Topic 4

Use Models and Strategies to

Multiply Decimals

Number of lessons: 10 A/D/E: 3 days

NVACS Focus: NBT.B

Total days: ~13

5th grade Curriculum Pacing Framework:

Balanced Calendar

▶ Grade 5 Topic 4: Use Models and Strategies to Multiply Decimals

Big Conceptual Idea: Numbers and Operations in Base Ten (pp. 18-21)

Prior to instruction, view the Topic 4 Professional Development Video located in Pearson Realize online. Read the Teacher's Edition (TE): Cluster Overview/Math Background (pp. 55A-55F), the Topic Planner (pp. 163A-163D), all 10 lessons, and the Topic Assessments (pp. 235-236A).

Mathematical Background:	Topic Essential Question:
Read Topics 2-6 Cluster	What are the standard procedures for estimating and finding
Overview/Math Background	products involving decimals?
(TE, pp. 55A-55F)	
(, pp. co. , co.)	Reference Answering the Topic Essential Questions (TE, pp. 231-232) for key
	elements of answers to the Essential Question.

The lesson map for this topic is as follows:

4-1	4-2	4-3	4-4	4-5	4-6	4-7	4-8	4-9	4-10	Assessment
3 A/D/E days used strategically throughout the topic										

Instructional Note:

The focus of this topic is multiplication with decimals. Instructional emphasis is on "...using concrete models

or drawings and strategies based on place value, properties of operations and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used." (NVACS, 2010, 5.NBT.B.7). Students have prior experience working with decimals, whole number multiplication, and understanding the place value system. Provide students opportunities to analyze patterns and build number sense using decimal factors in a multiplication problem. Students should notice the similarities between multiplication with whole numbers and decimals and how decimals change the size of a product. This conceptual understanding of decimal multiplication will allow students to determine the reasonableness of their solutions and will lay the groundwork for procedural understanding. Use estimation consistently during this topic as a tool to help students develop number sense and connect strategies for working with whole numbers to decimal multiplication (Van de Walle, Karp, & Bay-Williams, 2016).

A common misconception is that multiplication always results in bigger numbers. While this is true when multiplying *whole* numbers, when a number is multiplied by a decimal or fraction that is less than one, the product is *less* than the whole number factor. For example, 2x3 is 2 "**groups of**" 3 = 6. However, 0.2×3 is 0.2 "**of**" 3 = 0.6. A piece of the whole number factor instead of groups; or 6 groups of 0.2 (commutative property). The product is less than one of the factors. This concept will be addressed again in Topic 8 when students multiply fractions.

Throughout this topic, students will benefit from working with visual models while multiplying. Consistently use and be precise with language. Use the language "*of*, *pieces of*, and *two tenths*" (instead of *point two*) when referring to multiplication and decimals. "This level of precision in language will provide your students the opportunity to *hear* the connections between decimals and fractions" (Van de Walle, et al., p 146).

Math Practice 4: Model with mathematics

Focus on opportunities for students to develop *Mathematical Practice 4* behaviors as this is the focus of the Math Practices and Problem Solving, lesson 4-10. Reference the Teacher's Edition (TE, pp. F24-F24A) and the NVACS (2010, p.6).

Essential Academic Vocabulary Use these words consistently during instruction.		
New Academic Vocabulary: Review Academic Vocabulary:		
(First time explicitly taught)	(Vocabulary explicitly taught in prior grades or topics)	
	factors	
	products	
	partial products	
	tenths	
	hundredths	

Additional terminology that students may need support with: base, expanded form, exponential form, standard form, powers of ten

Collaborative Team Conversations (CTC)

Consider using *one* of the following as part of the formative assessment process at the lesson level to **collect student work** to analyze for <u>evidence of mathematical understanding</u>:

Guiding questions: "Are students able to estimate products of whole numbers and decimals? Can they explain why their estimate is reasonable?"

"Are students using a partial products strategy to multiply factors with decimals?"

Lesson	Evidence			Look for
4-2	Convince Me! (student	Convince Me! (student work samples)		lea:
				ce value understanding to justify estimates.
				or the context of a situation.
4-2	Quick Check (digital pla	tform)	Focus CTC around data ana	lysis and collection of student workspace
	Items 1, 2 and 5			rsion available under "Teacher Resources".
4-6	Homework and Practice		Focus CTC around the big ic	dea:
	(student work samples)		appropriate strategies a	and models used to multiply.
	Item 14		 correct placement of the 	e decimal.
4-7	Quick Check (digital pla	Quick Check (digital platform)		lysis and collection of student workspace
			(scratch paper). Printable ve	rsion available under "Teacher Resources".
		-		
	arning Cycle	Topic Performance Assessments		Use Scoring Guide TE pp. 235-236C
Assessn	Assessments (summative)			

Standards listed in **bold** indicate a focus of the lesson.

