2. <br> Developing the Big Idea: Students further develop their understanding of using picture graphs to represent data by finding that the key for a picture graph determines the number of pictures needed to represent the data. | Solve \& Share: <br> Consider posing the question from Look Back! while students share their solution methods and reasoning. <br> After students have shared solution methods and reasoning consider asking students if there is another scale that could have worked given the data (e.g., 5 because all of the balls are multiples of 5). <br> Convince Me: <br> Consider assigning the Convince Me! to provide students with the opportunity to reason with representing half quantities on a picture graph. <br> Independent Practice/Math Practices and Problem Solving: <br> Item 4 provides students the opportunity to practice reasoning with selecting an appropriate scale based on data. Consider also assigning item 7 to ensure students have sufficient opportunity to reason with selecting a scale based on a set of data and creating a picture graph. Watch to ensure that students have included all the elements of a picture graph: <br> - Title <br> - Category labels <br> - Key that includes the scale <br> - Accurately represent the data for each category <br> Assess and Differentiate: <br> If time permits, teach students how to play "Teamwork" (TE, p. 369A). All students should have the opportunity to play this game. <br> Child-watch to identify students who need additional support and pull them in a small group to do the Intervention Activity (TE, p. 369A). <br> Homework \& Practice: <br> Consider solving item 8 Common Core Assessment in class. This item is designated as an Advance item; therefore, it is not appropriate to assign as independent work for all students. However, this would work as a Solve \& Share for creating an additional lesson, if needed. <br> Consider saving item 2, to be completed independently in class, after lesson 7-3 as part of the formative assessment process to check students' reasoning with selecting an appropriate scale based on a set of data. |


| Lesson 7-3: Make Bar Graphs |  |  |
| :---: | :---: | :---: |
| $\begin{aligned} & \text { 3.MD.B. } 3 \\ & \text { 3.OA.A. } 3 \end{aligned}$ | Access Prior Learning: In lesson 7-1, Grade 3, students learned about scaled bar graphs. In topic 4, Grade 3, students developed understanding of "half" as division by 2 . | Math Anytime: <br> To ensure sufficient opportunity for students to practice reasoning with selecting an appropriate scale based on data consider assigning item 4 in the Common Core Review (TE, p. 365A). |
|  |  |  |
|  |  |  |
|  |  | Solve \& Share: |
| MP. 1 |  | Watch for and correct students that draw graphs with bars for different categories touching. For more information on this common error read the Instruction Note at the beginning of this topic. |
| MP. 2 |  |  |
| MP. 3 | Developing the Big Idea: Students further develop their understanding of using bar graphs to represent data by finding that the scale determines how long each bar needs to be to represent every number in a data set. | Look Back: |
| MP 4 |  | To support students' development of MP. 6 "Attend to precision," when constructing a bar graph |
| MP. 4 |  | consider assigning and discussing the Look Back!. |
| MP. 5 |  | Independent Practice/Math Practices and Problem Solving: |
| MP. 6 |  | Consider including item 6 to ensure students have sufficient opportunity to reason with selecting a scale based on a set of data and creating a bar graph. Watch to ensure that students have |
|  | to represent data by finding that the scale determines how long each bar needs to be to represent every number in a data set. | included all the elements of a bar graph: <br> - Title <br> - Category labels <br> - Scaled quantities <br> - Accurately represent the data for each category |
|  |  | Assess and Differentiate: <br> If time permits, you may consider replacing the Problem-Solving Reading Mat with the game "Teamwork" (TE p. 369A) or the Fluency Practice Activity (TE p. 389). |
|  |  | Based upon child-watching, identify students who need additional support and pull them in a small group to do the Intervention Activity (TE p. 375A). |
|  |  | Homework \& Practice: |
|  |  | Consider saving item 4, to complete independently in class, after lesson 7-4 as a formative assessment on students' reasoning with selecting an appropriate scale based on a set of data and creating a scaled bar graph. |
|  |  | *CTC: Solve \& Share (student work samples) |
| Lesson 7-4: Solve Word Problems Using Information in Graphs |  |  |
| $\begin{aligned} & \text { 3.MD.B. } 3 \\ & \text { 3.OA.A. } 3 \\ & \text { 3.OA.D. } 8 \end{aligned}$ | Access Prior Learning: <br> In previous grades, students have developed understanding of the operations addition and subtraction. In topics 1 through 5, | Solve \& Share: <br> Consider asking students what they have to find (e.g. the difference of how many students |
|  |  |  |
|  |  | prefer peanut butter more than cheese sandwiches and the difference of how many students prefer peanut butter more than tuna sandwiches) prior to letting students work on the problem. |
|  |  | Look Back: |
| MP. 1 | Grade 3, students have developed understanding of the operations | Consider discussing the Look Back! as it requires that students reason with key ideas when analyzing a scaled bar graph. |
|  | multiplication and division. In | Independent Practice/Math Practices and Problem Solving: |
| MP. 3 | previous lessons in this topic, students developed understanding | Notice that Quick Check items 9 and 12 flip the axis for the numbers and categories. Watch for |
| MP. 6 |  | and support students that struggle with this change. Consider discussing with the class how this |
| MP. 8 | of and created scaled picture and bar graphs. | change also changes the look of the scaled bar graph (e.g., the bars are horizontal now instead of vertical). |
|  | Developing the Big Idea: | Assess and Differentiate: |
|  | In this lesson, students further develop understanding of scaled | If time permits, you may consider replacing the Math and Science Activity with the game "Teamwork" (TE, p. 369A) or the Fluency Practice Activity (TE, p. 389) |
|  | picture and bar graphs by making, reading, and analyzing them to solve real-world problems using the 4 operations. | Child-watch to identify students who need additional support and pull them in a small group to do the Intervention Activity (TE, p. 381A). |
| Lesson 7-5: Math Practices and Problem Solving- Precision |  |  |
| $\begin{aligned} & \text { 3.MD.B. } 3 \\ & \text { 3.OA.A. } 3 \end{aligned}$ | Access Prior Learning: <br> Throughout this topic, students have used precise language and symbols when analyzing scaled picture and bar graphs to solve word problems. | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 6. Refer to the Math Practices and Problem Solving Handbook (TE, pp. 26A-26F, 29F) for suggestions on how to develop, connect and assess this Math Practice. Also, reference the handbook in the Student Edition (SE, p. 26F). <br> -continues on next page- |
|  |  |  |
|  |  |  |
| MP. 6 |  |  |
| MP. 1 |  |  |
| MP. 2 |  |  |


| MP. 4 | Securing the Big Idea: <br> In this lesson, students secure their <br> MP. 7 <br> understanding of making, reading, <br> and analyzing scaled picture and <br> bar graphs by focusing on <br> accuracy (MP.6). | Solve \& Share: <br>  <br> Share, you may want to restate that this includes using precise mathematical language. <br> Many students have a misconception that MP. 6 only refers to precise calculations. Consider <br> using the time where students are working on the Solve \& Share as an opportunity to child- <br> watch for behaviors associated with MP.6 that are listed in the Math Practices and Problem <br> Solving Handbook (TE, p. 26A). After discussing student solution methods and reasoning, have <br> students self-score for the behaviors associated with this math practice. <br> Look Back: <br> Consider discussing the Look Back! as the reasoning discussed here can then either be <br> confirmed, clarified, or corrected during the Visual Learning Animation. <br> Convince Me: <br> Consider assigning the Convince Me! as it offers another opportunity to work with MP. 6 and <br> assess for behaviors attributed to this math practice. |
| :--- | :--- | :--- |
|  | Assess and Differentiate: <br> If time permits, you may consider replacing the Problem-Solving Reading Mat with the game <br> "Teamwork" (TE, p. 369A) or the Fluency Practice Activity (TE, p. 389). <br> Child-watch to identify students who need additional support and pull them in a small group to <br> do the Intervention Activity (TE, p. 387A). |  |

## References

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## - 3rd Grade Topic 8: Use Strategies and Properties to Add and Subtract

Big Conceptual Idea: Numbers and Operations in Base Ten, K-5 (p. 12)
Prior to instruction, view the Topic 8 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 401A-401F), the Topic Planner (pp.401l-401K), all 9 lessons, and the Topic Assessments (pp. 469-470A).

| Mathematical | Topic Essential Question: |
| :--- | :--- |
| Background: | How can sums and differences be estimated and found |
| Read Topic 8 | mentally? |
| Cluster |  |
| Overview/Math | Reference Answering the Topic Essential Question (TE, pp. |
| Background (pp. | 465-466) for key elements of answers to the Essential |
| 401A-401F) | Question. |

The lesson map for this Topic is as follows:

| $8-1$ | $8-2$ | $8-3$ | $8-4$ | $8-5$ | $8-6$ | $8-7$ | $8-8$ | $8-9$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |



3 ${ }^{\text {rd }}$ Grade Curriculum
Pacing Framework:
Balanced Calendar

2 A/D/E days used strategically throughout the topic.

## Instructional note:

Topics 8,9 and 10 comprise a cluster on understanding place-value and the properties of operations to perform multi-digit operations. Topic 8 focuses on the properties of operations for addition: Commutative (Order) Property, Associative (Grouping) Property and Additive Identity Property of 0 (Zero). Note: The Additive Identity Property for $0(3+0=3)$ is different than The Multiplicative Identify Property for $1(3 \times 1=3)$ and unless explicitly discussed and compared may cause confusion for some children.

In this topic, students will use place value to estimate. Estimation strategies include rounding and using landmark and benchmark numbers to find "close to" sums and differences. Students often confuse rounding and estimating. The enVision glossary defines rounding as, "To replace a number with a number that tells about how much or how many to the nearest ten, hundred, thousand, and so on. Example: 42 rounded to the nearest 10 is 40 " (p. G7). The enVision glossary defines estimating as, "To give an approximate number or answer" (p. G3).

Rounding is one type of estimation. Other computational estimation strategies include front-end methods and compatible numbers (Van de Walle, Karp, \& Bay-Williams, 2016). To estimate the sum using rounding strategies $423+695$ may round to $400+700$. This estimate results in a sum of 1,100 . Some children may round to 420 and 690 resulting in an underestimate. Some may even choose a compatible number strategy such as mentally combining 410 with the 690 the "make another 100 " strategy. As long as students can justify their reasoning, accept 'close to' estimates.

Strategies for computational estimation should be chosen carefully. Rounding is not always the most accurate strategy for estimation because adding after rounding allows errors to accumulate. For example, I might estimate $444+649$ as $400+600=1,000$, despite the sum being closer to 1,100 . The purpose of these strategies is to get children in the "ballpark" or in a range for the answer so they can reason, make sense and reflect when working on problems.

Third graders are expected work with place values to 10,000. In second grade students, "Understand that the three digits of a threedigit number represent amounts of hundreds, tens, and ones..." (NVACS, 2010, 2.NBT.A.1), and "Read and write numbers to 1000 using base-ten numeral, number names, and expanded form" (NVACS, 2010, 2.NBT.A.3)". In fourth grade students, "Generalize place value understanding for multi-digit whole numbers" (NVACS, 2010, 4.NBT.A.). Note that, "Grade 4 expectations in this domain are limited to whole numbers less than or equal to $1,000,000^{\prime \prime}$ (NVACS, 2010, p. 29). This objective was added to bridge the gap from the $2^{\text {nd }}$ to the $4^{\text {th }}$ grade standards. Throughout this topic look for opportunities to review place value concepts from second grade and extend these to working with numbers up to ten-thousand. Consider altering numbers in problems to provide these opportunities. Lessons 8-3, 8-6, and 8-7 focus on using place value understanding to round and estimate.

## Focus Math Practice 4: Model with mathematics

Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs,
flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose (NVACS, 2010, p. 7).

To help students work towards security, encourage them to use multiple models and reflect on whether the results make sense. Problem solving lesson $8-9$ is designed to reinforce this mathematical practice. See also the following resource: Reference Teacher's Edition (TE, pp. F24 - F24A).

## Potential Misconception(s)

Students might confuse the addition and multiplication properties of operations for addition. For example, the Additive Identity Property of Zero ( $5+0=5, a+0=a$ ) and the Multiplicative Identity Property of One ( $5 \times 1=5$ or $a \times 1=a$ ) are easily confused for

|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 9 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 1 | 1 | 6 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 2 | 2 | 3 | 7 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| 3 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 4 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| 5 | 5 | 6 | 7 | 8 | 9 | 7 | 11 | 12 | 13 | 14 |
| 6 | 6 | 7 | 8 | 9 | 10 | 11 | 1 | 13 | 14 | 15 |
| 7 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 15 | 15 | 16 |
| 8 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 76 | 17 |
| 9 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 12 |

students with limited conceptual understanding. See the Properties of Operations Table for additional information (NVACS, 2010, p. 90).

Students will benefit from testing these properties to build conceptual understanding. Is this rule always true? Can you find an exception to the rule? Consider creating a class developed anchor chart to collect examples of these properties.

For students struggling to understand the Commutative Property of Addition, consider extending lesson 8-2. Include work with the patterns in the addition table by using the table to show the symmetrical nature of the table. The included image is from the book Uncomplicating Algebra (Small, 2014) and shows the symmetry along the diagonal for 4 $+3=7$ and $3+4=7$, as well as, $3+7=10$ and $7+3=10$ (Commutative Property).

## Looking Ahead:

On the Topic Performance Assessment, students will round numbers, estimate and justify their solutions to equations, and demonstrate a pattern on the addition table based on a context. Facilitate the development of problem solving thinking habits. Provide opportunities for problem solving prior to working on the Topic Performance Assessment. When grading student work, accept responses that are mathematically reasonable even if they are not suggested in the Teacher's Edition.

## Meaningful Fluency Practice \& Assessment:

The following game can help students develop the mental math strategies that will support attaining NVACS standard 3.NBT.A.2, "Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction" (NVACS, 2010, p. 24). Consider rotating days so that students still have the opportunity to engage in meaningful practice of multiplication facts. There is a Pre/Post Addition/Subtraction Assessment available on the C \&l, K5 Mathematics website in resources for Academic Parent-Teacher Teams (APTT).

## Rolling for 500: Estimation

See the directions for this game at the end of this document.

| Essential Academic Vocabulary <br> Use these words consistently during instruction. |  |
| :--- | :--- |
| New Academic Vocabulary: <br> (First time explicity taught) | Review Academic Vocabulary: <br> (Vocabulary explicitly taught in prior grades or topics) |
| Associative (Grouping) Property of Addition | round |
| Commutative (Order) Property of Addition | place value |
| Identity (Zero) Property of Addition | inverse operations <br> Compatible numbers |
|  | multiples |
|  | difference |
|  | sum |
|  | equation |

Additional terminology that students may need support with: about, mental math, generalize, related

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding questions: "Are students developing conceptual understanding of the properties of addition in order to solve addition problems?"
"Are student estimating whole numbers based on reasoning?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $8-2$ | Math Practices and Problem Solving <br> (student work samples) <br> Item 23 | Focus CTC around the big idea: <br> $\bullet \quad$ student strategies and models. <br> student use of reasoning to analyze the relationship between <br> addition and subtraction. <br> student use part/part/whole understanding when subtracting or <br> adding. |
| $8-3$ | Quick Check (digital platform) <br> Items 1, 4, and 5 | Focus CTC around data analysis and collection of student workspace <br> (scratch paper). Printable version available under "Teacher Resources". <br> $\bullet \quad$ rounding whole numbers based on reasonableness. |


| Learning Cycle | Topic Assessments <br> SE pp. 465-470 | Use Scoring Guide TE pp. 465-470A |
| :---: | :--- | :--- |
| Assessments (summative) |  |  |

Standards listed in bold indicate a focus of the lesson

| NVACS <br> (Content and Practices) | Mathematical Development of the Big Idea | Instructional Clarifications \& Considerations |
| :---: | :---: | :---: |
| Lesson 8-1: Addition Properties |  |  |
| 3.NBT.A. 2 <br> MP. 1 <br> MP. 3 <br> MP. 4 <br> MP. 7 <br> MP. 8 | Access Prior Learning: <br> In Grade 2 students learned to add within 1,000 using models or strategies. <br> Securing the Big Idea: <br> Students are securing understanding of addition as problems that involve joining, partpart whole, or comparing. Students are also securing understanding of the Associative, Commutative, and Identity Properties of Addition. | Topic Opener: <br> Introduce the Topic Essential Question, "How can sums and differences be estimated and found mentally?" (TE, p. 401). Consider making this an anchor chart in your classroom and allowing students to add strategies to the chart throughout the topic. <br> You might also consider having students complete the Review What You Know prior to beginning instruction on Topic 8 so that you can respond to student instructional needs using the Item Analysis for Diagnosis and Intervention prior to beginning the topic (TE, p. 402-404). <br> Consider introducing vocabulary as students encounter terminology in the lessons rather than introducing all terms at the beginning of the lesson. Add vocabulary to math word wall if possible. <br> Solve \& Share: <br> Watch for students that are able to identify that there are the same number of buttons on both sides without having to compute. Pose questions to these students to evaluate if they have an understanding of the Commutative Property of Addition. <br> Watch for students that try to multiply the 3 addends. Facilitate discussion to identify that this is not a multiplicative situation. Is this repeated addition? Are we skip counting? <br> After students share their solution methods and reasoning, consider asking students why this is an addition situation and not a multiplication situation (e.g. we are not joining equal groups to find a total). Consider discussing the Look Back! prompt so that the Visual Learning Animation can be used to confirm, clarify or correct student understanding. <br> Visual Learning: <br> After the Identity (Zero) Property of Addition has been introduced, consider comparing and contrasting the Additive Identity Property of 0 (Zero) and the Multiplicative Identity Property of 1 (versus the Multiplicative Zero Property), in order to confront common misconceptions regarding the properties. For more information on the differences read the Instructional note at the beginning of this topic. <br> Consider discussing the Convince Me! to support students' development of MP. 4 "Model with math." <br> Assess and Differentiate: <br> If time permits, teach students how to play the game Tic Tac Toe (TE, p. 409A). All students should have the opportunity to play this game. <br> -continues on next page- |


|  |  | Consider the Intervention Activity for students who need additional support with the Commutative and Associative Properties (TE, p. 409A). |
| :---: | :---: | :---: |
| Lesson 8-2: Algebra-Addition Patterns |  |  |
| 3.OA.CD. 9 MP. 7 MP. 8 | Access Prior Learning: <br> In Grade 2, students used the addition table to identify patterns in addition facts and work with even and odd numbers. In Grade 3, Topic 4, students explored patterns with even and odd numbers using a multiplication table. <br> Securing the Big Idea: <br> Students are securing their understanding of patterns in the addition table with even and odd numbers and properties of addition. | Solve \& Share: <br> In lesson 5-2, students compared and contrasted the addition and multiplication tables. Students have the opportunity to connect these ideas to foundations of mathematical argumentation, justification and proof. <br> The Solve \& Share enables students to play with numbers and identify patterns and rules that are not immediately apparent. This helps children understand what mathematics truly is and what it involves. <br> Visual Learning: <br> Consider having students use colored tiles to build the patterns during the video (01:27). <br> If after viewing the Visual Learning Animation students still seem unsure about patterns for even and odd numbers with addition, consider viewing the Another Look! video. <br> Independent Practice/Math Practices and Problem Solving: <br> Quick Check item 3 asks students to recognize that the shaded numbers illustrate the Commutative Property of Addition. For more information on using the addition table to illustrate the addition properties read the Instructional note at the beginning of this topic. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Problem-Solving Reading Mat with the game Tic Tac Toe (TE, p. 409A) or the Fluency Practice Activity (TE, p. 459). <br> Consider the Intervention Activity for students who need additional support with exploring the patterns when adding two even numbers, two odd numbers or an even and an odd number (TE, p. 415A). |
| Lesson 8-3: Round Whole Numbers |  |  |
| 3.NBT.A. 1 MP. 1 MP. 3 MP. 6 | Access Prior Learning: <br> In Grade 2, Topic 9, students learned how to compare 3-digit numbers using place value and a number line. <br> Developing the Big Idea: <br> Students develop understanding of place value to 10,000 and use place value to round using the language of "about" to signify approximation. | Possible 2-day lesson to review place value to the 1,000 and introduce to the 10,000. The Instructional note at the beginning of this topic describes the importance of these lessons. <br> Day 1 : <br> Solve \& Share: <br> Consider building a class anchor chart to collect various strategies for finding approximations or 'close to' numbers. <br> Students who struggle with place value understanding might benefit from the number line model. <br> Convince Me: <br> Consider assigning and discussing the Convince Me! to provide students the opportunity to reason with reasonable numbers based off of place value clues. <br> After Convince Me! consider introducing place-value to the ten-thousands place by posting the place values and asking students what patterns they notice (e.g. the "ones" and "tens" from the one's period repeats into the thousands period). <br> Pose numbers to have students practice rounding to the 1,000 and 10,000 place values. Ensure that students are justifying their rounding decisions rather than following a rule without understanding. <br> Day 2 : <br> Solve \& Share: <br> Consider revisiting the original Solve \& Share and ask students to solve again, with 1,728 stickers. <br> Visual Learning: <br> Consider watching the Another Look! video in place of the Visual Learning Animation and as a class round using the numbers 4,896 (e.g. rounding to hundreds is 4,900 , round to thousands is 5,000 ) and 9,982 (e.g. rounding to hundreds is 10,000 rounding to thousands is 10,000 ). <br> Strengthen students' number sense by discussing why when rounding 9,982 to both the hundreds and thousands place we end up 10,000. Consider providing time for students to use dice to roll 4 digit numbers, with a partner, that they practice rounding to both the hundred's and thousand's place values. |