NVACS (Content and Practices)	Mathematical Development of the Big Idea	Instructional Clarifications & Considerations			
Lesson 4-1: Multiply Decimals by Powers of 10					
5.NBT.A.2	Access Prior Learning: In Topic 1, students worked with powers of ten and explored patterns when multiplying by	Solve and Share: Use questioning to help students connect place value understandings to multiplying with decimals. Students who use structure and mental math are discovering patterns in multiplying decimals by powers of 10. Ask students to share their solutions and explain their thinking. Use			
MP.2 MP.3	powers of ten (5.NBT.A).	questioning to help students to see the patterns in their solutions. Draw out the idea that patterns can be used to multiply by 10, 100, and 1,000.			
MP.7	Beginning of the Big Idea: Students will extend their understandings of place value and multiplication to develop procedural skills and mental strategies for multiplying decimals by powers of ten. Using estimation and procedures, students will build conceptual understanding of decimals as factors.	 Visual Learning: A common misconception is that when multiplying by powers of 10, zeros can be added to find the product. Consider writing whole numbers with the decimal point in places after the ones place. For example, 36 can also be written as 36.0, 36.00, 36.000 without changing the value. It is important that students understand the place value is changing as they explore the movement of the decimal when multiplying by powers of 10. Assess and Differentiate: Students who see patterns in the products when multiplying by powers of 10 will be able to complete the <i>Guided and Independent Practice</i> problems mentally. If students are still having difficulty seeing or applying these patterns mentally, encourage them to use different representations including charts and tables to draw their attention to the patterns. Students will encounter multiplying by powers of 10, with numbers less than 1 such as 0.1 and 0.01 in the practice problems. Students may again need to see the whole numbers written with zeros in place values that are not represented. Showing how the example of 3.63 can be written as 03.63 will help students to see that this number contains no tens but the place value is still there. This gives students a visual for moving the decimal when multiplying 3.63 by 0.1 or 0.01 and connects to the same patterns to mentally calculate the problems in the <i>Guided and Independent Practices and Practice</i> (SE, p. 167), move them to the more challenging problems in the <i>Math Practices and Practice</i> (SE, p. 168) or <i>Homework and Practice</i> (SE, p. 167) to extend their thinking. Ask these students to explain and justify their thinking so that others can benefit from their insights. 			

Lesson 4-2: E	Estimate the product of a decimal	and a whole number
	Access Prior Learning:	Solve and Share:
5.NBT.B.7 MP.2 MP.6 MP.8	Students will use prior experiences with compatible numbers and rounding to estimate (5.NBT.A.4). Developing the Big Idea: Students will build conceptual understanding of decimal as factors through the use of estimation. These understandings will build students number sense and help them to accurately place the decimal point in future problems and to determine when exact products versus an estimate is required.	Students will need to apply what they know about multiplying with whole numbers to multiplying with decimals. Ask students to explain how they arrived at their estimates; as well as, how they know their estimate is reasonable. Ask, "How do you know if your solution will be too high or too low?" Orchestrate a discussion by asking students who used differing estimation strategies to share. This will highlight several strategies and methods used when forming estimations. Consider using the <i>Look Backl</i> to extend student thinking. Allow students to provide explanations for the methods they used and for determining the reasonableness of their solutions. Visual Learning: Focus on the context of this problem and ask students, "What makes an estimate appropriate?" Two different methods are shown for estimating the product. Consider facilitating a discussion about which method is better for this situation and why. Ask students if they can use these ideas to determine whether their solutions are reasonable for future problems. The <i>Convince Mel</i> offers an opportunity for students to apply their ideas using the same context but with different numbers. Assess and Differentiate:
		As students complete the practice problems using estimation techniques, continue to challenge them to use multiple methods and to explain whether their estimation will be higher or lower than the exact answer.
		*CTC: <i>Convince Me!</i> (student work samples) *CTC: <i>Quick Check</i> (digital platform) Items 1, 2 and 5
Lesson 4-3: L	Ise Models to Multiply a Decimal	
	Access Prior Learning:	Solve and Share: Ask students to model the given problem using the hundredths grids or objects. Encourage
5.NBT.B.7	In Topic 2 students added decimals. In Topic 3, students multiplied whole numbers.	students to explain how their models represent the context of the problem. Ask students if their model represents a problem that can be solved using more than one operation and which would
MP.3		be more efficient for this problem. Look for students who use a separate grid for each factor
MP.4	Developing the Big Idea: Students will use a model that	versus those who fit factors together continuously. Consider using multiple colors and a number line in addition to the hundredths grid as visuals to demonstrate how parts join to form wholes.
	encourages repeated addition to multiply a whole number and a decimal. This will help them to extend previous understandings of multiplication to include decimals.	Visual Learning: Students have another opportunity to model a multiplication problem using hundredths grids. Consider having students complete the multiplication problem without the decimals. By comparing the products created by 4 x 36, 4 x 360 and 4 x 3.6, students will connect to previous understanding of patterns and how the decimal is placed when using the U.S. traditional multiplication algorithm.
		Assess and Differentiate: Offer students the use of tools such as base ten blocks or blank hundredths grids as they practice modeling multiplying a whole number by a decimal.
Lesson 4-4: N	lultiply a Decimal by a Whole Nu	
5.NBT.B.7 MP.2	Access Prior Learning: In Topic 3 students estimated and multiplied whole numbers. During Topic 1 students used estimation	Solve and Share: This problem allows students to model with both repeated addition and multiplication. Look for students using multiplicative reasoning on this problem. Some students will be able to represent the different distances in a table and express the rule t x 1.15=d (km). Why is multiplication used to solve this problem?
MP.5	to round decimals. They will use	used to solve this problem?
MP.5 MP.6	these concepts together to multiply a decimal by a whole number.	Visual Learning:
MP.6 MP.8	a ucumai by a whole number.	Students are shown that it is possible to multiply the factors without a decimal and then place the decimal into the product. Placing the decimal is not given as a rule. The focus is on using
	Developing the Big Idea: Students will use understandings of multiplication and decimal place value to multiply a whole number and a decimal using a known algorithm and then correctly place the decimal in the product.	number sense and place value understanding to place the decimal as table. The focus is on using numbers. Consider having students generalize a rule based on the patterns in the given examples. Allow students to use different algorithms or strategies such as an area model for multi-digit multiplication. Ask students to use place value understanding and number sense to explain where the decimal is placed and why these methods work to efficiently multiply decimals. Ensure that students build a conceptual understanding prior to being given an abstract rule.
		Assess and Differentiate: Students should work to see the connection between multiplying whole numbers and decimals. If they are multiplying and placing the decimal with precision, indicating conceptual understanding, they might move to the <i>Math Practices and Problem Solving</i> page to practice with applying their understanding to contextualized problems.