|  |  | This is a good opportunity to discuss various ways to estimate, including rounding, front-end and compatible numbers. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Math and Science Activity with the game Tic Tac Toe (TE, p. 409A) or the Fluency Practice Activity (TE, p. 459). <br> Consider the Intervention Activity for students who need additional support with using a number line as a tool to round to 10 (TE, p. 421A). |
| :---: | :---: | :---: |
| Lesson 8-4: Mental Math-Addition |  |  |
| 3.NBT.A. 2 <br> MP. 1 <br> MP. 3 <br> MP. 4 <br> MP. 5 <br> MP. 6 <br> MP. 7 | Access Prior Learning: <br> In Grade 2, students learned to decompose and then recomposing numbers into 'friendly numbers' as a strategy for simplifying an addition problem and finding the solution mentally. <br> Developing the Big Idea: <br> Students further develop an understanding that there is more than one strategy for working with mental math, including using place value understandings. | Solve \& Share: <br> To encourage students to use mental math strategies, consider removing writing tools, instead, have students describe their solution strategy while their partner represents this thinking in their book, a whiteboard or in math journals. <br> As students share their strategies and reasoning, consider charting the different mental math strategies students create. Highlight a few strategies that are the most efficient given the numbers in the problem. <br> Visual Learning: <br> If the strategies in the Visual Learning Animation are not already on the chart created, add these mental math methods to the poster. If they are already there, explicitly connect those in the Visual Learning Animation to the student's strategy. Ask students, "How using friendly numbers (multiplies of 10), makes solving problems easier?" <br> Consider assigning the Convince Me! to give students the opportunity to practice the methods introduced in the Visual Learning Animation and support students' development of MP. 4, Model with Mathematics. <br> Assess and Differentiate: <br> If time permits, teach students how to play "Clip and Cover" (TE, p. 427A). All students should have the opportunity to play this game. <br> Consider the Intervention Activity for students who need additional support with using place value parts to add (TE, p. 427A). Connect this work to students using expanded notation to connect partial sums. |
| Lesson 8-5: Mental Math-Subtraction |  |  |
| 3.NBT.A. 2 <br> MP. 1 <br> MP. 3 <br> MP. 4 <br> MP. 7 <br> MP. 8 | Access Prior Learning: <br> In $2^{\text {nd }}$ grade students worked with compensation as a strategy. In the previous lesson, students developed understanding of mental math strategies for addition with decomposition and compensation. <br> Developing the Big Idea: Students further develop an understanding that there is more than one way to do mental math including compensation with subtraction. | Instructional Note: <br> To help students understand how compensation works with subtraction, consider investigating constant difference using the number line model. For example, the difference between two individuals' birth years will be the same as the difference between these two individuals' ages. Also, the "hop" on a number line can be slid up or down a number line to a benchmark number. <br> Solve \& Share: <br> To encourage students to use mental math strategies, consider removing writing tools, instead, students to describe their solution strategy while their partner represents this thinking in their book, mathematics journal or on a whiteboard. <br> As students share their strategies and reasoning, consider making a poster of the different mental math strategies students use. <br> Visual Learning: <br> Add the mental math methods introduced in the Visual Learning Animation to the poster of mental math strategies. Ask students, "How does using place value to solve subtraction problems make mental math easier?" <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Problem Solving Reading Mat with the game Tic Tac Toe (TE, p. 409A), Clip and Cover (TE, p. 427A), or the Fluency Practice Activity (TE, p. 459). <br> Instead of using the Intervention Activity for students whom need additional support, work with the idea of 'constant difference' and modeling this first on a number line and later applying this idea to compensation. |


| Lesson 8-6: Estimate Sums |  |  |
| :---: | :---: | :---: |
| 3.NBT.A. 2 MP. 2 MP. 3 MP. 4 MP. 6 | Access Prior Learning: <br> In 2 ${ }^{\text {nd }}$ grade, students worked with compatible numbers. In previous lessons in this topic, students have worked with rounding numbers and developed mental math strategies for addition. <br> Developing the Big Idea: <br> This lesson develops students' understanding of the purpose of estimation and strategies for estimating with addition using compatible numbers. | Solve \& Share: <br> After the Solve \& Share ask students what estimation strategies they used (e.g. rounding is one strategy for estimation). Ask, "How does estimating sums help us?" <br> Watch for students that solve for an exact number and support by asking the Ask Guiding Questions as Needed (TE, p. 435) prompts. Consider providing number lines to support conceptual understanding (Teaching Tool 7). Have students share their reasoning with the class. Students benefit from both successful strategies and the discussion of common misconceptions. <br> Convince Me: <br> Consider having students partner talk the Convince Me!. Discuss as a whole group as this supports students development of using number sense to estimate. <br> Assess and Differentiate: <br> If time permits, teach students how to play Clip and $\operatorname{Cover}$ (TE, p. 439A). All students should have the opportunity to play this game. <br> Consider the Intervention Activity for students who need additional support with using estimation strategies such as rounding or compatible numbers (TE, p. 439A). |
| Lesson 8-7: Estimate Differences |  |  |
| 3.NBT.A. 2 <br> MP. 1 <br> MP. 2 <br> MP. 4 <br> MP. 8 | Access Prior Learning: In previous lessons in this topic, students have worked with rounding numbers and developed mental math strategies for subtraction. <br> Developing the Big Idea: <br> This lesson develops students' understanding of the purpose of estimation and strategies for estimating with subtraction. | Solve \& Share: <br> Watch for students that solve for an exact number and support by asking the Ask Guiding Questions as Needed (TE, p. 441) prompts. Consider also supporting students struggling to estimate by providing them with number lines (Teaching Tool 7). <br> Consider discussing the Look Back! prompt to support students' development of estimation strategies. <br> Visual Learning: <br> After viewing the Visual Learning Animation, consider asking students if there is another way to estimate the difference. This is an opportunity to build understanding that there are multiple ways to estimate (e.g. rounding, front-end, compatible numbers). Students might round 493 to the hundreds place because it is so close to 500 , while they could round 126 to the nearest tens place. Rounding the numbers to different place values to make an easier estimate applies to Quick Check item 22. <br> Independent Practice/Math Practices and Problem Solving: <br> Quick Check item 22 aligns to Visual Learning Animation. An emphasis of this lesson has been on estimates giving different answers. Therefore, remember to accept student work that is mathematically reasonable. <br> Assess and Differentiate: <br> If time permits, teach students how to play Teamwork (TE, p. 445A). All students should have the opportunity to play this game. <br> Consider the Intervention Activity for students who need additional support with estimating differences using rounding (TE, p. 455A). |
| Lesson 8-8: Relate Addition and Subtraction |  |  |
| 3.NBT.A. 2 MP. 2 MP. 3 MP. 4 | Access Prior Learning: <br> In Grade 2, students developed understanding of addition and subtraction as inverse operations. <br> In previous lessons, students have solved addition and subtraction problems using mental math and estimation strategies. In Topic 4, students learned about the inverse relationship between multiplication and division. <br> Developing the Big Idea: <br> This lesson develops the understanding of addition and subtraction as inverse operations. | Solve \& Share: <br> Watch for students who select numbers and operations without reasoning. For these students return to the context of the problem, focus on understanding the question and developing a problem solving plan, rather than focusing on a solution and consider replacing the numbers with the word "some" to help the students understand the context. <br> Ask students that finish first, how they could prove their solutions are correct. Consider having students that are able to successfully check share their strategy so that as a class you can discuss why we can check a subtraction problem with addition (e.g. their inverse relationship). <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 10 for distributed practice of telling time using an analog clock. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Problem Solving Reading Mat with the game Tic Tac Toe (TE, p. 409A), Clip and Cover (TE, p. 427A; 439A), Teamwork (TE, p. 445A), or the Fluency Practice Activity (TE, p. 459). <br> Consider the Intervention Activity for students who need additional practice using the inverse operation to check answers (TE, p.277A). |


| Lesson 8-9: Math Practices and Problem Solving- Model with Math |  |  |
| :---: | :---: | :---: |
| 3.NBT.A. 2 <br> MP. 4 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 5 | Access Prior Learning: <br> In Topic 2 students focused on MP. 4 to solve multi-step problems. Throughout Topic 8 students have modeled the math with number lines, bar diagrams, and equations. <br> Developing the Big Idea: In this lesson, students further develop their understanding of MP. 4 "Model with Mathematics" by using bar diagrams and equations to represent problems that are more complex. | This lesson provides an opportunity to focus on the thinking habits and display the behaviors associated with Math Practice 4, "Model with math." Refer to the Math Practices and Problem Solving Handbook (TE, p. F24-F24A, F29) for suggestions on how to develop, connect and assess this Math Practice. Also, reference the handbook in the Student Edition (SE, p. F24). <br> Solve \& Share: <br> Consider reintroducing MP. 4 (SE p. F24) before introducing the Solve \& Share. After introducing, the Solve \& Share identify what the problem is asking (e.g., how many total minnows are in the pond?). Consider asking how this problem is similar to the last Solve \& Share (e.g. comparing quantities). Consider then asking students how they could model this problem (e.g. bar diagrams, number line, equations). <br> You might also consider using the time where students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP. 4 that are listed in the Math Practices and Problem Solving Handbook (TE p. 24A). After discussing student solution methods and reasoning, have students self-score for the behaviors associated with this math practice. <br> Convince Me: <br> Consider assigning the Convince Me! as it provides an opportunity for students to reason when it is appropriate to use a bar diagram. <br> Assess and Differentiate: <br> If time permits, teach students how to play Teamwork (TE, p. 457A) as this relates the mathematics developed in this topic to a real world context. <br> Consider the Intervention Activity for students who need additional support with adding using a bar diagram (TE, p. 457A). |

## References

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## Rolling for 500 <br> Mathematical Understanding: <br> Students strengthen numerical fluency through practice with strategies used for addition and subtraction. <br> Grade Level: 3-5 <br> Number of Players: 2-4 <br> Materials Needed: <br> - a die <br> - a game piece for each player <br> - game board

## Object of the Game:

The first player to reach or cross the Finish wins the game.

## Directions:

Each player places their marker on the Start square of the shared game board.

Player 1 rolls the die. Match the number rolled to the table on the game board to determine how many spaces to move forward or backward. Player 1 moves their marker.

Players take turns rolling the die and using the table to determine spaces moved.

The first player to reach or cross the Finish line wins the game.

Players cannot move below zero and wait at the start space for a positive roll.
Two players can be on the same space on the gameboard at the same time.

## Optional:

When playing the estimation version, players can state out loud what their exact space would be and how close they are to the space they move onto to. Which space is the closest and why?
Guiding Questions:
What do you know?
Where do you think you will begin?
Where are you stuck? What is confusing? What are you wondering about?
What are you going to try?
What did you think about to come to your answer?

## Differentiation:

Two versions of the game can be used for grades 3-5. Rolling for 500 gives practice with place value strategies to add and subtract numbers up to 500 . Rolling for 500 estimation gives practice with place value strategies for addition and subtraction and also requires comparative reasoning in order to properly place the gameboard marker.
Game Trajectory:
Pre K-K: Counting along a number line to 20
K-2: Addition and subtraction to get to 50

Clean up Checklist for Game Bag: Die
Game piece markers
Game boards

3-5: Rolling for 500 or Rolling for 500 estimation version
5-6: Rolling for 5


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## - Grade 3 Topic 9: Fluently Add and Subtract Within 1,000

Big Conceptual Idea: Numbers and Operations in Base Ten (p. 12)
Prior to instruction, view the Topic 9 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 401A-401F), the Topic Planner (pp.47IA-471C), all 8 lessons, and the Topic Assessments (pp. 533-534A).

| Mathematical | Topic Essential Question: |
| :--- | :--- |
| Background: | What are standard procedures for adding and subtracting |
| Read Topic 9 Cluster | whole numbers? |
| Overview/Math | Reference Answering the Topic Essential Question (TE, pp. 529-530) for key |
| Background (pp. | elements of answers to the Essential Question. |
| 401A-401F) |  |

The lesson map for this topic is as follows:

| $9-1$ | $9-2$ | $9-3$ | $9-4$ | $9-5$ | $9-6$ | $9-7$ | $9-8$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

4 A/D/E days used strategically throughout the topic.


## Instructional note:

As previously stated, this topic is part of a cluster that includes topics 8 and 10. These topics focus on using place-value understanding and properties of operations to perform multi-digit arithmetic. A big idea specific to topic 9 is the use of strategies and algorithms based on place-value understanding for solving multi-digit addition and subtraction problems within 1,000 (3.NBT.A.2). This understanding builds on the work done in second grade with standard 2.NBT.B. 7 that states, "Add and subtract within 1,000 , using concrete models or drawing and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtracting three-digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds" (p.19).

The phrase "relate the strategy to a written method" is bolded to point out that third graders should have had experiences with using a strategy to add and subtract within 1,000 and relating that to a written method. Fuson and Beckmann (2012) explain a trajectory from strategies, to written method, to standard algorithm (the full article can be accessed in the references section at the end of this document). See figures below (p. 19 and 21).

FIGURE 2: Multidigit Addition Methods that Decompose into Base Ten Units



These ideas relate to topic 9 as students move through various models and strategies towards a standard algorithm.
For example, in the problem $175+366$ students might say, "I carried the 1 ten in 11 to the tens place to add with the other tens. Then I added $10+70+60$ to make 140 so I wrote the 4 under the tens place and carried the 1 hundred to the hundreds place..."

Students might also explain that when adding the 1 (10), 7 (70), and 6 (60) in the tens place they had 14 tens and since 10 tens is 100 they carried a 1 to be added with the rest of the hundreds.

The essential question for this topic is, "What are standard procedures for adding and subtracting whole numbers?" This connects to the learning trajectory for the topic which focuses on connecting partial sums and differences to the expanded algorithm and then to a standard algorithm. In $4^{\text {th }}$ grade, students are expected to demonstrate security with a standard algorithm. The goal of this unit is to secure the language of regrouping and the concepts of partial sums and differences.

## Focus Math Practice 3: Construct viable arguments and critique the reasoning of others

The standard states, "They (students) make conjectures and build a logical progression of statements to explore the truth of their conjectures.... Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and -if there is a flaw in and argument- explain what it is" (NVACS, 2010, p. 6-7).

To help students work towards security, consider introducing a routine that when students are done working on the Solve \& Share they explain their reasoning to themselves to "convince yourself." After practicing, students could share their reasoning and conjectures with a classmate to "convince a friend." Finally, they share their reasoning with somebody that disagrees with their conjecture to "Convince a critic." Consider also requiring that if students feel there is flawed reasoning they must be able to explain the flaw or when a student revises their own thinking they must be able to explain why they have changed their conjecture. Behaviors associated with MP. 3 are described in the Teacher's Edition (pp. F23-F23A) and the NVACS.

## Meaningful Fluency Practice \& Assessment:

The following games can help students develop strategies that will support attaining NVACS standard 3.NBT.A.2, "Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction (NVACS, 2010, p. 24)." Consider rotating days so that students still have the opportunity to engage in meaningful practice of multiplication facts. There is a Pre/Post Addition/Subtraction Assessment available on the C \& I, K-5 Mathematics website in resources for Academic Parent-Teacher Teams (APTT).

## Rolling for 500

Directions: See below in this document for the directions and game board.

## Close Call: Addition Version

Directions: Remove 10s and face cards from the deck. Shuffle the deck and deal each player 8 cards. Each player selects six of their cards and creates two 3 -digit numbers from them. The goal is to create two numbers that have a sum as close to 1000 as possible, without going over. After players have made their selections, they place their cards face up in front of them, arranging them so other players can see which two numbers they have created. The player with the sum closest to 1000, without going over, wins a point. In the case of a tie, a point is awarded to each team. Shuffle the cards before dealing another round. Play continues for 5 rounds. The player with the most points after the last round wins the game.
For example, a student draws $7,4,5,6,8,2,1,1$ and chooses to use the cards $7,4,5,6,8,1$, creating the problem 754 $+186=940$. Just so long as another player does not get a number closer to 1000 without going over then this student earns 1 point for this round.

## Close Call: Subtraction Version

Directions: Remove 10s and face cards from the deck. Shuffle the deck and deal each player 8 cards. Each player selects five or six of their cards and creates two 3-digit numbers or a 2-digit number that's subtracted from a 3-digit number from the dealt cards. The goal is to create two numbers that have a difference as close to 10 as possible, without going lower. After players have made their selections, they place their cards face up in front of them, arranging them so other players can see which two numbers they have created. The player with the numbers closest to 10 , without going lower, wins a point. In the case of a tie, a point is awarded to each team. Shuffle the cards before dealing another round. Play continues for 5 rounds. The player with the most points after the last round wins the game. For example, a student draws 7, 4, 5, 6, 8, 2, 1, 1 and chooses to use the cards $7,4,5,6,8,1$, creating the problem $821-765=56$. Just so long as another player doesn't get a difference closer to 10 without going lower then this student earns 1 point for this round.

## Essential Academic Vocabulary

Use these words consistently during instruction.

| New Academic Vocabulary: <br> (First time explicity taught) | Review Academic Vocabulary: <br> (Vocabulary explicity taught in prior grades or topics) |
| :--- | :--- |
| conjecture | regroup |
|  | compatible numbers |
|  | Associative Property of Addition |
|  | Commutative Property of Addition |
|  | inverse operation |
|  | expanded form |

Additional terminology that students may need support with: more, fewer, less
*Collaborative Team Conversations (CTC)
Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding question: "Are students applying place value understanding to add and subtract whole numbers?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $9-1$ | Quick Check (digital platform) <br> Items 1, 3, and 4 | Focus CTC around data analysis and collection of student workspace <br> (scratch paper). Printable version available under "Teacher Resources". <br> $\bullet \quad$ understanding place value to break apart (decompose) numbers. |
| $9-5$ | Math Practices and Problem Solving <br> (student work samples) <br> Item 16 | Focus CTC around the big idea: <br> $\bullet$ student strategies and models. <br> $\bullet$ students understanding place value to break apart numbers. <br> $\bullet \quad$ students using partial differences. |


| Learning Cycle <br> Assessments (summative) | Topic Assessments <br> SE pp. 529-534 | Use Scoring Guide TE pp. 529-534A |
| :---: | :--- | :--- |

Standards listed in bold indicate a focus of the lesson.


|  |  | Look Back: <br> Consider discussing the Look Back! prompt to continue to support students' understanding of estimation and identify the connections in mathematical ideas. <br> Visual Learning: <br> The Visual Learning Animation only shows the U.S. Traditional Algorithm as a solution method. Research has shown that once students have been taught a standard algorithm, they are unlikely to go back to using invented algorithms and reasoning strategies. <br> If students are insecure in their place value understanding, consider not showing the Visual Learning Animation and instead run item 19 from Math Practices and Problem Solving as another Solve \& Share to give more opportunity to work with invented algorithms and connect them to place value understanding. <br> Convince Me: <br> If you do show the Visual Learning Animation, consider assigning and discussing the Convince Me! to support students' development of understanding the math behind procedures such as the U.S. Traditional Algorithm. <br> Independent Practice/Math Practices and Problem Solving: <br> Quick Check item 22 Higher Order Thinking may be more difficult for students because so far this year students have mostly worked with Add to-Result Unknown problem types (for more information on problem types see p. 88 of NVACS). Item 22 is a "Compare-Bigger Unknown" problem type. <br> Assess and Differentiate: <br> If time permits, teach students how to play the game "Clip and Cover" (TE, p. 485A). All students should have the opportunity to play this game. <br> Child watch to identify students who need additional support and consider the included Intervention Activity (TE, p. 485A). |
| :---: | :---: | :---: |
| Lesson 9-3: Continue to Add 3-Digit Numbers |  |  |
| 3.NBT.A. 2 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 6 <br> MP. 7 <br> MP. 8 | Access Prior Learning: <br> In the previous lesson, students learned to add 3-digit numbers using the U.S. Traditional Algorithm and place value understanding. <br> Developing the Big Idea: Students further develop the understanding of the U.S. Traditional Algorithm as a shortcut for the expanded algorithm by connecting it to place value understanding. | Instructional note: <br> Many problems in this lesson are the compare problem type, which can be difficult for learners still building an understanding of addition. Watch for students that seem to be struggling due to the comparative terminology and provide vocabulary support for the terms as well as questioning to push students to think about what is known and unknown. Ask them to connect back to the situation given and the relationship between these terms. Focus on making sense of problems and relationships helps students develop problem-solving habits. <br> Solve \& Share: <br> Prior to introducing the Solve \& Share, consider asking students to share out all the strategies they can think of for adding multi-digit numbers and posting these ideas to the anchor chart. Keep in mind that the outcome of this topic is not that students are fluent with the U.S. Traditional Algorithm, but rather that they are secure with the place value understandings to add multi-digit numbers. Therefore, it is acceptable for students to be using strategies based on place value understanding such as the expanded or partial sums algorithms to solve multi-digit addition problems. <br> Visual Learning: <br> The Visual Learning Animation only shows the U.S. Traditional Algorithm as a solution method. Consider pausing frequently to connect the computation used in the U.S. Traditional Algorithm to partial sums. Include modeling with using base-10 blocks if needed. You might also consider not showing the Visual Learning Animation, but still ask students to share their invented algorithms, or partial sums, and explain using place value understanding. <br> Assess and Differentiate: <br> If time permits, teach students how to play the game "Teamwork" (TE, p. 491A). All students should have the opportunity to play this game. <br> Child watch to identify students who need additional support and consider the included Intervention Activity (TE, p. 485A and/or TE, p. 491A). |


| Lesson 9-4 | 3 or More Numbers |  |
| :---: | :---: | :---: |
| 3.NBT.A. 2 <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 8 | Access Prior Learning: <br> In the previous lesson students learned to add two, 3-digit numbers using a standard algorithm, like the U.S. Traditional Algorithm. <br> Developing the Big Idea: <br> Students further develop an understanding of the U.S. <br> Traditional Algorithm as a shortcut for the expanded algorithm by connecting it to place value understanding with 3 multi-digit numbers. | Solve \& Share: <br> After introducing the Solve \& Share, consider asking students to make sense of the problem, identify what the problem is asking and develop a plan. To continue to support students' understanding of additive versus multiplication situations consider also asking students why this is not a multiplication problem (e.g. we do not have repeated equal sized groups of fish). <br> Visual Learning: <br> The Visual Learning Animation only shows the U.S. Traditional Algorithm as a solution method. Consider pausing frequently to connect the computation of the U.S. Traditional Algorithm to partial sums. Include modeling with using base-10 blocks if needed. You might also consider not showing the Visual Learning Animation, but still have students solve and share their invented algorithms, or partial sums, with place value understanding. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider using item 18 as it has students use information from a picture to find the total height. <br> Assess and Differentiate: <br> If time permits, teach students how to play "Display the Digits" (TE, p. 497A). All students should have the opportunity to play this game. <br> Child watch to identify students who need additional support and consider the included Intervention Activity (TE, p. 497A). |
| Lesson 9-5: Use Partial Differences to Subtract |  |  |
| 3.NBT.A. 2 MP. 3 MP. 6 MP. 7 MP. 8 | Access Prior Learning: <br> In topics 4 \& 6, Grade 2 students developed fluency with adding and subtracting 2-digit numbers. In topics 10 \& 11, Grade 2 students began to develop understanding for adding and subtracting 3-digit numbers using models such as place value blocks and number lines. In topic 8, students revisited the properties of addition, compensation with subtraction, and using the number line to model addition and subtraction. <br> Developing the Big Idea: <br> Students are further developing their understanding of using place value strategies to subtract 3-digit numbers by using the expanded algorithm to break the subtraction problems into a series of easier problems based on place value. | Solve \& Share: <br> Consider having a place value chart (Teaching Tool 5 ) and base-10 blocks available, especially for students that are struggling to connect regrouping in addition to place value understanding. <br> Watch for students that attempt or do use the U.S. Traditional Algorithm. For these students ask questions to determine if the student has conceptual understanding or if they are using a memorized procedure. Are they applying place value understanding to use a partial differences strategy? Are they making simpler problems and showing flexibility and efficiency in their thinking? Encourage all students to show or explain their reasoning and to connect these ideas to a written strategy. <br> For an example of how concrete modeling can be connected to a representational strategy, see Analyze Student Work in Lesson 9-6 (TE, p. 505); "Ira's Work". <br> Visual Learning: <br> The Visual Learning Animation only shows the U.S. Traditional Algorithm as a solution method, research states that once students have been taught a standard algorithm they are unlikely to go back to using invented algorithms. Consider pausing frequently to connect the computation with the U.S. Traditional Algorithm to the expanded algorithm and partial differences; include using base-10 blocks if needed. <br> You might also consider not showing the Visual Learning Animation and instead ask students to share their strategies and reasoning for solving. Are students applying addition strategies to help them subtract? Are there similarities in the use of place value between strategies that students can notice and use to make a generalization about place value and subtraction? <br> Convince Me: <br> Consider assigning and discussing the Convince Me! to support students' development of using place value understanding to subtract multi-digit numbers. <br> Independent Practice/Math Practices and Problem Solving: <br> Item 15 Higher Order Thinking of the Quick Check is a "compare" problem, which may present an extra challenge. Students have been working mostly with "Take from-Result Unknown" problems in this lesson (for more on the problem types see page 88 of the NVACS). Focus on helping students make sense of what problems are asking and developing a plan. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Problem Solving Reading Mat with the game "Clip and Cover" (TE, p. 485A), "Teamwork" (TE, p. 491A), "Display the Digits" (TE, p. 497A), or the Fluency Practice Activity (TE, p. 523). <br> Child watch to identify students who need additional support and consider the included Intervention Activity (TE, p. 503A). <br> *CTC: Math Practices and Problem Solving (student work samples) |



|  |  | Independent Practice/Math Practices and Problem Solving: <br> Quick Check item 19 requires students to reason with a multi-step compare problem type. <br> Consider asking students what the hidden questions are in order to solve this problem. <br> Assess and Differentiate: <br> If time permits, teach students how to play "Display the Digits" (TE, p. 515A). All students <br> should have the opportunity to play this game. <br> Child watch to identify students who need additional support and consider the included <br> Intervention Activity (TE, p. 515A). |
| :--- | :--- | :--- |
| Sesson 9-8: Math Practices and Problem Solving- Construct Arguments |  |  |

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## Rolling for 500

## Mathematical Understanding:

Students strengthen numerical fluency through practice with strategies used for addition and subtraction.

## Grade Level: 3-5

Number of Players: 2-4
Materials Needed:

- a die
- a game piece for each player
- game board


## Object of the Game:

The first player to reach or cross the Finish wins the game.

## Directions:

Each player places their marker on the Start square of the shared game board.
Player 1 rolls the die. Match the number rolled to the table on the game board to determine how many spaces to move forward or backward. Player 1 moves their marker.

Players take turns rolling the die and using the table to determine spaces moved.
The first player to reach or cross the Finish line wins the game.
Players cannot move below zero and wait at the start space for a positive roll.
Two players can be on the same space on the game board at the same time.

## Optional:

When playing the estimation version, players can state aloud what their exact space would be and how close they are to the space they move onto to. Which space is the closest and why

## Guiding Questions:

What do you know?
Where do you think you will begin?
Where are you stuck? What is confusing? What are you wondering about?
What are you going to try?
What did you think about to come to your answer?

## Differentiation:

Two versions of the game can be used for grades 3-5. Rolling for $\mathbf{5 0 0}$ gives practice with place value strategies to add and subtract numbers up to 500 . Rolling for 500 estimation gives practice with place value strategies for addition and subtraction and also requires comparative reasoning in order to properly place the game board marker.
Game Trajectory: $\quad$ Clean up Checklist for Game Bag:
Pre K-K: Counting along a number line to 20
K-2: Addition and subtraction to get to 50
3-5: Rolling for 500 or Rolling for 500 estimation version


# - Grade 3 Topic 11: Use Operations with Whole Numbers to Solve Problems 

Big Conceptual Idea: Operations and Algebraic Thinking, K-5 (pp. 22-28)

Prior to instruction, view the Topic 11 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 571A-571F), the Topic Planner (pp.57II-571J), all 4 lessons, and the Topic Assessments (pp. 603-604A).

## Mathematical Background:

Read Topic 11 Cluster Overview/Math Background (TE, pp. 571A-571F)

## Topic Essential Question:

What are ways to solve two-step problems?
Reference Answering the Topic Essential Question (TE, pp. 601-602) for key elements of answers to the Essential Question.

The lesson map for this Topic is as follows:

| $11-1$ | $11-2$ | $11-3$ | $11-4$ | Assessment |
| :---: | :---: | :---: | :---: | :---: |

4 A/D/E days used strategically throughout the topic.

## Instructional note:

In Topics 1 through 5, students developed conceptual understanding of multiplication and division. In Topics 6 \& 7, students applied this understanding of multiplication to area and data concepts. In Topics 8 \&

Topic 11 Use Operations with Whole Numbers to Solve Problems

Number of lessons: 4

A/D/E: 4 days

NVACS Focus: OA.D

Total Days: ~8 9 , students further developed their understanding of addition and subtraction concepts. All of this work developed operational sense.

In Topic 11 students further develop their operational sense by, "Solving problems involving the four operations..." (NVACS, 3.OA.D). Topic 11 provides students the opportunity to become more secure in this understanding as they solve two-step word problems using the four operations, identify arithmetic patterns and explain them using the properties. The focus in this topic is on algebraic thinking using, "real-world situations that can be represented using variables, operations, and equations" (TE, p. 571C). In supporting students with developing algebraic thinking, it is crucial that the algebraic language of an unknown and what the unknown represents is addressed through classroom discussion.

Third grade is the first time students start representing the unknown with a letter variable, in previous grades the unknown was represented with a box or symbol. Students should make the connection that a letter is equivalent to a question mark or an open box (Small, 2014).
"Students need to be aware that any letter they choose is acceptable, and no one letter is preferable to another. Many teachers and students advocate using a letter that helps the student remember what the value represents. For example, in the problem "There were 24 students at 4 tables. The same number of students was at each table. How many were at each table?" students might use $s$ in the equation $24 \div 4=s$ to represent students in the problem. Many students just pick any word in the problem to suggest a letter and might use $t$ from table. This, again, is not incorrect, but in the end it is critical that the students understand what their answer represents-the number of students at each table, not the number of tables" (Small, 2014, p. 31).

In this topic, students identify what the unknown is and represent it with a variable in both models and equations. To support students as they reason with two-step word problems enVisionmath2.0 asks students, "What is the hidden question?" referring to the first step that must be answered before the stated problem can be solved for. Students have worked with the idea of a "hidden question" since $2^{\text {nd }}$ grade and have revisited it in previous topics.

This topic extensively uses the bar diagram to model the two-step problems, often encouraging the use of a bar diagram for each step. Encourage students to make the area of each part of the part-part-whole bar diagram representative to the quantity of the numbers that part is representing. enVisionmath2.0 does a great job of modeling this for the students. In doing this, students are supported in developing magnitude of number, estimation skills (especially when the
 unknown is one of the parts), and being able to discern an additive situation from a multiplicative situation. As shown in the included image (TE, p. 571A), a multiplicative situation will have equal sized parts, whereas, an additive situation may have different size parts.

As students' algebraic thinking develops, they will discover that some multi-step problems are solved using different operations. As a result of this idea, students will revisit the conventions for order of operations by writing a single equation that represents the multiple steps taken to solve the problem (lesson 11-3). The Operations and Algebraic Thinking progression document provides more insight into the conventions of order of operations in regards to third grade:

Understanding and using the Associative and Distributive Properties (as discussed above) requires students to know two conventions for reading an expression that has more than one operation:

1. Do the operation inside the parentheses before an operation outside the parentheses (the parentheses can be thought of as hands curved around the symbols and grouping them).
2. If a multiplication or division is next to an addition or subtraction, imagine parentheses around the multiplication or division (it is done before these operations). In Grades 3 through 5, parentheses can usually be used for such cases so that fluency with this rule can wait until Grade 6.

These conventions are often called the Order of Operations and can seem to be a central aspect of algebra. But actually they are just simple "rules of the road" that allow expressions involving more than one operation to be interpreted unambiguously and thus are connected with the mathematical practice of communicating precisely (MP.6). Use of parentheses is important in displaying structure and thus is connected with the mathematical practice of making use of structure (MP.7). Parentheses are important in expressing the associative and especially the distributive properties. These properties are at the heart of Grades 3 through 5, because they are used in the Level 3 multiplication and division strategies, in multi-digit and decimal multiplication and division, and in all operations with fractions (pp. 27-28).

While we are not expecting security on these conventions and it is not assessed in our Topic Assessment, lesson 11-3 focuses on bullet 2 of these conventions. Consider modeling how to write equations used in the Solve \& Share and Visual Learning for all the lessons in this topic following these conventions.

Focus Math Practice 3: Construct viable arguments and critique the reasoning of others
The standard state, "They (students) make conjectures and build a logical progression of statements to explore the truth of their conjectures.... Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and -if there is a flaw in and argument- explain what it is" (NVACS, 2010, p. 6-7). Behaviors associated with MP. 3 are described in the Teacher's Edition (pp. F23-F23A) and the Nevada Academic Content Standards for Mathematical Practice.

Looking ahead to the Topic Performance Assessment, item 4 Part A requires students to use their understanding of estimation and number sense to assess the reasonableness of a fictitious teacher's argument. To support students' development of the mathematical understandings needed to respond to this question consider frequently asking students if a solution is reasonable and why. For students to be successful with this assessment they will have to attend to all the information provided in the questions. In item 3 , the word "all" makes a large impact on what students need to do to demonstrate what they know.

Therefore, throughout this topic continue to ask students if they have answered all of the problem and how they know. While developing the thinking habits that allow students to engage in this problem type are highly beneficial, you may need to scaffold working with the Topic Performance Assessment to help students develop these thinking habits.

| Essential <br> Use these words consistently during instruction. |  |  |
| :--- | :--- | :--- |
|  | Review Academic Vocabulary: |  |
| New Academic Vocabulary: |  | (First time explicitly taught) |

Additional terminology that students may need support with: unknown, hidden question

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding question: "Are students making sense of the problem and using appropriate operations to solve multi-step word problems?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $11-1$ | Solve \& Share (student work samples) | Focus CTC around the big idea: <br> $\bullet \quad$ look for students who explain the properties. <br> $\bullet \quad$ use information from table to accurately solve the problem. <br> $\bullet \quad$ all parts of multi-step problem are answered. |
| $11-3$ | Quick Check (digital platform) <br> Items 1, 4, and 5 | Focus CTC around data analysis and collection of student workspace <br> (scratch paper). Printable version available under "Teacher Resources". <br> $\bullet \quad$ all parts of multi-step problem are answered. <br> $\bullet \quad$ make sense of problems. |


| Learning Cycle | Topic Assessments <br> SE pp. 601-604 | Use Scoring Guide TE pp. 601-604A |
| :---: | :--- | :--- |
| Assessments (summative) |  |  |

Standards listed in bold indicate a focus of the lesson.

\(\left.$$
\begin{array}{|l|l|l|}\hline & & \begin{array}{l}\text { If students do not offer a solution method that is the same as "Diana's Work", then consider } \\
\text { discussing "Diana's Work" as a class. Notice that Diana uses a bar diagram to solve for both the } \\
\text { hidden question and the final question. } \\
\text { Look Back: }\end{array}
$$ <br>
Consider discussing the Look Back! prompt to help students develop habits of estimation to <br>

determine reasonableness of solutions.\end{array}\right\}\)| Visual Learning: |
| :--- |
| Read the Instructional Note at the beginning of this topic for information on supporting students |
| as they transition from using a box or symbol to represent the unknown to using a letter |
| variable. |


|  |  | After viewing the Visual Learning Animation, consider asking students how they could write a single equation for the Solve \& Share (e.g. $9 \times 5+75$ ). <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 9 Number Sense to practice estimation using compatible numbers. <br> Assess \& Differentiate: <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 589A). <br> *CTC: Quick Check (digital platform) |
| :---: | :---: | :---: |
| Lesson 11-4: Math Practices and Problem Solving- Critique Reasoning |  |  |
| 3.OA.D. 8 <br> MP. 3 <br> MP. 1 <br> MP. 2 <br> MP. 5 <br> MP. 6 | Access Prior Learning <br> In lesson 11-3 students continued to develop their understanding of 2-step word problems and operational sense with all 4 operations and MP. 3 as they justified the operations they used. <br> Developing the Big Idea In this lesson, students further develop their understanding of MP. 3 "Construct viable arguments and critique the reasoning of others" using all 4 operations to justify conjectures. | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 3, "Construct viable arguments and critique the reason of others." Refer to the Math Practices and Problem Solving Handbook (TE, pp. F23-F23A, F29) for suggestions on how to develop, connect and assess this Math Practice. Also reference the handbook in the Student Edition (SE, p. F23). <br> Solve \& Share: <br> Consider reintroducing MP. 3 Thinking Habits (SE, p. F23) before introducing the Solve \& Share. Watch for students that agree with Skip's reasoning and support by asking the questions provided in Ask Guided Questions as Needed. <br> Also consider using the time where students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP. 3 that are listed in the Math Practices and Problem Solving Handbook (p. F23A), and after discussing student solution methods and reasoning, have students self-score for the behaviors associated with this math practice. <br> Look Back: <br> Consider facilitating a whole class discussion using the Look Back! question to support students' mathematical reasoning skills and place value understandings. <br> Visual Learning: <br> Consider pausing the animation to discuss Danielle's reasoning. <br> Convince Me: <br> Consider assigning the Convince Me! as it provides an opportunity for students to reason more with MP. 3 by supporting a conjecture. <br> Assess \& Differentiate: <br> If time permits, you may consider replacing the Math and Science Activity with games from previous topics or the Fluency Practice Activity (TE, p. 597). <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided. |

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## - Grade 3 Topic 12: Understand Fractions as Numbers

Big Conceptual Idea: Number and Operations Fractions, 3-5 (pp. 3-5)
Prior to instruction, view the Topic 12 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 605A-605F), the Topic Planner (pp.605I-605K), all 8 lessons, and the Topic Assessments (pp. 667-668A).

| Mathematical | Topic Essential Question: |
| :--- | :--- |
| Background: | What are different interpretations of fractions? |
| Read Topic 12-13 Cluster | Reference Answering the Topic Essential Question (TE, pp. 663-664) for key elements |
| Overview/Math Background |  |
| (TE, pp. 605A-605F) | of answers to the Essential Question. |

## The lesson map for this topic is as follows:

| $12-1$ | $12-2$ | $12-3$ | $12-4$ | $12-5$ | $12-6$ | $12-7$ | $12-8$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

4 A/D/E days used strategically throughout the topic.

$3^{\text {rd }}$ Grade Curriculum
Pacing Framework:
Balanced Calendar
Topic 12
Understand Fractions as Number of lessons: 8

A/D/E: 4 days
NVACS Focus: NF.A

Total Days: ~12

## Instructional note:

Topic 12's big idea is on developing understanding of fractions as numbers (fractional number sense).
Students work to accurately position fractional numbers on the number line. Third grade is the first time the Numbers and Operations-Fractions domain appears in the Nevada Academic Content Standards (NVACS). However, students build fractional understanding beginning in Kindergarten. Prior knowledge that was developed in the Geometry domain (please note there are other ideas in MD that also build toward these outcomes and understandings).

Kindergarten
K.G.B. 6 Compose simple shapes to form larger shapes. For example, "Can you join these two triangles with full sides touching to make a rectangle?" (NVACS, 2010, p. 12).
First
1.G.A. 3 Partition circles and rectangles into two and four equal shares, describe the shares using the words halves, fourths, and quarters, and use the phrase half of, fourth of, and quarter of. Describe the whole as two of, or four of the shares. Understand for these examples that decomposing into more equal shares creates smaller shares (NVACS p.16).
Second
2.G.A. 3 Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, fourths, half of, third of, and etc., and describe the whole as two halves, three thirds, or four fourths. Recognize that equal shares of identical wholes need not have the same shape (NVACS, p. 20).