Lesson 4-5: U	Ise Models to Multiply a Decimal	and a Decimal
	Access Prior Learning:	Solve and Share:
5.NBT.B.7 MP.3	In fourth grade students used area models to multiply whole numbers (4.NBT.B.5) and in Topic 3 students used area models to	Students will benefit from discussing the value one small square of this grid (1/100) represents before modeling this problem. Note that this problem asks for one possible solution. Consider having students share different plausible solutions and discuss why they are multiple solutions. Help students make connections to pervious understandings about factors.
MP.4	multiply multi-digit whole numbers.	
MP.5	manipity manifestion in an electron	Visual Learning: The students will see how overlapping two decimals in the hundredths grid gives a solution to a
MP.6 MP.8	Developing the Big Idea: Students will multiply two decimal factors for the first time building on the understanding that when one factor is less than one, the product is less than the larger factor. Students will work with two decimal factors to discover how the product is affected.	decimal multiplication problem. The word "of" can help students to understand what this model is demonstrating and why it works. 2 x 3 is 2 groups "of" 3. Decimals are less than 1, so they take a piece "of" a whole number. Two decimals multiplied together finds a piece "of" a piece. The overlap created on the hundredths grid model visually shows the size of the piece created when two decimals are multiplied. This will later connect to multiplication of fractions. Part C will use two hundredths grids side by side because one of the factors is 1.5. Students often have trouble modeling numbers greater than one when using hundredths grids. Ask students if they can rename the 1.5 into an equivalent value to assist them with thinking about this. Ask students if renaming 1.5 to 15 tenths changes its value. This will help students understand the multiple ways they can reason about value and that either way enables them to use this model to multiply decimals, even when whole numbers are included. (Note: Continue to explore equivalent names for 100 hundredths or 10 tenths to solidify understanding that either of these will make a whole unit and thus 1 "whole" hundredths grid).
	ultinh, Desimale Using Derticl D	Assess and Differentiate: Allow students to use a variety of tools such as blank hundredths grids or base 10 blocks to complete the <i>Guided and Independent Practice</i> problems (<i>Teaching Tools 8 and 9, Teacher's</i> <i>Resource Masters Volume 2</i>). Students will work with numbers greater than 1 on items 4, 7, 8, 10, 11, 14, and 16 (SE, pp. 191-192). Strong base-ten understanding will help students think fluidly about number. Help students make connections between numbers such as 2.1 as 21 tenths and 1.7 as 17 tenths. This understanding of equivalency will help students to see how these numbers can be represented on the hundredths grid models while supporting deeper number sense.
Lesson 4-6: IV	Iultiply Decimals Using Partial Pr	
5.NBT.B.7 MP.1 MP.2 MP.4	Access Prior Learning: In Topic 3 students used partial products strategies such as an area model to multiply two digit numbers. Developing the Big Idea:	Solve and Share: Students will use a visual model to multiply two decimal factors, which represents partial products created. Students should connect how strategies for multiplying decimals are similar to those used for whole numbers. Ask students to think about the <i>Look Back!</i> question and share their observations. Draw out the mathematical generalization that the product of two decimals less than one is less than either factor. Visual Learning:
MP.5	Students will develop conceptual understanding while building procedural skills for multiplying decimals using a partial products strategy.	An area model is used to visually show the partial products created by multiplying two decimals. Consider asking students to complete the same multiplication problem without the decimals using an area model. Students will be able to see the similarities between the partial products created by both problems and use place value reasoning to think about how decimals are placed in the product created by the decimal factors. Ask students if the example seen here confirms, denies, or changes the generalizations made about the product when multiplying two decimals less than one.
		Guided and Independent Practice: Have students solve these problems on a blank page to allow use of visual model strategies such as the open area model demonstrated in the <i>Visual Learning Bridge</i> .
		Assess and Differentiate: The intervention activity models a partial products strategy that could increase conceptual understanding of multiplication for all students. This partial products algorithm does not hide place value. Instead, it shows all of the partial products and is procedurally similar to other standard algorithms for multiplication, including the U.S. traditional algorithm.
		*CTC: Homework and Practice (student work samples) Item 14