Both first and second grade work with establishing fractional language of fourths, thirds, halves, and the whole. Topic 12 begins with dividing shapes into equal regions and formally naming them as a fraction. Students name the area with unit fractions. Empson and Levi describe, "The value of any fraction is determined by the multiplicative relationship between the numerator and denominator" (2010, p. 4). This relationship is seen in third grade standards with unit fractions and iterating units. Students are expected to engage in reasoning with the structure of iterations and unit fractions. They are asked to identify what the whole would look like when only shown a fractional amount of the whole. For example, students are shown $\frac{1}{3}$ of a distance on a line segment and are expected to identify which line segment represents the whole. This mathematical understanding relies on iterations, or copies of the unit fraction. When the unit fraction is known, we can then make additional copies of it until the whole has been built.

Note that students with weak spatial structuring and reasoning may struggle with this idea. Consider providing support with geoboards and linear measuring tools such as tape measures and rulers when relating to a number line. This understanding becomes critical for developing the fractional sense in fourth grade that's needed for operating on fractions. In fourth grade students will explore the idea that fractions, just like whole numbers, can be decomposed. For example, just as I can decompose 10 into 8 and 2, I can decompose $\frac{3}{4}$ into $\frac{1}{4}+\frac{1}{4}+\frac{1}{4}$.

Second grade standards are designed to develop students' spatial structures and reasoning to be able to, "Recognize that equal shares of identical wholes need not have the same shape" (NVACS, 2010, 2.G.A.3). Another important idea worth revisiting is that while our parts do have to be equal in area they do not have to be congruent in shape (NVACS, 2010, 2.G.A.3).

Developing concept of the whole in the part-whole structure is crucial for future work in the other interpretations. Therefore, as we continue to stress the importance of what is the whole, we also discuss ideas such as, "How can we show a whole ( $1, \frac{4}{4}, \frac{3}{3}$, etc.)", "How do we show a fraction beyond one (whole) on the number line ( $\frac{4}{3}, \frac{2}{1}$, etc.)?" and, "How does the fraction communicate the relationship between the amount of equal parts being discussed in the whole?"

Despite previously partitioning circles and rectangles in equal parts for halves, thirds, and quarters, doing so on a number line may be new for students; especially if they did not have sufficient time working with the second grade measurement standards. As a wholegroup enrichment activity it may be helpful to build a number line that stretches across the classroom starting at 0 and going to 2 that shows halves, thirds, fourths, sixths, and eighths (these are the denominators that fractions in $3^{\text {rd }}$ grade are limited to per NVACS, 2010, p.25). Going beyond one whole gives students the opportunity to discuss and communicate how a fraction can be greater than one and understand that depending upon the equal number of parts needed to make the whole(s) (denominator), fractions greater than one can be named in many different ways. This will also connect to the understandings developed in $2^{\text {nd }}$ grade and help link measurement to working with the number line. Providing students the opportunity to discuss the difference between $\frac{1}{2}, \frac{2}{1}$ and $\frac{2}{2}$ will clarify common confusions, partial understandings and misunderstandings that are often found at this grade level and better develop understanding of the role of the numerator and denominator.

Developing fractional sense offers many opportunities to confront common misconceptions. Small (2014) identifies the following common misconceptions:

- conflicts with prior knowledge about whole numbers, such as:
o there is always a specific "next" whole number, but there is no specific next fraction.
o 1 being the smallest number, but then finding out there are smaller numbers.
o division makes amounts smaller, but not when dividing by proper fraction (not covered in 3 rd grade).
o 3 being more than 2 , but $\frac{1}{3}$ being less than $\frac{1}{2}$; or $\frac{4}{5}$ being more than $\frac{7}{10}$ even though 7 and 10 are more than 4 and 5 .
- too often using faulty perceptual arguments rather than mathematical reasoning to compare two fractions.
- viewing the numerator and denominator as separate entities (as essentially two numbers) rather than viewing the fraction as a single number.
- believing that fractions are always less than 1, perhaps because of the early emphasis on fractions as being parts of a whole, which become problematic once fractions greater than 1 are introduced.
- difficulties in placing fractions on number lines that extend past 1 (e.g., marking the point 2 when asked to place $1 / 2$ on a number line that extends from 0 to 4).
- not recognizing the role the whole plays in describing a fraction.

The commonly accepted definitions for the numerator and denominator often develop the misconception of seeing each as a separate whole number. This misconception results in confusion in later grades when students are asked to operate on fractions by generalizing whole number strategies. Avoiding this misconception means we need to develop understanding of fractions as numbers the same way students developed understanding of whole numbers, by starting with counting and redefining our numerator and denominator to honor this development. Doetch (2017) explains it this way:
"Students must learn that a fraction does not tell us anything about the size of the whole or the size of the part. A fraction tells us only about the relationship between the part and the whole".
"In whole-number learning, counting helps students compare the size of numbers and later to add and subtract. This is also true with fractions. Students should come to think of counting fractional parts in much the same way as they might count with counters (bears, cubes, Unifix cubes, or other objects). When students know the parts they are counting, they can tell when they get to one whole. Students should be able to answer the following questions.
'How many thirds are in a whole?'
'How many fifths are in a whole?'
'How many twelfths are in a whole?'
Counting by repeating a piece is called iterating. Understanding that $\frac{3}{4}$ can be thought of as a count of three parts called
fourths. This concept becomes clear when focusing on these two ideas about fractions.

- The numerator counts.
- The denominator tells what fractional part is being counted.

Another way to think of it is.

- The numerator tells how many to count.
- The denominator tells what is being counted."

Additionally, when students develop understanding of fractions as numbers by counting we no longer need to use the language "out of" to describe a fractional amount, for example, $\frac{3}{4}$ as 3 out of 4 . This language supports ratio understandings which are not explored until $6^{\text {th }}$ grade.

As this is students' first formal introduction to fractions there may be need to spend more than 1 day on a lesson. The need to spend more than 1 day on a lesson should be a balance of being learner responsive and pacing considerations; therefore, making a lesson a 2-day lesson is a class by class decision. As a result, an additional Solve \& Share is offered for most lessons. The Another Look videos could be used to fill-in for a Visual Learning Animation. Please note the intent is not that every lesson become a 2-day lesson, but rather, to provide the resource if it is needed.

Throughout this topic, you will notice how essential it is for our $1^{\text {st }}$ and $2^{\text {nd }}$ grade teachers to ensure instruction to both the Geometry and Measurement and Data Domains. Failure to instruct to all the standards in $1^{\text {st }}$ and $2^{\text {nd }}$ grade have a critical impact on forming the necessary foundations for working with fractional models and developing the necessary understandings of fractions in 3rd grade.

Focus Math Practice 1: Make sense of problems and persevere
Focus on opportunities for students to develop Mathematical Practice 1 behaviors throughout the entire topic, as this is the focus of the Math Practices and Problem Solving lesson 4-9. Reference the Teacher's Edition (pp. F21-F21A) and the Nevada Academic Content Standards for Mathematical Practice.

|  | Essential Academic Vocabulary <br> Use these words consistently during instruction. |  |
| :--- | :--- | :--- |
| New Academic Vocabulary: <br> (First time explicitly taught) | Review Academic Vocabulary: <br> unit fraction | line plot |
| (Vocabulary explicitly taught in prior grades or topics) |  |  |

Additional terminology that students may need support with: divide (meaning to equally partition something)

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding questions: "Are students understanding the size of the whole is determined by the fractional part?"
"Are students able to accurately display data on a line plot?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $12-3$ | Quick Check (digital platform) | Focus CTC around data analysis and collection of student workspace <br> (scratch paper). Printable version available under "Teacher Resources". <br> • understand the fraction part of the whole determines the whole. |
| $12-7$ | Solve \& Share (student work samples) | Focus CTC around the big idea: <br> $\bullet \quad$look for students who accurately measure sides of polygon. <br> and display data on line plot to the nearest $1 / 2$ inch. <br> identify most common length of polygon. |


| Learning Cycle <br> Assessments (summative) | Topic Assessments <br> SE pp. 663-668 | Use Scoring Guide TE pp. 663-668A |
| :---: | :--- | :--- |

Standards listed in bold indicate a focus of the lesson.

| NVACS <br> (Content and Practices) | Mathematical Development of the Big Idea | Instructional Clarifications \& Considerations |
| :---: | :---: | :---: |
| Lesson 12-1: Divide Regions into Equal Parts |  |  |
| $\begin{gathered} \text { 3.NF.A. } 1 \\ \text { 3.G.A. } 2 \\ \\ \text { MP. } 1 \\ \text { MP. } 2 \end{gathered}$ | Access Prior Learning: In Topic 15, Grade 2, students partitioned rectangles into rows and columns of same-size squares. They also partitioned circles and rectangles into halves, thirds, and fourths. | Instructional note: <br> Consider creating a class anchor chart to connect prior foundational knowledge from grades 1 (1.G.A.3) and 2 (2.G.A.3) by drawing one polygon and partitioning it into halves. Have students provide the language that each equal part is a half and label each equal part as a half of the whole polygon. Include the idea that two halves make one whole. Repeat this process with thirds and fourths (connecting the term "quarters" to fourths). <br> -continues on next page- |


| MP. 3 <br> MP. 4 <br> MP. 6 <br> MP. 7 | Beginning of the Big Idea: <br> Students are beginning to develop fractional sense by connecting the language of halves, thirds, and fourths to formal written form $\frac{1}{2}, \frac{1}{3}$, and $\frac{1}{4}$ while introducing $\frac{1}{6}$. <br> Students will also begin developing understanding of a unit fraction. | Solve \& Share <br> Students are asked to color two different area models to show six equal parts of the whole. Students should recognize that even when colored differently, the number of equal sized parts to make the whole must be the same (denominator) to compare the number of equal sized colored parts (numerator) between the regions. <br> Visual Learning: <br> The term "unit fraction" as being single equal parts of the whole will be used in the Visual Learning Animation. Numerator and denominator will also be discussed. <br> Convince Me: <br> Consider assigning and discussing the Convince Me! as this supports the development of spatial structure in fractions. Students that are struggling with this idea may benefit from additional work with geoboards or area model representations to explore these ideas further. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning items 5, 6, 9, and 10 and support with geoboards or area model representations to support understanding fractions as equal parts of a whole. <br> Assess and Differentiate: <br> If time permits, consider using the Intervention Activity to strengthen the idea that fractions must be equal parts of the whole. Students will benefit from explaining their reasoning about how they know the parts are equal. |
| :---: | :---: | :---: |
| Lesson 12-2: Fractions and Regions |  |  |
| $\begin{gathered} \text { 3.NF.A. } 1 \\ \text { 3.G.A. } 2 \\ \\ \text { MP. } 1 \\ \text { MP. } 2 \\ \text { MP. } 4 \\ \text { MP. } 6 \end{gathered}$ | Access Prior Learning: In Topic 15, Grade 2, students partitioned rectangles into rows and columns of same-size squares. They also partitioned circles and rectangles into halves, thirds, and fourths. <br> Beginning of the Big Idea: Students are beginning to develop fractional sense by connecting the language of halves, thirds, and fourths to formal written form $\frac{1}{2}, \frac{1}{3}$, and $\frac{1}{4}$ while introducing $\frac{1}{6}$. <br> Students will also begin understanding that a fraction represents multiple copies of a unit fraction (iterations). | Solve \& Share: <br> Watch for students that do not partition the rectangle into four equal size parts and support as needed. <br> During the whole class discussion consider developing student understanding of naming parts of a whole as a fraction, as well as, fraction as number; by asking them, "How much of the garden did Pat plant flowers?" Students may likely say 3. In this case, build on their $2^{\text {nd }}$ grade learning experiences by asking them, "What did we break the whole into?" At this point, support students in developing understanding of the denominator as telling us "what fractional part is being counted" and the numerator counts (Van de Walle, Karp, Lovin, \& Bay-Williams, 2014). <br> Look Back: <br> Consider discussing the Look Back! as a whole group to facilitate and develop students' understanding that there are 2 fractions with every representation, the one being discussed and what's not being discussed. For example, when $3 / 4$ of the whole is shaded, $1 / 4$ of the whole is unshaded. <br> Visual Learning: <br> Consider pausing and discussing after the Visual Learning Animation asks, "What is the whole?" Can students explain how they know what the whole is? Another pausing point to consider is, "Which parts of the fractions are the same? Why?". <br> Convince Me: <br> Consider assigning and discussing the Convince Me! to give students the opportunity to reason with the idea of unit fractions. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 14 as it provides an opportunity for distributed practice of 2-step problems with multiple operations. <br> Assess and Differentiate: <br> If time permits, teach students how to play Toss and Talk or Teamwork. All students should have the opportunity to play both of these games as they provide engaging and meaningful practice of a key concept. |
| Lesson 12-3: Understand the Whole |  |  |
| 3.NF.A.3c <br> 3.NF.A. 1 <br> MP. 2 <br> MP. 3 <br> MP. 7 | Access Prior Learning: <br> In previous lessons students learned that a fraction represents multiple copies (iterations) of a unit fraction. | Solve \& Share: <br> To assess students' readiness consider drawing a rectangle partitioned into halves and ask students to label the unit fraction into each part prior to introducing the Solve \& Share. <br> For students that struggle with the idea that a unit fraction can be iterated (make additional copies of) until the whole has been built, see the Instructional note at the beginning of this document for ideas on how to support and consider discussing the prompts provided in Ask Guiding Questions as Needed. <br> -continues on next page- |


| MP. 8 | Developing the Big Idea: Students are beginning to understand that they can repeat copies (iterate) of a unit fraction this can determine the whole. | Look Back: <br> Consider discussing the Look Back! while students share their solution methods and reasoning. This question helps students understand that there are 2 fractions with every representation, the one being discussed and what's not being discussed. This question develops an idea that will be discussed in the Visual Learning Animation, the size of the unit fraction can help to discover the size of the whole. <br> Visual Learning: <br> The Visual Learning Animation illustrates the part-whole relationship with the unit fraction. Students discover that the size of the whole can be determined by knowing the size of the unit fraction. This relates well to area models which make the relationship between wholes and unit fractions explicit. Consider $\frac{1}{6}$ of a personal pizza and $\frac{1}{6}$ of a family size pizza. To support students' development of this understanding, consider pausing and discussing after the following questions are posed: <br> - Do you think your pictures for the tracks will be the same or different? Why? <br> - What do you need in order to draw 6 lengths of $1 / 6$ ? <br> - What fraction is one whole equal to in this problem? <br> Another Example: <br> Consider posing the question, "How are the area model (used in the Solve \& Share and Another Example!) and the linear model (used in the Visual Learning) similar and different?" Help students make connections across models and recognize fraction as a number (represents a quantity) to the models. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Math and Science Activity with the games Teamwork, Toss and Talk, or the Fluency Practice Activity. <br> *CTC: Quick Check (digital platform) |
| :---: | :---: | :---: |
| Lesson 12-4: Number Line- Fractions Less than 1 |  |  |
| 3.NF.A.2a <br> 3.NF.A.2b <br> MP. 3 <br> MP. 4 <br> MP. 6 | Access Prior Learning: <br> In previous lessons in this topic students learned that the denominator indicates the number of equal parts that the whole is divided into and the numerator indicates how many equal parts the fraction represents. <br> Developing the Big Idea: <br> Students further develop their understanding of fractions by finding that points on a number line can represent fractions. The denominator represents the number of equal parts between 0 to 1 , and the numerator represents the number of parts between 0 and the point. | Solve \& Share: <br> Child-watch for students that have the misconception of starting with $\frac{1}{3}$ instead of $\frac{0}{3}$. In addition, child-watch for students that are confusing what the whole represents (1-mile). <br> Look Back: <br> Consider discussing the Look Back! to support students' fraction reasoning. <br> Visual Learning: <br> Consider discussing the Convince Me! to revisit the ideas developed in lesson 12-3's Visual Learning Animation. <br> Assess and Differentiate: <br> Consider having all students do the Intervention Activity (TE, p. 631A) to work more with the number line model. <br> Possible Day 2 Solve \& Share: <br> (Read the Instructional note at the beginning of this topic for guidance on making a lesson more than 1 day.) Consider using item 10 MP. 6 Be Precise from the Independent Practice/Math Practices and Problem Solving. |
| Lesson 12-5: Number Line- Fractions Greater than 1 |  |  |
| 3.NF.A.2b <br> 3.NF.A.2a <br> 3.NF.A.3c <br> MP. 3 <br> MP. 4 <br> MP. 5 <br> MP. 6 <br> MP. 8 | Access Prior Learning: <br> In the previous lesson students learned to use number lines to work with fractions. <br> Developing the Big Idea: Students further develop their understanding of representing fractions on a number line by generalizing to represent fractions greater than 1 on a number line. Students further develop their fractional sense by developing | Instructional note: <br> The primary purpose of this lesson is to confront the misconception that it is not possible to have fractions greater than 1. <br> Solve \& Share: <br> As students generalize understanding of fractions greater than 1 to a number line, it may be helpful to relate it to fractions on a ruler. Consider discussing the Look Back! to support students' fraction reasoning. <br> After students have shared their solution methods and reasoning, consider discussing the Look Back! to generalize understandings developed from the Solve \& Share. |


|  | understanding of how to represent a whole number as a fraction. | NVACS standard 3.NF.A.3c calls for students to, "Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. Examples: Express 3 in the form $3=$ $\frac{3}{1}$; recognize that $\frac{6}{1}=6$; locate $\frac{4}{4}$ and 1 at the same point of the number line diagram" (2010). Therefore, consider holding up 2 more whole strips of paper and asking students how do represent 2 wholes as a fraction (e.g., $\frac{2}{1}$ ). Don't worry if students are struggling with this idea, it will be further developed in lesson 13-7. <br> Visual Learning: <br> The Visual Learning Animation asks, "What do the marks on the number line represent?" Consider pointing out that it is necessary to know how many equal parts there are from 0 to 1 on a number line before writing missing fractions. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 13 Critique Reasoning for distributed practice of the Associative and Distributive Properties of Multiplication. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Problem Solving Reading Mat with the game Teamwork (TE, p. 619A) or Toss and Talk (TE, p. 613A, TE, p. 631A). <br> Possible Day 2 Solve \& Share: <br> (Read the Instructional Note at the beginning of this topic for guidance on making a lesson more than 1 day.) Consider using item 10 MP. 6 Be Precise from the Independent Practice/Math Practices and Problem Solving. |
| :---: | :---: | :---: |
| Lesson 12-6: Line Plots and Length |  |  |
| $\begin{gathered} \text { 3.MD.B. } 4 \\ \text { MP. } 1 \\ \text { MP. } 2 \end{gathered}$ | Access Prior Learning: In Topic 14, Grade 2, students measured to the whole inch and represented the data on a line plot. In lesson 12-4, Grade 3, students learned to represent fractions on a number line. <br> Developing the Big Idea: Students further develop their understanding of representing fractions on a number line by generalizing understanding from lesson 12-4 and extend it to representing fractions beyond 1 on a number line. | Instructional Note: <br> Standard 3.MD.B. 4 states that students use rulers to collect measurement data and show the data using whole numbers, halves, or quarters. Student measure to the nearest $1 / 4$ inch before the nearest half inch to establish the $1 / 4$ marks as benchmarks for when measuring to the nearest $1 / 2$ inch. <br> Solve \& Share <br> Consider assessing readiness prior to introducing the Solve \& Share, by distributing rulers and asking students what they know or notice about the inches side of a ruler. Ideas to generate in this conversation are: <br> - When measuring objects, we start at 0 . <br> - The numbers on the ruler indicate inches. <br> - The lines in between the inches indicate where each inch has been partitioned into halves and quarters. <br> - Where the marks for halves and quarters marks are located. <br> - How to read measurements that go past a whole to the nearest $\frac{1}{2}$; and $\frac{1}{4}$ inch. <br> Child-watch for students that do not start their measurements correctly along the ruler and support as needed. Also watch for students that need support to measure to the half inch and quarter inch. <br> After students have shared their solution methods and reasoning, consider discussing the Look Back! to revisit ideas from Topic 7 with bar graphs and picture graphs. <br> Visual Learning: <br> As students generalize understanding of fractions to a number line, it may be helpful to relate it to fractions on a ruler. Consider asking and discussing, "How do you know which tick mark is appropriate for reasoning with fractions of fourths?". Also discuss and revisit the ideas of scaling and precision when gathering/representing data from Topic 7. <br> Assess and Differentiate: <br> Consider doing the Intervention Activity (TE, p. 643A) with all students as it asks them to make a line plot using the given lengths. <br> Possible Day 2 Solve \& Share: <br> (Read the Instructional Note at the beginning of this topic for guidance on making a lesson more than 1 day.) Consider using items 9 and 10 from the Independent Practice/Math Practices and Problem Solving. |


| Lesson 12-7: More Line Plots and Length |  |  |
| :---: | :---: | :---: |
| $\begin{gathered} \text { 3.MD.B. } 4 \\ \text { MP. } 1 \\ \text { MP. } 2 \\ \text { MP. } 4 \\ \text { MP. } 5 \\ \text { MP. } 6 \end{gathered}$ | Access Prior Learning: <br> In the previous lesson, students use what they know about number lines and fractions to understand that points plotted onto a number line create a line plot, which helps organize and interpret data to the quarter inch. <br> Developing the Big Idea: <br> In this lesson, students are further developing their understanding of line plots, but to the nearest half inch. Students also develop the understanding that a half-inch is two quarter inches. | Instructional note: <br> Identifying $1 / 4$ measurements on a ruler can be reinforced in lesson 12-7 as students can use $1 / 4$ and $3 / 4$ measurements to determine if the measurement is closest to a whole inch or the half inch. <br> Solve \& Share: <br> Consider printing the rulers provided in Teaching Tool 19 and drawing your own polygon for students to measure as the one provided in the book does not yield consistent measurements. Continue to watch for students that do not start their measurements correctly along the ruler and support as needed. Also watch for students that need support to measure to the half inch and quarter inch. <br> Visual Learning: <br> After the Visual Learning Animation asks, "How do you know that the $3 \frac{1}{2}$ - inch length occurred most often?" Consider wrapping up the discussion by pointing out that every dot on a number line represents actual data. When data changes, the line plot also needs to change. <br> Independent Practice/Math Practice and Problem Solving: <br> Consider using items 12 and 13 as students use information in a table to solve problems. Consider asking students to make a line plot of the data presented in the table. <br> Assess and Differentiate: <br> Consider having all students do the Intervention Activity (TE, p. 649A) as it gives students the opportunity to measure items, collect data and use the data collected to build a line plot. |
| Lesson 12-8: Math Practices and Problem Solving- Make Sense and Persevere |  |  |
| 3.NF.A. 1 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 6 | Access Prior Learning: In previous lessons, students have developed an understanding of fractions as number and representing data with fractions on a line plot. <br> Developing the Big Idea: Students are further developing their understanding of MP. 1 and fractions as numbers to analyze given information and determine what is or is not needed to solve problems in real-world contexts. | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 1. Refer to the Math Practices and Problem Solving Handbook (TE pp. F21-F21A, F29) for suggestions on how to develop, connect and assess this Math Practice. Also reference the handbook in the Student Edition (SE, p. F21). <br> Solve \& Share: <br> Consider reintroducing MP. 1 Thinking Habits (SE, p. F21) before introducing the Solve \& Share. Also consider using the time students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP. 1 that are listed in the Math Practices and Problem Solving Handbook (TE, p. F21A). After discussing student solution methods and reasoning, have students self-score for the behaviors associated with this math practice. <br> Visual Learning: <br> Considering pausing and discussing, "How can I make sense of and solve this problem?". For all problem solving it is key that students know what the problem is asking and generate a plan for finding that information. <br> Assess and Differentiate: <br> If time permits, consider teaching students how to play the game Teamwork (TE, p. 655A). All students should have the opportunity to play this game as it provides engaging and meaningful practice of a key concept. |

## References

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Empson, S. B., \& Levi, L. (2011). Extending children's mathematics: Fractions and decimals. Mathematics Education, 27(4), 403-434.
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Van de Walle, J., Karp, K., Lovin, L., \& Bay-Williams, J. (2014). Teaching student-centered mathematics: Developmentally appropriate instruction for grades 3-5 (2nd ed.). Boston, MA: Pearson.

## - Grade 3 Topic 13: Fraction Equivalence and Comparison

Big Conceptual Idea: Number and Operations Fractions, 3-5 (pp. 3-5)
Prior to instruction, view the Topic 13 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 605A-605F), the Topic Planner (pp.669A-669C), all 8 lessons, and the Topic Performance Assessment (pp. 731-732A).

| Mathematical | Topic Essential Question: |
| :--- | :--- |
| Background: | What are different ways to compare fractions? |
| Read Topic 12-13 | Reference Answering the Topic Essential Question (TE, pp. 727--728) for key |
| Cluster Overview/Math | elements of answers to the Essential Question. |
| Background (TE, pp. |  |
| 605A-605F) |  |

## The lesson map for this topic is as follows:

| $13-1$ | $13-2$ | $13-3$ | $13-4$ | $13-6$ | $13-5$ | $13-7$ | $13-8$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

3 A/D/E days used strategically throughout the topic.

## Instructional note:

Topic 13's big idea is in developing the idea of fractions as numbers (fractional number sense) and equivalence. As you read on, you will find that the question, "What is the whole?" will be critical when working with fraction equivalence and comparison. Students must be able to identify, or make the assumption that they are working with the same size whole in order to identify equivalent fractions and make comparisons. Chapin and Johnson (2006) state the following in regards to fraction equivalence:
"Equivalence is one of the most important mathematical ideas for students to understand, particularly with regard to fractions. Equivalence is used in when comparing fractions, ordering fractions, and adding and subtracting fractions. Equivalent fractions are fractions that represent equal value; they are numerals that name the same fractional number. When represented using a number line, equivalent fractions represent the same distance" (p.114).

The importance of the whole is key to third grade fraction standards. Van de Walle, Karp, Lovin, Bay-Williams (2014) state, "Every fraction is equal to an infinite number of other fractions" (p. 220). This idea includes seeing whole numbers as fractions as outlined in the Numbers and Operations-Fractions, 3-5 progression document (p. 4). Consider using a number line to model this understanding. Topic 13 does this throughout the topic using the double number line.

This topic explores strategies to compare nonequivalent fractions with the same whole. A key idea in comparing fractions is understanding that the larger the denominator the smaller the unit fraction, when comparing fractions with the same denominator the larger the numerator the larger the fraction. Emphasize and formalize these ideas as student discover them. Focus on providing many experiences for students to notice these patterns rather than explicitly teaching them.

Throughout this topic, fraction strips and number lines are heavily used to model the ideas of fraction equivalence and comparison. Van de Walle, et. al. states, "Sometimes it is useful to do the same activity with two different representations as they offer different opportunities to learn. For example, an area model helps students visualize parts of the whole, and a linear model shows that there is always another fraction to be found between any two numbers" (2014, p. 207). It may be beneficial to plan and select students with two different models to share and compare.

Consider spending more than 1 day on a lesson. The need to spend more than 1 day on a lesson should be a balance of being learner responsive and pacing considerations; therefore, making a lesson a 2-day lesson may be different from class to class. As a result, an additional Solve \& Share for each lesson is offered. The Another Look videos could be used to fill-in for a Visual Learning Animation. Please note the intent is not that every lesson become a 2-day lesson, but rather, to provide a resource for when it is needed.

## Focus Math Practice 3: Construct viable arguments and critique the reasoning of others

Focus on opportunities for students to develop Mathematical Practice 3 behaviors throughout the entire topic, as this is the focus of the Math Practices and Problem Solving lesson 13-8. To support students' development of MP. 3 consider using some of the language as a regular part of instruction. Giving students directions that include phrases such as, "construct an argument" and "justify your conjecture" may help students build understanding of what MP. 3 entails. Additional resources include the Teacher's Edition (pp. F23-F23A) and the Nevada Academic Content Standards (NVACS) for Mathematical Practice.

|  | Essential Academic Vocabulary <br> Use these words consistently during instruction. |
| :--- | :--- |
| New Academic Vocabulary: <br> (First time explicity taught) | Review Academic Vocabulary: <br> (Vocabulary explicity taught in prior grades or topics) |
| equivalent fractions | fraction <br> *numerator <br> *denominator <br> greater than |
|  | less than |
| conjecture |  |

Additional terminology that students may need support with: compare, *Consider using the definition described in Topic 12 Curriculum Guide's Instructional note to avoid developing misconceptions.

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding question: "Are students finding equivalent fractions and comparing fractions based on the whole using multiple strategies?" (Fraction strips, number lines, models, benchmark fractions)

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $13-2$ | Quick Check (digital platform) | Focus CTC around data analysis and collection of student workspace <br> (scratch paper). Printable version available under "Teacher Resources". <br> $\bullet \quad$ ability to use a number line to identify equivalent fractions |
| $13-8$ | Math Practices and Problem Solving <br> (student work samples) <br> Items 7 and 9 | Focus CTC around the big idea: <br> $\bullet \quad$ student understanding of the whole (item 7) <br> constructing a math argument based on comparison of fractions (item 9) |


| Learning Cycle | Topic Assessments <br> SE pp. 727-732 | Use Scoring Guide TE pp. 727-732A |
| :---: | :--- | :--- |
| Assessments (summative) |  |  |

Standards listed in bold indicate a focus of the lesson.


|  |  | Assess and Differentiate: <br> If time permits, teach students how to play Display the Digit (TE, p. 677A). All students should have the opportunity to play this game as it provides engaging and meaningful practice of a key concept. <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 677A). <br> Possible Day 2 Solve \& Share: <br> (Read the Instructional note at the beginning of this topic for guidance on making a lesson more than 1 day.) Consider using items 9 and/or 10 from Math Practices and Problem Solving. |
| :---: | :---: | :---: |
| Lesson 13-2: Equivalent Fractions- Use the Number Line |  |  |
| 3.NF.A.3a <br> 3.NF.A.3b <br> MP. 3 <br> MP. 4 <br> MP. 5 | Access Prior Learning: <br> In Topic 12, Grade 3, students learned to represent fractions on number lines. In the previous lesson students learned about equivalent fractions. <br> Developing the Big Idea: Students further develop their understanding of equivalent fractions by finding that there are limitless number of fraction names for each point on a number line. <br> These points can be used to name equivalent fractions. | Solve \& Share: <br> A common misconception when working with number lines is for students to count the hash marks instead of the sections to name the fractions. Consider discussing "Drew's Work" (TE p. 679) to confront this misconception. <br> Since both the fraction strips (area) and number line (linear) models have been introduced, it may be beneficial to have a class discussion on how both models represent the same mathematics through their similarities and differences. <br> Look Back: <br> Consider wrapping up the class discussion of students' solutions and reasoning by discussing the Look Back! prompt. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider discussing item 8 as it offers an opportunity to discuss and develop understanding of equivalent names for 1. <br> Consider discussing item 12 MP. 3 Construct Arguments to support students' development of MP.3, and to develop schema for the next lesson. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Math and Science Activity with the game Display the Digit (TE, p. 677A) or the Fluency Practice Activity (TE, p. 721). <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 783A). <br> Possible Day 2 Solve \& Share: <br> (Read the Instructional Note at the beginning of this topic for guidance on making a lesson more than 1 day.) Consider using the Convince Me! <br> *CTC: Quick Check (digital platform) |
| Lesson 13-3: Use Models to Compare Fractions- Same Denominator |  |  |
| 3.NF.A.3d <br> MP. 2 <br> MP. 3 <br> MP. 5 <br> MP. 6 <br> MP. 8 | Access Prior Learning: <br> In previous lessons, students used fraction strips and number lines to find equivalent fractions. <br> Developing the Big Idea: <br> Students are further developing fractional sense by comparing fractions with the same denominator. <br> Students use quantitative reasoning to determine that when comparing fractions with the same denominator, the fraction with the greater numerator is the greater fraction. | Solve \& Share: <br> Consider reviewing the meaning of comparison symbols (<, >, and =) after introducing the Solve \& Share, to reinforce the significance of the whole when comparing fractions. Consider asking students if we have the same size whole (e.g., yes, the whole is 1 mile for both joggers) being compared. Then ask, "Can we compare if they were different size wholes (e.g., no because the wholes have to be the same size in order to compare)?" <br> Visual Learning: <br> Considering pausing and discussing after the question is posed, "Which is greater $4 / 6$ or $2 / 6$ ?". <br> Independent Practice/Math Practices and Problem Solving: <br> Consider discussing item 18 MP. 8 Generalize to begin to develop schema for the next lesson. <br> Assess and Differentiate: <br> If time permits, you consider teaching students how to play Tic Tac Toe (TE, p. 689A). All students should have the opportunity to play this game it provides engaging and meaningful practice of a key concept. <br> Possible Day 2 Solve \& Share: <br> (Read the Instructional note at the beginning of this topic for guidance on making a lesson more than 1 day.) Consider using item 17 from the Independent Practice/Math Practices and Problem Solving. |


| Lesson 13-4: Use Models to Compare Fraction- Same Numerator |  |  |
| :---: | :---: | :---: |
| 3.NF.A.3d <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 6 | Access Prior Learning: <br> In the previous lesson, students used fraction strips and pictorials to compare fractions with the same denominator. <br> Developing the Big Idea: <br> Students are further developing fractional sense by comparing fractions with the same numerator. <br> Students use quantitative reasoning to determine that when comparing fractions with the same numerator, the fraction with the greater denominator is less than the other fraction. | Convince Me: <br> Consider discussing the Convince Me! to support student's development of MP. 3 Construct Arguments, as well as, to extend the ideas covered in the Visual Learning Animation. <br> Independent Practice/Math Practices and Problem Solving: <br> Item 18 Higher Order Thinking from the Quick Check addresses a common misconception that results from students applying reasoning with whole numbers to rational numbers. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Math and Science Activity with the game Display the Digit (TE, p. 677A), Tic Tac Toe (TE, p. 689A), or the Fluency Practice Activity (TE, p. 721). <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 695A). <br> Possible Day 2 Solve \& Share: <br> (Read the Instructional note at the beginning of this topic for guidance on making a lesson more than 1 day.) Consider using item 15 from Math Practices and Problem Solving. |
| Lesson 13-6: Compare Fractions- Use the Number Line |  |  |
| 3.NF.A.3d <br> MP. 2 <br> MP. 3 <br> MP. 6 <br> MP. 7 | Access Prior Learning: <br> In lessons 13-1 through 13-4, students used quantitative reasoning and models to compare fractions with either the same numerator or the same denominator. Students have also represented fractions on a number line. <br> Developing the Big Idea: <br> Students further develop their fractional sense by comparing fractions using a number line. | Instructional note: <br> Lesson $13-6$ is recommended to be taught before 13-5, as it offers stronger visual representations for comparing fractions and establishing benchmark fractions, which will be explored further in $13-5$. Watch for students that are confusing the comparison symbols. Students may have understanding of which fraction is greater than or less than, but still have confusion about which symbol accurately communicates their relationship. Interview these students to determine if they understand the mathematics. <br> Look Back: <br> After students have shared their solution methods and reasoning, consider discussing the Look Back! <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Math and Science Activity with the game Display the Digit (TE, p. 677A), Tic Tac Toe (TE, p. 689A), Think Together (TE, p. 701A), or the Fluency Practice Activity (TE, p. 721). <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 707A). <br> Possible Day 2 Solve \& Share: <br> (Read the Instructional note at the beginning of this topic for guidance on making a lesson more than 1 day.) Consider using the Convince Me! |
| Lesson 13-5: Compare Fractions- Use Benchmarks |  |  |
| 3.NF.A.3d MP. 1 MP. 2 MP. 3 | Access Prior Learning: <br> In lessons 13-1 through 13-4, students used quantitative reasoning and models to compare fractions with either the same numerator or the same denominator. Students have also represented fractions on a number line. <br> Developing the Big Idea: Students are further developing fractional sense by comparing fractions using the benchmark fractions $0, \frac{1}{2}$, and 1 to reason the larger fraction. | Solve \& Share: <br> Consider discussing the Look Back! to support students' quantitative reasoning about fractions. <br> Visual Learning: <br> Consider assigning the Convince Me! to reinforce ideas shared in the Visual Learning Animation. <br> Assess and Differentiate: <br> If time permits, consider teaching students how to play Think Together (TE, p. 701A). All students should have an opportunity to play this game it provides engaging and meaningful practice of a key concept. <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 701A). <br> Possible Day 2 Solve \& Share: <br> (Read the Instructional Note at the beginning of this topic for guidance on making a lesson more than 1 day.) Consider using item 18 MP. 3 Critique Reasoning from the Independent Practice/Math Practices and Problem Solving. |


| Le | ns |  |
| :---: | :---: | :---: |
| 3.NF.A.3c <br> 3.NF.A.3a <br> MP. 2 <br> MP. 3 <br> MP. 7 | Access Prior Learning: In lesson 12-5, students represented fractions on a number line, including fractions greater than 1 . In lessons 131 and 13-2, students learned that when using fractions to name quantities, a quantity can have more than one equivalent fraction. <br> Developing the Big Idea: In this lesson, students are further developing their fractional sense by finding that whole numbers can be represented by many different fraction names. | Instructional note: <br> Consider making this a 2-day lesson as the Developing the Big Idea understanding in this lesson is critical for future grade level work with fractions and has much depth; especially when connecting these understandings to division concepts. <br> Solve \& Share: <br> Consider covering the given model so students are unable to see it and thus more inclined to represent the mathematics using tools, models or other representations that makes the most sense to them. <br> Visual Learning: <br> Consider pausing and informally assessing students' connections to Topic 12 and lesson 13-2 when the question is posed, "What are some equivalent fraction names for 1,2 , and 3 ? How do you know?" <br> After viewing the Visual Learning Animation consider asking students what is the difference between $\frac{1}{2}$ and $\frac{2}{1}$ and create a model to prove the difference. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Problem Solving Reading Mat with the game Display the Digit (TE, p. 677A), Tic Tac Toe (TE, p. 689A), Think Together (TE, p. 701A), or the Fluency Practice Activity (TE, p. 721). <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 713A). <br> Possible Day 2 Solve \& Share: <br> (Read the Instructional Note at the beginning of this topic for guidance on making a lesson more than 1 day.) Consider using items 18 Higher Order Thinking from the Homework \& Practice. |
| Lesson 13-8: Math Practices and Problem Solving- Construct Arguments |  |  |
| 3.NF.A.3b <br> 3.NF.A.3d <br> MP. 3 <br> MP. 1 <br> MP. 4 <br> MP. 5 <br> MP. 6 | Access Prior Learning: <br> In previous lessons, students have developed an understanding that when using fractions to name quantities, a quantity can have more than one equivalent fraction. <br> Developing the Big Idea: <br> Students are further developing their understanding of equivalent fractions and comparing fractions by constructing arguments to solve problems in real-world contexts. | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 3. Refer to the Math Practices and Problem Solving Handbook (TE, pp. F23-F23A, F29) for suggestions on how to develop, connect and assess this Math Practice. <br> Solve \& Share: <br> Consider reintroducing MP. 3 Thinking Habits (SE, p. F23) before introducing the Solve \& Share. Also consider using time students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP. 3 that are listed in the Math Practices and Problem Solving Handbook (TE, p. F23A). After discussing student solution methods and reasoning, have students self-score for the behaviors associated with this math practice. <br> Look Back: <br> After discussing students' solution methods and reasoning, consider discussing the Look Back! if these ideas did not already come out from the classroom discussion. <br> Visual Learning: <br> Consider pausing to discuss," Why are 2 number lines a good drawing to justify the conjecture?" and, "Is this a representation you might try to use? Why or why not?" <br> Assess and Differentiate: <br> If time permits, consider teaching students how to play the game Teamwork (TE, p. 719A). <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 719A). <br> *CTC: Math Practices and Problem Solving (student work samples) |

## References

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## - Grade 3 Topic 14: Solve Time, Capacity, and Mass Problems

Big Conceptual Idea: Measurement and Data (Measurement Part) (pp. 16-18)
Prior to instruction, view the Topic 14 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 733A-733F), the Topic Planner (pp.7331-733K), all 9 lessons, and the Topic Assessments (pp. 803-804A).

## Mathematical Background:

Read Topic 14 Cluster
Overview/Math Background
(TE, pp. 733A-733F)

## Topic Essential Question:

How can time, capacity, and mass be measured and found?
Reference Answering the Topic Essential Question (TE, pp. 799-800) for key elements of answers to the Essential Question.

The lesson map for this topic is as follows:

| $14-1$ | $14-2$ | $14-3$ | $14-4$ | $14-5$ | $14-6$ | $14-7$ | $14-8$ | $14-9$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

5 A/D/E days used strategically throughout the topic.

## Instructional note:

Topic 14's big idea is that some attributes of objects are measureable and can be quantified using

$33^{\text {rd }}$ Grade Curriculum
Pacing Framework:
Balanced Calendar unit amounts. In this topic students learn to solve a variety of problems involving measurement of such attributes as time, capacity (liquid volume), and mass. The Measurement Data (Measurement Part) progression document states that working problems with intervals of time, liquid volumes, and masses of objects supports, "the work done in multiplication and the mathematical practices of making sense of problems (SMP 1) and representing them with equations, drawings, or diagrams" (NVACS, 2010, SMP 4).