Lesson 4.7.11	se Properties to Multiply Decima	als
	Access Prior Learning:	Solve and Share:
5.NBT.B.7 MP.1	Students have worked with the associative and commutative properties in previous grades	Estimating will help students to use the context of the problem and think about reasonable solutions. Providing a blank hundredths grid to students will remind them that they can use visual models to multiply decimals. Look for students who use properties to break apart the
MP.2	(4.NBT.B.5) and topics.	decimals and multiply. If needed, project and share the student sample titled "Javier's work" provided in <i>Analyze Student Work</i> (TE, p. 201).
MP.6	Developing the Big Idea:	Visual Learning:
MP.7	Students will develop conceptual understanding of multiplication with decimals through use of the associative and commutative properties. Important conceptual understandings are built in	Several understandings need to be used together to understand the example shown. Students need to understand that decimals can be written as equivalent fractions, rewritten as a whole number times a fraction using the associative property, and that the commutative property states you can change the order of the factors. Students can utilize these properties to decompose decimal factors and use number sense to multiply.
	preparation for use of the standard algorithm to multiply decimals. Connections are made between	Assess and Differentiate: The Intervention Activity provides steps for using properties to multiply decimals. Use these steps as a scaffold to help students connect the different concepts being used in this lesson.
	fractions and decimals.	*CTC: Quick Check (digital platform)
Lesson 4-8: U	se Number Sense to Multiply De	
5.NBT.B.7	Access Prior Learning: In previous lessons students have multiplied whole numbers and decimals. They have also estimated products using decimals.	Solve and Share: The digits that make up the products of several decimal multiplication problems are given. Students will need to think about the size of the factors and reason to place the decimals in these products. Facilitate discussion around student reasoning about how factors affect the size of products.
MP.2	Developing the Division	Visual Learning:
MP.3 MP.8	Developing the Big Idea: Students will build conceptual understanding of decimal	Build on students' ideas from the <i>Solve and Share</i> to create generalizations about how the size of decimal factors can help us to place the decimal.
	multiplication through using number sense and estimation to correctly place decimals in a product.	Guided and Independent Practice: Ask students to connect how they might use whole number strategies to reason about decimal placement. This will build conceptual understanding of decimal multiplication and lay the groundwork for the standard multiplication algorithms. Students may choose to use whole number strategies and place the decimals using reasoning.
Lesson 4-9: M	lultiply Decimals	
	Access Prior Learning:	Solve and Share:
5.NBT.B.7 MP.1	In previous lessons students used models and partial products strategies to multiply decimals.	Consider setting parameters for this <i>Solve and Share</i> such as asking students to use 0.5 as a factor for a portion of their created problems. This will help to keep the discussion focused. Students should notice that there are several ways to find the product of two decimals which includes using whole numbers and then reasoning about the numbers or counting the number
	They have used estimation and	of decimal places in the factors.
MP.3	reasoning to place the decimal in products.	
MP.6		Visual Learning: The U.S. traditional algorithm is shown using decimal factors. Estimating a reasonable answer
MP.7	Securing the Big Idea:	before calculating will help students to remember to use reasoning and number sense as they
MP.8	Students will use a standard algorithm to build procedural knowledge of multiplying decimals.	also learn the procedure of counting decimal places in the factors to place the decimal. In <i>Another Example</i> , the U.S. traditional algorithm is used to explicitly model the problem. Students are shown to count decimal places in the factors after using the same algorithm with whole numbers. Avoid showing any rules until you are confident that students have the conceptual understanding to know why they work.
	algorithm to build procedural knowledge of multiplying decimals. ath Practices and Problem Solving-	Another Example, the U.S. traditional algorithm is used to explicitly model the problem. Students are shown to count decimal places in the factors after using the same algorithm with whole numbers. Avoid showing any rules until you are confident that students have the conceptual understanding to know why they work. Model with Math
Lesson 4-10: M 5.NBT.B.7 MP.1	algorithm to build procedural knowledge of multiplying decimals. ath Practices and Problem Solving- Access Prior Learning: Students have worked to represent real world contexts using mathematical expressions in	Another Example, the U.S. traditional algorithm is used to explicitly model the problem. Students are shown to count decimal places in the factors after using the same algorithm with whole numbers. Avoid showing any rules until you are confident that students have the conceptual understanding to know why they work. Model with Math Solve and Share: Models used to represent this problem may be visual models or numerical expressions. Ask students to explain how their models represent the context of the problem. Share students' models and facilitate a discussion about how different models are useful for analyzing and solving problems. Facilitate a discussion about how using models promotes the habits that
Lesson 4-10: M 5.NBT.B.7	algorithm to build procedural knowledge of multiplying decimals. ath Practices and Problem Solving- Access Prior Learning: Students have worked to represent real world contexts using	Another Example, the U.S. traditional algorithm is used to explicitly model the problem. Students are shown to count decimal places in the factors after using the same algorithm with whole numbers. Avoid showing any rules until you are confident that students have the conceptual understanding to know why they work. Model with Math Solve and Share: Models used to represent this problem may be visual models or numerical expressions. Ask students to explain how their models represent the context of the problem. Share students' models and facilitate a discussion about how different models are useful for analyzing and
Lesson 4-10: M 5.NBT.B.7 MP.1	algorithm to build procedural knowledge of multiplying decimals. ath Practices and Problem Solving- Access Prior Learning: Students have worked to represent real world contexts using mathematical expressions in	Another Example, the U.S. traditional algorithm is used to explicitly model the problem. Students are shown to count decimal places in the factors after using the same algorithm with whole numbers. Avoid showing any rules until you are confident that students have the conceptual understanding to know why they work. Model with Math Solve and Share: Models used to represent this problem may be visual models or numerical expressions. Ask students to explain how their models represent the context of the problem. Share students' models and facilitate a discussion about how different models are useful for analyzing and solving problems. Facilitate a discussion about how using models promotes the habits that

Assess and Differentiate:
The Intervention Activity calls for students to use play money as a scaffold to model a
mathematical situation. Consider using a manipulative or tool throughout all components of this
lesson to build conceptual understanding.

References

Council of Chief State School Officers. (2010). The Nevada Academic Content Standards. Retrieved from <u>http://www.doe.nv.gov/uploadedFiles/nde.doe.nv.gov/content/Standards_Instructional_Support/Nevada_Academic_Standards/</u> <u>Math_Documents/mathstandards.pdf</u>.

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