In Topic 14, students first investigate time by extending the second grade understanding from standard 2.MD.C.7, "Tell and write time from analog and digital clocks to the nearest five minutes, using a.m. and p.m." (NVACS, 2010). In third grade students, "Tell and write time to the nearest minute and measure time intervals in minutes and solve word problems involving addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram" (NVACS, 2010, 3.MD.A.1). In Topic 14, students will develop this understanding by finding that:

- Time can be measured using seconds, minutes, and hours. Lengths of time can be found by adding or subtracting time intervals.
- There is more than one way to write and tell time to the nearest minute. We can use analog clocks, digital clocks, words, numbers, and symbols to show and tell time as precisely as possible (TE, p. 740).
- When solving for elapsed time it is helpful to first count the number of elapsed hours and then the number of elapsed minutes (TE, p. 746). Sometimes the elapsed time is provided and students need to figure out the start or end time.
- The methods used to solve elapsed time questions are similar to those used to solve for other addition and subtraction problems (TE, p.752).

Another unit of measure that students will be exploring in Topic 14 is capacity. Capacity is the amount a container can hold measured in liquid units. To help students develop benchmark measurements in capacity and to make concepts more concrete, consider providing students with concrete experiences with measuring liquids. In Topic 14 students will be introduced to milliiters and liters as metric units for measuring capacity. Students may need support on the conventions of reading the markings in a 1-liter container or graduated cylinder. Again, consider introducing this with concrete models (e.g., graduated cylinders), if available, before having students read measurements from a pictorial representation. Measurement Data (Measurement Part) progression document states that:
"Compared to the work in area, volume introduces more complexity, not only in adding a third dimension and thus presenting a significant challenge to students' spatial structuring, but also in the materials whose volumes are measured. These materials may be solid or fluid, so their volumes are generally measured, e.g., "packing" a right rectangular prism with cubic units or "filling" a shape such as a right circular cylinder" (2012, p.19).

Finally, students will be exploring mass as a unit of measurement. Mass is the amount of matter in an object. Metric units for measuring mass include grams and kilograms. In this topic, students will develop understanding that knowing benchmark measurements of mass is helpful in estimating the mass of other objects. Students will also come to realize that one way to measure
the mass of an object is to use a pan balance and metric weights. Please note that the measure of mass is different from weight. Mass is a measurement of the amount of matter something contains, while weight is the measurement of the pull of gravity on an object.

While teaching this topic you may want to consider providing experiences and facilitating discussions that help students to develop benchmark measurements for the different units of measure explored. This is often accomplished by providing concrete learning experiences with the units of measure and comparing new units of measure to known measurements. For example, students that are comfortable with the size of a measuring cup can visually see how many milliliters are equivalent to the cup and then decide what others amounts would be appropriate to measure with milliliters. As much as possible, experiences with the following materials are recommended to facilitate students developing benchmark measurements:

- Pan balance
- Metric weights
- Gram weights
- Kilogram weights
- 1-Liter bottle
- Large bowls
- Eye dropper or pipette
- Gallon container
- Graduated cylinder
- 1-Liter beaker


## Focus Math Practice 2: Reason abstractly and quantitatively

The Nevada Academic Content Standards state that, "Mathematically proficient students make sense of quantities and their relationships in problem situations. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects" (NVACS, 2010, SMP 2). Focus on opportunities for students to develop Mathematical Practice 2 behaviors throughout the entire topic, as this is the focus of the Math Practices and Problem Solving lesson 14-9. Resources to support students' development of MP. 2 include the Teacher's Edition (pp. F22-F22A) and the Nevada Academic Content Standards for Mathematical Practice.

Looking ahead to the Topic Performance Assessment, students need select an appropriate units of measure and be able to use a number line to represent elapsed time.

|  | Essential Academic Vocabulary <br> Use these words consistently during instruction. |  |
| :--- | :--- | :---: |
| New Academic Vocabulary: <br> (First time explicity taught) | Review Academic Vocabulary: |  |
| time interval | (Vocabulayy explicitly taught in prior grades or topics) |  |

Additional terminology that students may need support with: clock face, nearest, past, volume, abbreviations

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding questions: "Are students able to determine the elapsed time?"
"Are students able to use their knowledge of operations to solve real world mass and liquid volume problems?

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $14-2$ | Quick Check (digital platform) | Focus CTC around data analysis and collection of student workspace <br> (scratch paper). Printable version available under "Teacher Resources". <br> $\bullet$ students understand time as a measurement (elapsed time). |
| $14-8$ | Solve \& Share (student work samples) | Focus CTC around the big idea: <br> $\bullet$ student strategies and models. <br> use of operational knowledge to solve mass and/or liquid volume <br> problems |


| Learning Cycle | Topic Assessments <br> SE pp. 799-804 | Use Scoring Guide TE pp. 799-804A |
| :---: | :--- | :--- |
| Assessments (summative) |  |  |

Standards listed in bold indicate a focus of the lesson.

| NVACS <br> (Content and Practices) | Mathematical Development of the Big Idea | Instructional Clarifications \& Considerations |
| :---: | :---: | :---: |
| Lesson 14-1: Time to the Minute |  |  |
| 3.MD.A. 1 <br> MP. 3 <br> MP. 4 <br> MP. 5 <br> MP. 6 | Access Prior Learning: In Topic 8, Grade 2, students learned to tell time to the nearest 5 minutes. In Topic 2, Grade 3, students learned about patterns with 5 as a factor. <br> Developing the Big Idea: Students are further developing time concepts by applying their knowledge of counting by 5 s and 1s to tell time to the nearest minute. | Topic Opener: <br> Introduce the Topic Essential Question, "How can time, capacity, and mass be measured and found?". Consider using this question to begin a class anchor chart to which new ideas can be added each day. This allows students to see the development of their own thinking and ideas and make new connections with the content of this topic. <br> Consider having students complete the Review What You Know prior to beginning instruction on Topic 14 so that you can respond to students' instructional needs using the Item Analysis for Diagnosis and Intervention (TE, p. 734). <br> Consider introducing vocabulary terms as they are encountered in the lessons rather than introducing all terms at the beginning of the topic. <br> Solve \& Share: <br> Consider having tools readily available for students to use such as clocks or Teaching Tool 20. Watch for students who struggle to begin the Solve \& Share. Ask students what the tic marks on the clock represent to help them connect to the work they did in $2^{\text {nd }}$ grade. <br> Consider having students share their solution methods and reasoning that match the samples provided. Both Jasmin \& Timothy's work correctly marks the minutes; however, only Jasmin's work accurately notes where the hour hand would be for the given time. Showing both of these solution methods provides the opportunity to discuss movement of the hour hand. <br> Consider wrapping up the whole class discussion by asking students how they can tell time to the nearest minute. The Visual Learning Animation can then be used to confirm, clarify or correct students' ideas. <br> Visual Learning: <br> Consider pausing and discussing after it poses the question, "Why is an analog clock a good tool for showing time to the nearest minute?" Use tools to have students show time in different ways. For example, contrasting the difference between digital and analog time. <br> Assess and Differentiate: <br> If time permits, teach students how to play Display the Digit (TE, p. 743A). All students should have the opportunity to play this game. <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 743A). |



|  |  | Look Back: <br> After students have shared their solution methods and reasoning, consider discussing the Look Back! prompt. <br> Visual Learning: <br> Consider discussing the ideas provided in the Prevent Misconceptions section (TE, p. 758) during the Visual Learning Animation. <br> Convince Me: <br> To support students' development of MP. 2 consider discussing the Convince Me! prompt. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider discussing item 18 to help students develop familiarity with liters (L) and milliliters $(\mathrm{mL})$ to be able to select the appropriate unit of measure for the items listed. <br> Assess and Differentiate: <br> If time permits, teach students how to play Toss and Talk (TE, p. 761A). All students should have the opportunity to play this game. <br> Child watch to identify students who need additional support and pull them in a small group to do the Intervention Activity (TE, p. 761A). |
| :---: | :---: | :---: |
| Lesson 14-5: Measure Liquid Volume |  |  |
| 3.MD.A. 2 <br> MP. 3 <br> MP. 4 <br> MP. 5 <br> MP. 6 <br> MP. 8 | Access Prior Learning: <br> In the previous lesson students developed benchmarks to estimate capacity (liquid volume) in $L$ and mL . <br> Developing the Big Idea: <br> Students further develop an understanding of estimation and units of measure by using standard units, liters ( L ) and milliliters ( mL ), to estimate capacity (liquid volume). | Instructional note: <br> A marked 1-liter beaker and 6 containers are necessary to complete the Solve \& Share and to help students develop benchmark measurements. <br> Look Back: <br> Consider discussing the Look Back! to support students' problem solving and appropriate use of mathematical tools after students have had an opportunity to work on the Solve \& Share. <br> Visual Learning: <br> Consider pausing and discussing the following questions from the Visual Learning Animation: <br> - "How can he find the capacity of the fish bowl?" <br> - "What does the abbreviation mL mean?" <br> - "How many mL are represented by each little mark on the 1 -Liter container?" <br> - "If the top mark were labelled in mL , what would it say?" <br> Convince Me: <br> Consider discussing the Convince Me! to support students' development of benchmark measurements and choosing an appropriate unit of measure. <br> Assess and Differentiate: <br> If time permits, consider teaching students how to play Teamwork (TE, p. 767A). All students should have an opportunity to play this game. <br> Based upon child-watching, identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 767A). |
| Lesson 14-6: Estimate Mass |  |  |
| $\begin{gathered} \text { 3.MD.A. } 2 \\ \text { MP. } 2 \\ \text { MP. } 3 \\ \text { MP. } 4 \\ \text { MP. } 5 \end{gathered}$ | Access Prior Learning: <br> In Topic 8, Grade 3, students learned to estimate sums and differences. Students have also applied estimation skills to measurement throughout this topic. <br> Developing the Big Idea: <br> Students further develop an understanding of units of measure by finding that mass is a measure of the quantity of matter in an object. <br> Students also further develop understanding of units of measure by estimating mass measurements in grams and kilograms. | Instructional note: <br> If available, have a pan balance, gram, and kilogram weights to help students develop benchmark measurements. <br> To support students' understanding of mass and their development of MP. 6, "Attend to precision" watch for students that confuse weight and mass. Consider correcting inaccurate language of describing an object as "weighing" some amount by providing the language "has the mass of" to describe the object. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Math and Science Activity with the game Display the Digit (TE, p. 743A), Clip and Cover (TE, p. 749A), Toss and Talk (TE, p. 761A), Teamwork (TE, p. 767A), or the Fluency Practice Activity (TE, p. 793). <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 773A). |


| Lesson 14-7: Measure Mass |  |  |
| :---: | :---: | :---: |
| 3.MD.A. 2 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 6 <br> MP. 7 | Access Prior Learning: <br> In the previous lesson, students learned about estimating mass. <br> Developing the Big Idea: <br> Students further develop understanding of estimation and units of measure by using standard units, grams ( g ) and kilograms $(\mathrm{Kg})$, to estimate mass. | Instructional note: <br>  <br> Share and to help students develop benchmark measurements. <br> Look Back: <br> After student solution methods and reasoning have been shared, consider using the Look Back! to facilitate a class discussion. <br> Convince Me: <br> To support students' reasoning with the appropriate unit of measure, consider discussing the Convince Me! <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Problem Solving Reading Mat with the game Display the Digit (TE, p. 743A), Clip and Cover (TE, p. 749A), Toss and Talk (TE, p. 761A), Teamwork (TE, p. 767A), or the Fluency Practice Activity (TE, p. 793). <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 779A). |
| Lesson 14-8: Solve Word Problems Involving Mass and Liquid Volume |  |  |
| $\begin{gathered} \text { 3.MD.A. } 2 \\ \text { MP. } 1 \\ \text { MP. } 2 \\ \text { MP. } 4 \\ \text { MP. } 6 \end{gathered}$ | Access Prior Learning: In previous lessons in this topic, students have estimated and measured for capacity and mass. <br> Developing the Big Idea: In this lesson, students are developing an understanding of measuring capacity and mass by using all four operations to solve problems. | Visual Learning: <br> During the Visual Learning Animation, consider doing the Try It! activity as this connects the context of the problem to the visual representations and model. After the Try Itt, the Visual Learning Animation makes the connections between the context and the bar diagram explicit. Consider pausing the video after it shows the connections to discuss what is known and unknown, what operation is needed to solve, and how to complete the bar diagram. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 9 to provide students distributed practice with elapsed time. <br> On Quick Check item 12 Common Core Assessment, watch for students that have incorrect responses as a result of struggling to read the pictorial representations of the containers. <br> Assess and Differentiate: <br> If time permits, consider teaching students how to play Teamwork (TE, p. 785A). All students should have an opportunity to play this game. <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 785A). <br> *CTC: Solve \& Share (student work samples) |
| Lesson 14-9: Math Practices and Problem Solving- Reasoning |  |  |
| 3.MD.A. 1 <br> MP. 2 <br> MP. 1 <br> MP. 3 <br> MP. 4 <br> MP. 6 <br> MP. 8 | Access Prior Learning: In previous lessons, students solved problems involving time. <br> Developing the Big Idea: Students are developing the understanding of elapsed time by making sense of the quantities and relationships to solve problems in real-world contexts. | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 2. Refer to the Math Practices and Problem Solving Handbook for suggestions on how to develop, connect and assess this Math Practice (TE, pp. F22-F22A, F29). Also reference the handbook in the Student Edition (SE, p. F22). <br> Solve \& Share: <br> Consider reintroducing MP. 2 Thinking Habits (SE, p. F22) before introducing the Solve \& Share. Also consider using the time students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP. 2 that are listed in the Math Practices and Problem Solving Handbook (TE, p. F22A). After discussing student solution methods and reasoning, have students self-score for the behaviors associated with this math practice. <br> Look Back: <br> After discussing students' solution methods and reasoning, consider discussing the Look Back! prompt to support students understanding of when a time when be the answer versus minutes being the answer to elapsed time problems. <br> Convince Me: <br> To support students' development of MP. 2, consider discussing the Convince Me! prompt. |


|  |  | Assess and Differentiate <br> If time permits, you may consider replacing the Math and Science Activity with the game <br> Display the Digit (TE, p. 743A), Clip and Cover (TE, p. 749A), Toss and Talk (TE, p. 761A), <br> Teamwork (TE, p. 767A), Teamwork (TE, p. 785A), or the Fluency Practice Activity (TE, p. 793). |
| :--- | :--- | :--- |
|  | Child watch to identify students who need additional support and pull them into a small group to <br> do the Intervention Activity (TE, p. 791A). |  |

## References

Common Core Standards Writing Team. (2013). Progressions for the Common Core State Standards in Mathematics (draft). K-5, Measurement and data-Measurement. Tucson, AZ: Institute for Mathematics and Education, University of Arizona.

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## - Grade 3 Topic 16: Solve Perimeter Problems

Big Conceptual Idea: Measurement and Data (Measurement Part) (pp. 16-18)
Prior to instruction, view the Topic 16 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 843A-843F), the Topic Planner (pp.8431-843J), all 6 lessons, and the Topic Performance Assessment (pp. 889-890A).

| Mathematical | Topic Essential Question: |
| :--- | :--- |
| Background: |  |
| Read Topic 16 Cluster |  |
| Overview/Math Background |  |
| (TE, pp. 843A-843F) |  |$\quad$| Reference Answering the Topic Essential Question (TE, pp. 887-888) for key elements of |
| :--- |
| answers to the Essential Question. |

## The lesson map for this topic is as follows:

| $16-1$ | $16-2$ | $16-3$ | $16-4$ | $16-5$ | $16-6$ | Assessment |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

4 A/D/E days used strategically throughout the topic.

## Instructional note:

Topic 16's big idea is that some attributes of objects are measurable and can be quantified using units. New learning to this topic is perimeter as a measurable unit, while developing a deeper understanding of area through exploring the relationship between area and perimeter.

$3^{\text {rd }}$ Grade Curriculum
Pacing Framework:
Balanced Calendar

Perimeter as defined by the Geometric Measurement progression document, "is the boundary of a two-dimensional shape. For a polygon, the length of the perimeter is the sum of the lengths of the sides" (2012, p.16). Students begin to develop understanding of perimeter concepts by finding the perimeter of polygons on a grid. A common misconception when determining the perimeter of shapes on a grid is to count the vertices rather than the unit segments. In such cases, support students by clarifying what/how to count the unit segments to determine the side lengths. See the Math Background pages for information regarding this.

Students further develop understanding of perimeter concepts by determining the perimeter of parallelograms when only 2 lengths of adjacent sides are provided. Students may choose to solve by doubling each side's length and adding them together or by adding the adjacent sides' measures and doubling. A common error in these cases is for students to only add the 2 side lengths where the measures are given. In this event, revisit the definition of perimeter and ask students what sides they have found the total length for and what they need to find to get the perimeter of the shape.

In the case where a parallelogram is a square, only 1 side's length may be offered and students will have to reason with what they know about attributes of squares to determine the perimeter of a square. In this case students may choose to add the measure 4 times (repeated addition), double the measure and double it again (a strategy for solve for multiplication facts with 4 as a factor), or multiply the length of the one side times 4 (or 4 times). To connect to previous learning this year, and to revisit understandings of grade 3 critical content area of multiplication, it may be a worthy class discussion on these 3 different solution strategies and why they all work and in what situations or context one may work better than another.

Students also develop understanding of perimeter concepts by exploring how to find perimeter when they have to solve for an unknown side length of polygons. Initially enVisionmath2.0 represents the unknown side length with a question mark (?); however, further in the lesson it is represented with a variable and the unit of measurement. For example, if side lengths were measured in centimeters they identify the unknown side length as " $x \mathrm{~cm}$." This connects with standard 3.OA.D.8, "Solve 2 -step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity" (NVACS, 2010). You may need to clarify the difference between the letter for the unknown and the letters for the abbreviated unit of measurement.

Students also explore the relationship between area and perimeter. Students often confuse perimeter and area measures. The Geometric Measurement progression document states that, "Differentiating perimeter from area is facilitated by having students draw congruent rectangles and measure, mark off, and label the unit lengths all around the perimeter on one rectangle, then do the same on the other rectangle but also draw the square units. This enables students to see the units involved in length and area and find patterns in finding the lengths and areas of non-square and square rectangles (MP 7)" (2012, p. 18). Chapin and Johnson (2006) suggest asking the following questions to facilitate students developing understanding of the relationship between area and perimeter:

- What do all the figures with smaller perimeters have in common?
- The figures with smaller perimeters are more condensed and compact.
- The shape of these figures is more closely related to a square.
- What do all the figures with large perimeters have in common?
- The figures with larger perimeters are elongated. Most of the square tiles are adjacent to another square tile only on one side (p.284-285).

Students do not need to be secure in the responses to these questions, the questions just help to identify that there is a relationship between perimeter and area.

## Focus Math Practice 2: Reason abstractly and quantitatively

Focus opportunities for students to develop Mathematical Practice 2 behaviors throughout the entire topic, as this is the focus of the Math Practices and Problem Solving lesson 16-6. Resources to support students' development of MP. 2 include the Teacher's Edition (pp. F22 - F22A) and the Nevada Academic Content Standards for Mathematical Practice. The Nevada Academic Content Standards state that, "Mathematically proficient students make sense of quantities and their relationships in problem situations. ... Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects" (2010, SMP 2).

| Essential Academic Vocabulary <br> Use these words consistently during instruction. |  |  |  |
| :--- | :--- | :---: | :---: |
| New Academic Vocabulary: <br> (First time explicitly taught) | Review Academic Vocabulary: <br> (vocabulary explicitly taught in prior grades or topics) |  |  |
| perimeter <br> equilateral triangle | ara <br> square units |  |  |

Additional terminology that students may need support with: grid, distance, around, representations,
*Collaborative Team Conversations (CTC)
Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding questions: "Are students showing understanding that rectangles can have the same area and different perimeters?" "Are students able to explain the relationship between area and perimeter using rectangles with the same area and different perimeters?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $16-2$ | Quick Check (digital platform) | Focus CTC around data analysis and collection of student workspace <br> (scratch paper). Printable version available under "Teacher Resources". <br> $\bullet \quad$ using given measurements to determine the perimeter of a polygon. |
| $16-5$ | Solve \& Share (student work samples) | Focus CTC around the big idea: <br> $\bullet \quad$comparing the relationship between the area and perimeter of <br> rectangles. |


| Learning Cycle Assessments (summative) | Topic Assessments SE pp. 887-890 | Use Scoring Guide TE pp. 887-890A |
| :---: | :---: | :---: |

Standards listed in bold indicate a focus of the lesson.

| NVACS <br> (Content and Practices) | Mathematical Development of the Big Idea | Instructional Clarifications \& Considerations |
| :---: | :---: | :---: |
| Lesson 16-1: Understand Perimeter |  |  |
| $\begin{gathered} \text { 3.MD.D. } 8 \\ \text { MP. } 1 \\ \text { MP. } 2 \\ \text { MP. } 3 \\ \text { MP. } 4 \\ \text { MP. } 6 \end{gathered}$ | Access Prior Learning: In Topic 6, Grade 3, students learned how to find area using standard, as well as nonstandard, units of measurement. Students also learned how to count unit squares to determine side length. <br> Developing the Big Idea: <br> Students begin to understand perimeter as the distance around a figure and solve for perimeter. | Topic Opener: <br> Introduce the Topic Essential Question, "How can perimeter be measured and found?" (TE p. 843). Consider using this question to begin a class anchor chart to which new ideas can be added each day. This allows students to see the development of their own thinking and ideas and make new connections with the content of this topic. <br> Consider having students complete the Review What You Know prior to beginning instruction on Topic 16 so that you can respond to students' instructional needs using the Item Analysis for Diagnosis and Intervention (TE, pp. 844-846). Consider introducing vocabulary terms as they are encountered in the lessons rather than introducing all terms at the beginning of the topic. <br> Solve \& Share: <br> Watch for students that count vertices rather than the unit segments. For ideas on supporting students that are miscounting the unit segments read Prevent Misconceptions (TE, p. 848). <br> -continues on next page- |


|  |  | Visual Learning: <br> Consider pausing the Visual Learning Animation after it asks, "How do you find the perimeter?" The Visual Learning Animation introduces finding perimeter using side measurements without the grid. Consider asking students "How does removing the grid lines change finding the perimeter?" <br> Convince Me: <br> Consider assigning the Convince Me! to support students' development of perimeter measurements. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning Homework and Practice item 8 to give students the opportunity to create a polygon using a given perimeter measurement. <br> Assess and Differentiate: <br> If time permits, you may consider using the Math and Science Activity. <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 851A). |
| :---: | :---: | :---: |
| Lesson 16-2: Perimeter of Common Shapes |  |  |
| 3.MD.D. 8 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 6 <br> MP. 7 <br> MP. 8 | Access Prior Learning: <br> In Topic 15, Grade 3, students learned about sides of polygons as being attributes of polygons. In the previous lesson, students found the perimeter of polygons by counting the unit segments around a figure or adding all the sides' measurements. <br> Developing the Big Idea: <br> Students develop perimeter concepts by using reasoning and their knowledge of attributes of polygons, to finding the perimeter of figures with missing side lengths. | Solve \& Share: <br> Watch for students that appear to be struggling, help them to apply knowledge of the attributes of rectangles. Support students' problem solving by asking them what they know about rectangles (e.g., opposites sides are the same length, 2 pair of parallel sides, 4 right angles, etc.). Then ask them which of those attributes could help them figure out the perimeter of the rectangle (e.g., opposites sides are the same length). <br> After students have shared their solution methods and reasoning, consider discussing the Look Back! to help students focus on how they can use multiplication and addition to find perimeter. <br> Visual Learning: <br> After the Visual Learning Animation show how repeated addition can be used to solve for the perimeter of a square. Consider asking, "Is there another way to solve for the perimeter of squares?" Are students connecting using repeated addition to multiplication to find perimeter? <br> Assess and Differentiate: <br> If time permits, teach students how to play Clip and Cover (TE, p. 857A). All students should have the opportunity to play this game. <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 857A). <br> *CTC: Quick Check (digital platform) |
| Lesson 16-3: Perimeter and Unknown Side Lengths |  |  |
| 3.MD.D. 8 <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 7 | Access Prior Learning: <br> In the previous lessons, students solved for perimeter by using attributes of regular polygons where some of the side lengths were not labelled. <br> Developing the Big Idea: Students are further developing perimeter concepts by solving for a missing side length in a polygon with a given perimeter. | Solve \& Share: <br> Watch for students that incorrectly determine the unknown side as 3 ft . They are likely applying reasoning based on understanding rectangles. Remind students what is known and unknown in this problem. Can they write an equation that represents the known sides, the unknown side (use a variable) and perimeter? How does this expression help to determine the missing side length? Are students able to use an inverse operation to check their solution? <br> Visual Learning: <br> During the Visual Learning Animation consider pausing to allow students to solve for $x$ in the equation $x+18=22$. Are they able to use more than one operation to find the value of $x$ ? <br> Assess and Differentiate: <br> If time permits, consider having student play Clip and Cover (TE, p. 857A) or the Fluency Practice Activity (TE p. 883). <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 863A). |
| Lesson 16-4: Same Perimeter, Different Area |  |  |
| $\begin{gathered} \text { 3.MD.D. } 8 \\ \text { 3.MD.C.7b } \end{gathered}$ <br> MP. 1 | Access Prior Learning: In previous lessons, students found the perimeter of polygons, in some cases, with an unknown side length. | Solve \& Share: <br> To assess student readiness, consider asking students, "What is the difference between perimeter and area?" Are students able to describe area as the measure of space inside a figure and perimeter as the measure of the distance around a figure. Also consider asking students "What is the same?" to remind them that both are measurements. Adding these ideas to the class anchor chart will allow students to revisit these concepts in future lessons. -continues on next page- |


| MP. 2 <br> MP. 3 <br> MP. 6 <br> MP. 7 <br> MP. 8 | Developing the Big Idea: Students further develop perimeter and area concepts by using what they know about perimeter and rectangles to discover that polygons with the same perimeter can have different areas. | After students have shared their solution methods and reasoning, use the Look Back! to extend thinking about the relationship between perimeter and area. <br> Visual Learning: <br> Consider pausing the Visual Learning Animation and giving students time to solve for the area of the shapes. Prevent Misconceptions section (TE, p. 866) suggests checking to be sure that students understand how to find perimeter and area. Can students generalize how side length is related to area? Also, consider discussing the Convince Me! to extend upon ideas presented in the Visual Learning Animation. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning Math Practices and Problem Solving item18 to provide students distributed practice with a division situation. <br> Assess and Differentiate: <br> If time permits, teach students how to play Teamwork (TE, p. 869A). All students should have the opportunity to play this game. <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 869A). |
| :---: | :---: | :---: |
| Lesson 16-5: Same Area, Different Perimeter |  |  |
| 3.MD.D. 8 <br> 3.MD.C.7b <br> MP. 1 <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 5 <br> MP. 7 <br> MP. 8 | Access Prior Learning: <br> In the previous lesson, students discovered that different rectangles can have the same perimeter and different areas. <br> Developing the Big Idea: Students further develop perimeter and area concepts by using what they know about area and rectangles to discover that polygons with the same area can have different perimeters. | Solve \& Share: <br> Prior to introducing the Solve \& Share consider having centimeter grid paper (Teacher Tool 13) and colored tiles available. After introducing the Solve \& Share, ask students what tool might be helpful in solving the problem. <br> After students have shared their solution methods and reasoning, consider discussing the Look Back! if the relationship between area and perimeter was not yet discussed. <br> Visual Learning: <br> Consider pausing and discussing the Visual Learning Animation after it asks the question, "Why do the water tiles surround this rectangle?" <br> Convince Me: <br> Consider discussing the Convince Me! to support students' development with choosing the appropriate unit of measure (linear vs. square units). <br> Assess and Differentiate: <br> If time permits, consider using the Math and Science Activity, games Clip and Cover (TE, p. 857A), Teamwork (TE, p. 869A), or the Fluency Practice Activity (TE, p. 883). <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 875A). <br> *CTC: Solve and Share (student work samples) |
| Lesson 16-6: Math Practices and Problem Solving- Reasoning |  |  |
| 3.MD.D. 8 <br> MP. 2 <br> MP. 1 <br> MP. 3 <br> MP. 6 <br> MP. 7 | Access Prior Learning: In previous lessons, students developed perimeter concepts and learned about the relationship between perimeter and area. <br> Developing the Big Idea: <br> Students are developing understanding of perimeter concepts by focusing on MP. 2 to understand the relationship between numbers in order to simplify and solve problems involving perimeter. | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 2. Refer to the Math Practices and Problem Solving Handbook for suggestions on how to develop, connect and assess this Math Practice (TE, pp. F22-F22A, F29). Also reference the handbook in the Student Edition (SE, p. F22). <br> Solve \& Share: <br> Consider reintroducing MP. 2 Thinking Habits (SE, p. F22) before introducing the Solve \& Share. Also consider using the time students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP. 2 that are listed in the Math Practices and Problem Solving Handbook (TE, p. F22A). After discussing student solution methods and reasoning, have students self-score for the behaviors associated with this math practice. <br> Visual Learning: <br> To support students' development of MP. 2, consider discussing the Convince Me! prompt. <br> Assess and Differentiate: <br> If time permits, you consider replacing the Problem Solving Reading Mat with the games "Clip and Cover (TE, p. 857A), Teamwork (TE, p. 869A), or the Fluency Practice Activity (TE, p. 883). <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 881A). |

## References

Chapin, S. H., \& Johnson, A. (2006). Math matters: Understanding the math you teach, Grades K-8. Sausalito, CA: Math Solutions Publications.

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## - Grade 3 Topic 15: Attributes of Two-Dimensional Shapes

Big Conceptual Idea: K-6, Geometry (pp. 13-14)
Prior to instruction, view the Topic 15 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 805A-805F), the Topic Planner (pp.8051-805J), all 4 lessons, and the Topic Assessments (pp. 841-842A).

| Mathematical |
| :--- |
| Background: |
| Read Topic 15 Cluster |
| Overview/Math Background |
| (TE, pp. 805A-805F) |

## Topic Essential Question:

How can two-dimensional shapes be described, analyzed, and classified?

Reference Answering the Topic Essential Question (TE, pp. 839-840) for key elements of answers to the Essential Question.

## The lesson map for this Topic is as follows:

\section*{| $15-1$ | $15-2$ | $15-3$ | $15-4$ | Assessment |
| :---: | :---: | :---: | :---: | :---: |}

7 A/D/E days used strategically throughout the topic includes the "enrichment" lessons.

$3^{\text {rd }}$ Grade Curriculum
Pacing Framework:
Balanced Calendar

## Instructional note:

Topic 15 's big idea is that two-dimensional shapes can be described, analyzed, and classified based on their attributes. Students learn to analyze a variety of geometric shapes and begin to explore relationships between the shapes based on their attributes. The Geometry progression document (2014) describes attributes as, "any characteristic of a shape, including properties, and other defining features (e.g., straight sides) and non-defining features (e.g., "right-side up")" (p. 3).
Much of what makes this standard a struggle for students is the vocabulary and hierarchical inclusion of geometric shapes (any shape in a sub category is also a member of the larger category; yet a shape of a larger category may or may not be part of particular sub categories).

Geometric hierarchy is the idea that, "Shapes have many attributes that make them similar to and different from one another. You can describe and classify different groups of shapes by their attributes" (TE, p. 818). This means that a shape can fall into many different groups when being classified. For example, when classifying a square, a square meets the requirements of being a polygon, quadrilateral, rectangle, parallelogram, and a rhombus. However, a rectangle and a rhombus are not necessarily squares.


Note that rhomboids are parallelograms that are not rhombuses or rectangles. This example uses the inclusive definition of trapezoid (see p. [pageref "T(E)"])].

To illustrate this idea, please see the image to the right from page 18 of the K-6, Geometry progression document (2014). Additional A/D/E days allow instructional time for tasks that build understanding of the idea that shapes can be classified into a group that is part of another group. Include non-examples to help students establish limitations to categories.

Vocabulary becomes an important component of recognizing and classifying shapes by their attributes. This can be illustrated by the example of classifying a square which moves through several subcategories and also retains the attributes and names from those subcategories. For example, to be labeled a square, students have to recall that the shape must also meet all of the following criteria:

- be a polygon (and the all the attributes for a polygon)
- have four sides
- have 2 pairs of parallel sides
- all sides are the same length
- all angles are the same size

Students who have had limited experiences with working with geometric ideas in previous grades may need additional language support. Consider using the graphic organizers from Teaching Tools 24 through 28 found in the Teacher's Resource Masters Volume 2 to support language acquisition and use. Anchor charts, cognitive content dictionaries or personal word walls in addition to writing and reasoning tasks will support students in use of the academic language needed to explore these ideas.

A common misconception that students will form is that a shape is only that shape when presented in its prototypical orientation. For example, the first trapezoid below is shown in its prototypical orientation, while the second trapezoid is shown a non-prototypical orientation.


To avoid this misconception, provide many opportunities for students to reason with polygons in multiple orientations and name polygons based on evidence of the atributes stated in the shape's definition.

There are two different definitions for a trapezoid, an inclusive and exclusive definition. Per the Geometry progression document (2014) the inclusive definition of a trapezoid states that, "a trapezoid is a quadrilateral with at least one pair of parallel sides" (p.3). Therefore, in the inclusive definition, a trapezoid would fit into the sub-category of parallelograms. In the Geometry progression document (2014) the exclusive definition of a trapezoid states that, "a trapezoid is a quadrilateral with exactly one pair of parallel sides" (p.3). Therefore, in the exclusive definition, a trapezoid would not fit into the sub-category of parallelograms. There is no harm in students being made aware of the two different definitions. However, enVisionmath2.0 and WCSD use the exclusive definition (KAlgebra 1).

The WCSD $3^{\text {rd }}$ Grade Pacing Framework allows an additional 7 days of lessons to explore geometric ideas and build a solid understanding that will be necessary for students as they progress through the grade levels. To assist in building strong conceptual development and support learner responsive instruction, additional "Enrichment" lessons are included throughout the topic. More ideas are found at the conclusion of this document.

## Focus Math Practice 6: Attend to precision

Focus on opportunities for students to develop Mathematical Practice 6 behaviors throughout the entire topic, as this is the focus of the Math Practices and Problem Solving lesson 15-4. Resources to support students' development of MP. 6 include the Teacher's Edition (pp. F26-F26A) and the Nevada Academic Content Standards for Mathematical Practice.

Looking ahead to the Topic Performance Assessment, students need to be familiar with the attributes of two-dimensional figures and be able to identify shared attributes among grouped two-dimensional figures. Develop thinking habits that allow students to engage in these types of problems through encouraging discussions, deliberations and debates while having students work with these ideas in triads (groups of 3).

|  | Essential Academic Vocabulary <br> Use these words consistently during instruction. |  |
| :--- | :--- | :--- |
| New Academic Vocabulary: |  | Review Academic Vocabulary: <br> (First time explicity taught) |
| polygon | (Vocabulary explicitly taught in prior grades or topics) |  |
| side | parallelogram | lircle |
| quadrilateral | rectangle | hexagon |
| angle | right angle | pentagon |
| vertex | rhombus | triangle |
| trapezoid | square | rhombus |
| parallel sides | convex | rectangle |

Additional terminology that students may need support with: attributes, alike, different, square angle

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding questions: "Are students able to classify and analyze quadrilaterals based on their attributes?"

| Lesson | Evidence | Look for |
| :---: | :--- | :--- |
| $15-3$ | Quick Check (digital platform) | Focus CTC around data analysis and collection of student workspace <br> (scratch paper). Printable version available under "Teacher Resources". <br> students are able to analyze and compare quadrilaterals based on their <br> attributes. |
| $15-4$ | Convince me! (student work samples) | Focus CTC around the big idea: <br> $\bullet \quad$ construct shapes within given parameters. |


| Learning Cycle | Topic Assessments |
| :---: | :--- | :--- |
| SE pp. 839-842 |  |$\quad$ Use Scoring Guide TE pp. 839-842A

Standards listed in bold indicate a focus of the lesson.

| NVACS <br> (Content and Practices) | Mathematical Development of the Big Idea | Instructional Clarifications \& Considerations |
| :---: | :---: | :---: |
| Optional Enrichment |  |  |
| 3.G.A. 1 <br> MP. 1 <br> MP. 3 <br> MP. 6 <br> MP. 7 | Access Prior Learning: In Topic 15, Grade 2, students learned about polygons and angles. Students have been working with prototypical and nonprototypical shapes and defining attributes since pre-K or Kindergarten. <br> Developing the Big Idea: Students further develop geometric concepts by identifying common attributes amongst shapes (both defining and non-defining). | Materials: <br> Attribute Blocks (these may be checked out from the UNR LRC) <br> Shape clues (attributes of various shapes that may fall in various subcategories). <br> Opener: Students work in triads to create an attribute train. One player starts by picking a block. The next player must pick a block that is different in only one way. The difference can be shape, size, thickness or color. The triad keeps taking turns building their train and checking that each car is different in only one way. Once all blocks have been placed rotate the triads so that one triad checks another triad's train for accuracy. Play again, this time choose blocks that change in all but one attribute. That means that cars that touch must have only one attribute in common. <br> Whole Group Discussion: After the second version of the game has been played, choose one group's work to discuss whole group. Consider using a fishbowl strategy to explore the train. Highlight attributes of shapes. <br> Extend attribute thinking by giving students clues (attributes of a shape) and having them draw the shape (2 ${ }^{\text {nd }}$ grade standard). Example: I have four equal sides and four equal corners (this could be a square or a rhombus). Purposely choose attributes that could be used to make shapes that may fit more than one category. See "Polygons on the Geoboard" at the end of this guide for clue ideas. Encourage children to visualize or mentally construct the shape as they are drawing the shape. <br> Create an anchor chart that lists the attributes of triangles, quadrilaterals, pentagons and hexagons (2 ${ }^{\text {nd }}$ grade standard). Add on to this chart throughout the topic starting with 15-1. <br> Note: "Distinguish between defining atributes (e.g., triangles are closed and three-sided) versus non-defining attributes (e.g., color, orientation, overall size); build and draw shapes to possess defining attributes" (1 ${ }^{\text {st }}$ grade NVAC, 1.G.A.1). |
| Lesson 15-1: Describe Quadrilaterals |  |  |
| 3.G.A. 1 <br> MP. 1 <br> MP. 3 <br> MP. 4 <br> MP. 6 <br> MP. 7 <br> MP. 8 | Access Prior Learning: In Topic 15, Grade 2, students learned about polygons and angles. Students have been working with prototypical and nonprototypical shapes and defining attributes since pre-K or Kindergarten. <br> Developing the Big Idea: <br> Students further develop geometric concepts by describing and classify | Topic Opener: Introduce the Topic Essential Question, "How can two-dimensional shapes be described, analyzed, and classified?" (TE p. 805). Consider making an anchor chart highlighting key ideas so that students can see the conceptual development and connections throughout the topic. <br> Have students complete the Review What You Know prior to beginning instruction on Topic 15 so that you can respond to students' instructional needs. Some students may benefit from additional support using the Item Analysis for Diagnosis and Intervention prior to beginning the topic (TE, p. 806). Consider introducing vocabulary as students encounter terminology in the lessons rather than introducing all terms at the beginning of the lesson (avoid front loading). <br> -continues on next page- |


|  | different quadrilaterals by their sides and angles. | Solve \& Share: Consider providing copies of various quadrilaterals (Teach Tool 21). After introducing the Solve \& Share, discuss the questions provided in the section Build Understanding to help students develop a possible strategy for solving (TE, p. 811). Consider adding non-prototypical shapes. For more details, see the Instructional note at the beginning of this topic. <br> Look Back!: <br> After discussing students' solution methods and reasoning, discuss the Look Back! prompt if those ideas do not already come out during the whole class discussion. <br> Visual Learning: <br> Consider pausing and discussing after the Visual Learning Animation poses the question, "Why are all of these shapes quadrilaterals?" <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning items 11 and 12 "Vocabulary" to provide students with additional opportunities to develop the mathematical language in this topic. |
| :---: | :---: | :---: |
| Enrichment |  |  |
| 3.G.A. 1 <br> MP. 1 <br> MP. 3 <br> MP. 6 | Access Prior Learning: In Topic 15, Grade 2, students learned about polygons and angles. Students have been working with prototypical and nonprototypical shapes and defining attributes since pre-K or Kindergarten. <br> Developing the Big Idea: Students further develop geometric concepts by describing and classify different quadrilaterals using attributes. | Materials: <br> Assorted Shape BLM 44,45 and 46 from: https://tinyurl.com/Topic-15-Shapes <br> Opener: Students work in triads to cut out the shapes from the above masters. Students work as a group to sort the shapes into several categories (open sort of at least four categories). <br> Once all the shapes have been placed into groups, have students rotate to another triad's sort. Have this triad analyze the classification by labeling each group of shapes. Have students create a list of all the attributes the shapes in the group have in common. Ask triads to write a statement on if they agree or disagree with the sort and why. <br> Whole Group Discussion: Choose one triad's work to discuss whole group. Highlight attributes of shapes. When analyzing parallel lines, consider using two straight edges (meter sticks or rulers) to test lines that students think are parallel, yet end up intersecting (when the straight edges are placed on either supposedly parallel line to show the lines will eventually intersect even if they are not intersecting now). |
| Lesson 15-2: Classify Shapes |  |  |
| 3.G.A. 1 <br> MP. 3 <br> MP. 5 <br> MP. 6 <br> MP. 7 <br> MP. 8 | Access Prior Learning: <br> In the previous lesson, students explored classifying shapes using their attributes. This builds from $2^{\text {nd }}$ grade when students recognized and drew space when given specified attributes. <br> Developing the Big Idea: Students further develop geometric concepts by classifying shapes by the number of sides, equal sides, parallel sides, size of angles, and concavity versus convexity. | Instructional note: <br> In third grade, students do not formally measure angles. Students classify based on size of angles from "eye balling" right/square angles. <br> Solve \& Share: <br> Consider assigning the Look Back! to extend students' reasoning of how they sorted the triangles. <br> Visual Learning: <br> During the Visual Learning Animation, consider pausing and discussing the questions: <br> - "How are the groups different?" <br> - "How are the groups alike?" <br> After viewing the Visual Learning Animation consider discussing the prompt provided in Prevent Misconceptions (TE, p. 818). Assign the Convince Me! to check for understanding of the Visual Learning Animation and extend the ideas presented. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 16 "Algebra" to provide distributed practice of "Put Together/Addend Unknown" (see page 88 of NVACS, 2010 for more information of problem types) problem type and algebraic reasoning. <br> Assess \& Differentiate: <br> Consider providing an opportunity for all students to interact with the Math and Science Activity (TE, p. 821A). This activity provides a meaningful experience with identifying and naming polygons based on their attributes. <br> Child watch to identify students who need additional support and pull them into a small group to do the Intervention Activity (TE, p. 821A). Use triangles from master cutouts (see above lesson). |


| Enrichment |  |  |
| :---: | :---: | :---: |
| 3.G.A. 1 <br> MP. 1 <br> MP. 3 <br> MP. 6 | Access Prior Learning: <br> In the previous lesson, students explored classifying quadrilaterals by using their attributes. <br> Developing the Big Idea: Students further develop geometric concepts by classifying shapes into formalized categories in this case parallelograms and quadrilaterals. | Materials: <br> Assorted Shape BLM 44,45 and 46 from: https://tinyurl.com/Topic-15-Shapes (see enrichment after 15-1). <br> Parallelogram vs. Quadrilateral sorting mat: https://tinyurl.com/Topic-15-sort-mat <br> Opener: Students work in partners or triads to sort the shapes using the Parallelogram vs. Quadrilateral sorting mat. After about 6 minutes of exploration, pull the group together and have students share the attributes of a parallelogram. Post or list these on an anchor chart for students to reference. Post the word quadrilateral and have students discuss what a quadrilateral is in their triads (yet don't post attributes yet). Have students analyze their work so far and then continue working. <br> Whole Group Discussion: Have students do a gallery walk to look at the other triads work. Bring students together to discuss their findings. What did students find? What is interesting about this sort? Can they think of a shape that could go into just the parallelogram spot (that would not fit both or either too)? Highlight attributes of shapes. Use two straight edges (meter sticks or rulers) to test lines that students think are parallel. Full lesson available at: https://tinyurl.com/Topic-15-enrichment-lesson) |
| Lesson 15-3: Analyze and Compare Quadrilaterals |  |  |
| 3.G.A. 1 3.MD.C.5b <br> MP. 2 <br> MP. 3 <br> MP. 4 <br> MP. 7 | Access Prior Learning: In previous lessons, students described and classified quadrilaterals. <br> Developing the Big Idea: Students further develop geometric concepts by analyzing and comparing quadrilaterals and group them by their attributes. | Instructional note: A common struggle for students is recognizing that while all squares are rhombuses not all rhombuses are squares. Consider using an ADE day to develop a class anchor chart that represents the hierarchical inclusion of these shapes. This idea refers to the hierarchical inclusion of geometric shapes, for more details on this read the Instructional Note at the beginning of this topic. <br> Solve \& Share: After introducing the Solve \& Share consider asking the questions provided in Build Understanding activate prior learning. <br> Consider assigning the Look Back! prompt to extend student reasoning from the Solve \& Share. <br> Visual Learning: Consider pausing and discussing after the Visual Learning Animation poses the question, "How do you know all the shapes are quadrilaterals?" Consider assigning the Convince Me! to check for understanding of the Visual Learning Animation and extend the ideas presented. <br> Independent Practice/Math Practices and Problem Solving: Consider having students work in partners and triads and to reason about and discuss the problems. Encourage students to discuss, debate, define possible solutions using appropriate and precise mathematical terminology. <br> Assess \& Differentiate: <br> Child watch to identify students who need additional support and pull them in a small group to do the Intervention Activity (TE, p. 827A). <br> *CTC: Quick Check (digital platform) |
| Lesson 15-4: Math Practices and Problem Solving- Precision |  |  |
| MP. 6 <br> MP. 1 <br> MP. 3 <br> MP. 5 <br> MP. 7 <br> 3.G.A. 1 | Access Prior Learning: In previous lessons, students described, classified, analyzed, and compared quadrilaterals. <br> Securing the Big Idea: <br> Students secure the geometric concepts of describing, classifying, analyzing, and comparing quadrilaterals by using accurate language and using appropriate tools. | This lesson provides an opportunity to focus on the Thinking Habits and display the behaviors associated with Math Practice 6. Refer to the Math Practices and Problem Solving Handbook for suggestions on how to develop, connect and assess this Math Practice (TE, pp. F26-F26A, F29). Also reference the handbook in the Student Edition (SE, p. F26). <br> Solve \& Share: Consider reintroducing MP. 6 Thinking Habits (SE p. F26) before introducing the Solve \& Share. Also consider using time students are working on the Solve \& Share as an opportunity to child-watch for behaviors associated with MP.6, that are listed in the Math Practices and Problem Solving Handbook (TE, p. F26A). After discussing student solution methods and reasoning, have students self-score for the behaviors associated with this math practice. <br> Have grid paper, rulers, and index cards (or other tools for making right angles) available. After introducing the Solve \& Share, consider discussing the questions provided in the section Build Understanding to help students develop a possible strategy for solving (TE, p. 829). <br> After discussing students' solution methods and reasoning, consider discussing the Look Back! prompt to support students' development of MP.6. |


|  |  | Assess \& Differentiate: Consider providing an opportunity for all students to interact with the <br> Math and Science Activity (TE, p. 833A). This activity provides a meaningful experience with <br> identifying and naming polygons based on their attributes. |
| :--- | :--- | :--- |
|  | Child watch to identify students who need additional support and pull them in a small group to <br> do the Intervention Activity (TE, p. 833A). <br>  <br>  <br> $\quad$*CTC: Convince Me! (student work samples) |  |

References
Common Core Standards Writing Team. (2013, September 19). Progressions for the Common Core State Standards in Mathematics (draft). K-6, Geometry. Tucson, AZ: Institute for Mathematics and Education, University of Arizona.

Council of Chief State School Officers. (2010). The Nevada Academic Content Standards. Retrieved from http://www.doe.nv.gov/uploadedFiles/nde.doe.nv.gov/content/Standards Instructional Support/Nevada Academic Standards/Math Doc uments/mathstandards.pdf.

Wiest, L. (2015). Lecture 3: Polygons. Reno, NV: University of Nevada, Reno
Van De Walle, J. A., Bay-Williams, J. M., Lovin, L. H., \& Karp, K. S. (2014). Teaching student-centered mathematics: Developmentally appropriate instruction for grades 3-5 (2nd ed.). New York, NY: Pearson.

Additional enrichment activities:

- Graham Fletcher's "Geo-Dotting" (DOK 2 potential when incorporated into whole class discussion)
- Shape-Match (DOK 1, limited to prototypical standard orientations)
- Quadrilateral Riddle Creator (DOK 1)
- Quadrilateral \& Polygon Sort (DOK 2)


## Polygons On The Geoboard

1) Make a 3-sided polygon with 1 square corner and no 2 sides the same length.
2) Make a 4-sided polygon with no parallel sides.
3) Make a 4-sided polygon with all sides different lengths.
4) Make a 4-sided polygon with no square corners but with two pairs of sides parallel.
5) Make a 5-sided polygon that has exactly one pair of parallel sides.
6) Make a 6-sided polygon with three pairs of parallel sides.
7) Make a 6-sided polygon with one pair of sides perpendicular.
8) Make a polygon that is not a square and looks the same no matter on which side you rest the geoboard.
9) Make a polygon with as many sides as is possible on the geoboard.

[^0] https://apps.mathlearningcenter.org/geoboard/.

These are polygons.


These are not polygons.


Which of these are polygons?
A.

B.

C.

D.


Draw some polygons.

Define "polygon."

These are trapezoids:


These are not trapezoids:


Which of these are trapezoids?


Draw something that is a trapezoid.
Draw something that is not a trapezoid.
What is a trapezoid?

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## - Grade 3 Topic 10: Multiply by Multiples of 10

## Big Conceptual Idea: Numbers and Operations in Base Ten, K-5 (p. 12)

Prior to instruction, view the Topic 10 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 571A-571F), the Topic Planner (pp.535A-535B), all 4 lessons, and the Topic Assessments (pp. 569-570A).

| Mathematical | Topic Essential Question: |
| :--- | :--- |
| Background: | What are ways to multiply by multiples of 10? |
| Read Topic 10 Cluster | Reference Answering the Topic Essential Question (TE, pp. 567-568) for key elements of |
| Overview/Math Background <br> (TE, pp. 571A-571F) | Refsers <br> answers to the Essential Question. |

The lesson map for this topic is as follows:

| $10-1$ | $10-2$ | $10-3$ | $10-4$ | Assessment |
| :--- | :--- | :--- | :--- | :--- |


$3^{\text {rd }}$ Grade Curriculum
Pacing Framework: Balanced Calendar

Topic 10 Multiply by Multiples of 10

Number of Lessons: 4

A/D/E: 4 days

NVACS Focus: NBT.A

Total Days: ~8

## Instructional note:

In Topics 1 through 5 students developed conceptual understanding of multiplication and division. These critical mathematical understandings come together in Topic 10 to develop understanding regarding multiplying by a multiple of 10 . Topic 10 is part of a topic cluster with Topics 8 and 9 that share the big idea of using place-value understanding and properties of operations to perform multi-digit arithmetic. A big idea specific to Topic 10 is the place value pattern that exists when multiplying by 10. This understanding will be critical in establishing the "write a zero" rule that is the focus of lesson 10-3.

It is important that the work in this topic not be minimized to having students memorize that they can write a zero and multiply the remaining digits. Teaching the "zero trick" without developing the mathematical understanding behind the rule creates misconceptions when students need to generalize this understanding to working with multiples of 100, 1,000, etc., when confronted with a zero in the middle of a number such as 6,402 and in later grades when students begin working with decimals. Students should understand that a place value is being added to a number when it becomes 10 times greater because of the base-10 place value system.

To help develop this understanding, many learners need to model groups of 10 with the base-ten blocks. For example, in lesson 10-2 the Associative and Distributive Property of Multiplication are used to decompose the multiple of 10. In the Visual Learning Animation, the 20 is decomposed into $2 \times 10$ so that the expression $4 \times 20$ becomes $4 \times 2 \times 10$. Allowing students to build the two different but equivalent expressions with base-ten blocks makes these ideas more accessible and concrete for all students.

## Focus Math Practice 7: Look for and make use of structure

The standard states, "Mathematically proficient students look closely to discern a pattern or structure" (NVACS, 2010, p. 8). To help students work towards security, consider connecting ideas for the "write a zero" rule to our base-10 place value system. Behaviors associated with MP. 7 are described in the Teacher's Edition (TE, pp. F27-F27A) and the Nevada Academic Content Standards for Mathematical Practice.

Looking ahead to the Topic Performance Assessment, students will have to apply strategies for division to answer item 6. Topic 4 developed students' ability to reason and solve for division situations without having to formally divide.

Finally, please note there is an error in the Teacher's Edition on page 567. The error is indicated in the image; the multiplication symbol should be an addition symbol.

```
- Multiplication by multiples of }10\mathrm{ can be shown by using the
    Associative Property of Multiplication to regroup factors. The
    multiple of }10\mathrm{ can be broken into two factors. The Distributive
    Property can also be used to decompose a factor.
    Example:
    Associative Property Distributive Properly
    8\times50=8\times(5\times10) 8\times50=(4+4)\times50
    8\times50=(8\times5)\times10 8 < 50=(4\times50) (2) (4\times50)
    8\times50=40\times10 
- After using different strategies to multiply by multiples of 10,
    students can use a rule: a basic fact can be multiplied first and then
    write one zero after the product.
    Example: To find 7 }\times40\mathrm{ , you can think: 7 }\times4=28
    7\times40=280.
```


## Meaningful Fluency Practice \& Assessment:

For students to attain security with NVACS 3.OA.C. 7 and 3.NBT.A. 2 it is critical that the established meaningful fluency practice and assessment practices continue. Refer to Topic 1 for details about meaningful fluency practice and assessment practices. Topics 1-5 include games for meaningful fluency practice for multiplication and division (NVACS 3.OA.C.7). Topics 8 and 9 include games for meaningful fluency practice for multi-digit addition and subtraction within 1000 (NVACS 3.NBT.A2). The following game will support students developing understanding of multiplying with 10 s and provides sentence frames to support language development necessary for explanations.

## Phase 3: Multiply by Multiples of 10

Materials: set of cards (0-9)
Game board (one for each player)
Sentence frames (one for each player)
Counters and/or Base-10 blocks to support student understanding
Directions: Shuffle the cards and place them face down in a stack. Each player flips over two cards from the top of each stack and places the cards on the empty boxes on the gameboard (at the end of this document) to make the multiplication equation. Each player solves their own equation and explains their thinking, using the sentence frames (at the end of this document), if needed. The player with the largest product earns 1 point. Play continues until a player earns 10 points.

| Essential Academic Vocabulary Use these words consistenty during instruction. |  |
| :---: | :---: |
| New Academic Vocabulary: <br> (First time explicitly taught) | Review Academic Vocabulary: <br> (Vocabulary explicitly taught in prior grades or topics) |
| open number line | equation <br> product <br> multiple <br> Associative Property of Multiplication <br> Distributive Property of Multiplication |

Additional terminology that students may need support with: pattern, relationship, basic fact (see 10-3 Visual Learning Animation for details)

## *Collaborative Team Conversations (CTC)

Consider using one of the following as part of the formative assessment process at the lesson level to collect student work to analyze for evidence of mathematical understanding:

Guiding question: "How are students applying place value understanding to add and subtract whole numbers?"

| Lesson | Evidence |  | Look for |  |
| :---: | :---: | :---: | :---: | :---: |
| 10-2 | Solve \& Share (student work samples) |  | Focus CTC around the big idea: <br> - look for students who explain the properties. <br> - differences and similarities between student examples. <br> - applying multiplication to multiples of 10 and use of basic facts. |  |
| 10-4 | Quick Check Items 1 and 3 | tform) | Focus CTC around data analysis and collection of student workspace (scratch paper). Printable version available under "Teacher Resources". - understanding patterns based on multiples of 10 . |  |
| Learning Cycle Assessments (summative) |  | Topic Assessments SE pp. 567-570 |  |  |


| NVACS <br> (Content and Practices) | Mathematical Development of the Big Idea | Instructional Clarifications \& Considerations |
| :---: | :---: | :---: |
| Lesson 10-1: Use an Open Number Line to Multiply |  |  |
| 3.NBT.A. 3 <br> MP. 2 <br> MP. 4 <br> MP. 7 <br> MP. 8 | Access Prior Learning: <br> In Topic 1, students learned how to use number lines to show multiplication and that multiplication is the joining of equal groups. <br> Developing the Big Idea: <br> Students begin to understand strategies for multiplying by a multiple of 10 by showing the multiplication on an open number line. | Topic Opener: <br> Introduce the Topic Essential Question, "What are ways to multiply by multiples of 10 ?" (TE p. <br> 535). Consider using this question to make an anchor chart with your student. As new ideas are added during the topic, students will see the development of ideas and make connections. <br> You might also consider having students complete the Review What You Know prior to beginning instruction on Topic 10 so that you can respond to students' instructional needs using the Item Analysis for Diagnosis and Intervention (TE, p. 536-537). <br> Consider introducing vocabulary as terms are encountered in the lessons rather than introducing all terms at the beginning of the lesson. <br> -continues on next page- |


|  |  | Solve \& Share: <br> The questions provided in the Build Understanding (TE, p. 539) help students access prior learning in the conventions of using an open number line to show multiplication. Watch for students struggling to find an appropriate strategy and consider asking these questions to scaffold as students are working. <br> If students do not offer a solution method similar to "Alex's Work", then consider discussing "Alex's Work" as a class (TE, p. 539). Alex's work shows an example of using repeated addition to solve for multiplication which helps to make the reasoning accessible to all students. <br> Look Back: <br> To support students' development of MP. 7, consider discussing the Look Back! prompt and, if necessary, providing students with a multiplication table to help them develop conjectures for patterns with the 2's facts, 10's facts, and the facts they solved for in today's Solve \& Share. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning and discussing item 9 to help students develop schema for patterns that can be used when multiplying with 10s. This problem also offers language that can support students' ability to connect multiplying facts they know to multiplying with 10s. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Math and Science Activity with games from previous topics or the Fluency Practice Activity (TE, p. 563). <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 543A). |
| :---: | :---: | :---: |
| Lesson 10-2: Use Properties to Multiply |  |  |
| 3.NBT.A. 3 <br> MP. 1 <br> MP. 3 <br> MP. 6 <br> MP. 7 | Access Prior Learning: <br> In Topic 3, students learned the Associative and Distributive Properties of Multiplication. <br> Developing the Big Idea: Students are further developing their understanding of strategies for multiplying by a multiple of 10 by using their understanding of place value and the properties of multiplication. | Solve \& Share: <br> Watch for students that say that Earl's response is incorrect because he starts his argument with an equation that shows the product on the wrong side (e.g., $30=3 \times 10$ ). These students are misinterpreting the equal sign as a symbol for "the answer goes here" and need support on understanding the equal sign as a symbol that communicates equivalence. <br> Look Back: <br> Consider discussing the Look Back! prompt as a key idea to understanding the use of the Associative Property of Multiplication to get a basic fact. <br> Visual Learning: <br> Consider pausing and discussing strategies to answer, "How can you find the product $4 \times 20$ ?". <br> Convince Me: <br> Consider assigning and discussing the Convince Me! to give students the opportunity to reason with the Associative Property of Multiplication after it's been applied. <br> Independent Practice/Math Practices and Problem Solving: <br> Consider assigning item 16 Number Sense to support students' development of number sense and the application of the Associative Property of Multiplication to reason with numbers. <br> Assess and Differentiate: <br> If time permits, you may consider replacing the Problem Solving Reading Mat with games from previous topics or the Fluency Practice Activity (TE, p. 563). <br> Child-watch to identify students who need additional support and consider the Intervention Activity provided (TE, p. 549A). <br> *CTC: Solve \& Share (student work samples) |
| Lesson 10-3: Multiply by Multiples of 10 le |  |  |
| 3.NBT.A. 3 MP. 1 MP. 3 MP. 4 MP. 5 MP. 7 $M P .8$ | Access Prior Learning In the previous lesson, students used the properties of multiplication to multiply by a multiple of 10 . <br> Securing the Big Idea Students are securing their understanding of strategies for multiplying by a multiple of 10 by using their understanding of place | Solve \& Share: <br> Watch for students that appear to be struggling with $4 \times 50$, as the basic fact ends with zero. For these students have them identify the basic fact product (e.g., 20). An instructional suggestion is offered in Prevent Misconceptions (TE, p. 552). <br> After students have shared their solution methods and reasoning, consider discussing the Look Back! prompt. Ask students to generalize and create a rule for multiplying with 10s based on their observations of patterns in the products in the Solve and Share problems. <br> Visual Learning: <br> Consider discussing the Convince Me! prompt if you feel your students need an additional opportunity to apply the Associative Property of Multiplication for multiplying by multiples of 10. -continues on next page- |



## References

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## Multiply by Multiples of 10



Multiply by Multiples of 10
Sentence Frames

| I know that $\qquad$ times $\qquad$ is $\qquad$ , so $\qquad$ times tens equals $\qquad$ tens or $\qquad$ | I know that $\qquad$ times $\qquad$ is $\qquad$ , so $\qquad$ times tens equals $\qquad$ tens or $\qquad$ |
| :---: | :---: |
| times $\qquad$ means $\qquad$ groups of tens, which is tens or $\qquad$ | $\qquad$ times $\qquad$ means $\qquad$ groups of tens, which is $\qquad$ tens or $\qquad$ |


[^0]:    * To incorporate technology and encourage discussion on 2-dimensional shapes consider using,

